# Edexcel Maths Core 2 

Mark Scheme Pack

2005-2013

## GCE

Edexcel GCE
Core Mathematics C2 (6664)

Summer 2005

Mark Scheme (Results)

J une 2005
6664 Core Mathematics C2

## Mark Scheme

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 1. | $\begin{array}{ll} \frac{\mathrm{d} y}{\mathrm{~d} x}=4 x-12 & \\ 4 x-12=0 & x=3 \\ & y=-18 \end{array}$ | B1 <br> M1 A1ft <br> A1 <br> (4) |
|  | M1: Equate $\frac{\mathrm{d} y}{\mathrm{~d} x}$ (not just $y$ ) to zero and proceed to $x=\ldots$ <br> A1ft: Follow through only from a linear equation in $x$. <br> Alternative: <br> Alternative: <br> $(x-3)^{2} \quad$ B1 for $(x-3)^{2}$ seen somewhere $y=2\left(x^{2}-6 x\right)=2\left\{(x-3)^{2}-9\right\} \quad x=3$ <br> M1 for attempt to complete square and deduce $x=\ldots$ <br> A1ft $\left[(x-a)^{2} \Rightarrow x=a\right]$ $y=-18$ <br> A1 |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 2. | (a) $x \log 5=\log 8, \quad x=\frac{\log 8}{\log 5}, \quad=1.29$ <br> (b) $\log _{2} \frac{x+1}{x} \quad\left(\right.$ or $\left.\log _{2} 7 x\right)$ <br> $\frac{x+1}{x}=7 \quad x=\ldots, \quad \frac{1}{6} \quad$ (Allow 0.167 or better) | $\begin{array}{ll} \text { M1, A1, A1 (3) } \\ \text { B1 } & \\ \text { M1, A1 } & \text { (3) }  \tag{3}\\ & \mathbf{6} \end{array}$ |
|  | (a) Answer only 1.29 : Full marks. <br> Answer only, which rounds to 1.29 (e.g. 1.292): M1 A1 A0 <br> Answer only, which rounds to 1.3 : M1 A0 A0 <br> Trial and improvement: Award marks as for "answer only". <br> (b) M1: Form (by legitimate log work) and solve an equation in $x$. Answer only: No marks unless verified (then full marks are available). |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 3. | (a) Attempt to evaluate $\mathrm{f}(-4)$ or $\mathrm{f}(4)$ $\begin{equation*} f(-4)=2(-4)^{3}+(-4)^{2}-25(-4)+12 \quad(=128+16+100+12)=0, \tag{2} \end{equation*}$ <br> so ..... is a factor. <br> (b) $(x+4)\left(2 x^{2}-7 x+3\right)$ $\ldots \ldots \ldots .(2 x-1)(x-3)$ | M1 <br> A1 <br> M1 A1 <br> M1 A1 <br> (4) |
|  | (b) First M requires $\left(2 x^{2}+a x+b\right), a \neq 0, b \neq 0$. <br> Second $M$ for the attempt to factorise the quadratic. <br> Alternative: <br> $(x+4)\left(2 x^{2}+a x+b\right)=2 x^{3}+(8+a) x^{2}+(4 a+b) x+4 b=0$, then compare coefficients to find values of $a$ and $b$. [M1] $\begin{equation*} \overline{a=-7}, b=3 \tag{A1} \end{equation*}$ <br> Alternative: <br> Factor theorem: Finding that $\mathrm{f}\left(\frac{1}{2}\right)=0, \therefore(2 x-1)$ is a factor $\quad[\mathrm{M} 1, \mathrm{~A} 1]$ n.b. Finding that $\mathrm{f}\left(\frac{1}{2}\right)=0, \therefore\left(x-\frac{1}{2}\right)$ is a factor scores M1, A0 , unless the factor 2 subsequently appears. <br> Finding that $\mathrm{f}(3)=0, \therefore(x-3)$ is a factor <br> [M1, A1] |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 4. | (a) $1+12 p x,+\frac{12 \times 11}{2}(p x)^{2}$ $\begin{gathered} \text { (b) } 12 p(x)=-q(x) \quad 66 p^{2}\left(x^{2}\right)=11 q\left(x^{2}\right) \\ \Rightarrow \quad 66 p^{2}=-132 p \\ p=-2, \quad q=24 \end{gathered}$ <br> (Equate terms, or coefficients) <br> (Eqn. in $p$ or $q$ only) | B1, B1  <br> M1  <br> M1  <br> A1, A1 $(4)$ <br>  6 |
|  | (a) Terms can be listed rather than added. <br> First B1: Simplified form must be seen, but may be in (b). <br> (b) First M: May still have $\binom{12}{2}$ or ${ }^{12} C_{2}$ <br> Second M: Not with $\binom{12}{2}$ or ${ }^{12} C_{2}$. Dependent upon having $p$ 's in each term. Zero solutions must be rejected for the final A mark. |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 5. |  | B1  <br> M1  <br> M1 A1 (4) <br> B1  <br> M1  <br> M1 A1 (4) <br>  $\mathbf{8}$ |
|  | (a) First M: Must be subtracting from 180 before subtracting 10. <br> (b) First M: Must be subtracting from 360 before dividing by 2, or dividing by 2 then subtracting from 180. <br> In each part: <br> Extra solutions outside 0 to 180 : Ignore. <br> Extra solutions between 0 and 180 : A0. <br> Alternative for (b): (double angle formula) $\begin{array}{ccl} 1-2 \sin ^{2} x=-0.9 & 2 \sin ^{2} x=1.9 & \text { B1 } \\ & \sin x=\sqrt{0.95} & \text { M1 } \\ x=77.1 & \\ & x=180-77.1=102.9 & \text { M1 A1 } \end{array}$ |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 6. | (a) Missing $y$ values: $1.6(00) 3.3(00)$ <br> (b) $(A=) \frac{1}{2} \times 4,\{(0+0)+2(1.6+2.771+3.394+3.2)\}$ $=43.86 \text { (or a more accurate value) } \quad(\text { or } 43.9, \text { or } 44)$ $\begin{aligned} \text { (c) Volume } & =A \times 2 \times 60 \\ & \left.=5260\left(\mathrm{~m}^{3}\right) \quad \text { (or } 5270, \text { or } 5280\right) \end{aligned}$ | B1 <br> B1 <br> (2) <br> B1, M1 A1ft <br> A1 (4) <br> M1 <br> A1 <br> (2) |
|  | (b) Answer only: No marks. <br> (c) Answer only: Allow. (The M mark in this part can be "implied"). |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 7. | (a) $\frac{\sin x}{8}=\frac{\sin 0.5}{7}$ or $\frac{8}{\sin x}=\frac{7}{\sin 0.5}, \quad \sin x=\frac{8 \sin 0.5}{7}$ $\sin x=0.548$ <br> (b) $\begin{aligned} & x=0.58 \quad(\alpha) \\ & \pi-\alpha=2.56 \end{aligned}$ <br> (This mark may be earned in (a)). |  |
|  | (a) M: Sine rule attempt (sides/angles possibly the "wrong way round"). A1ft: follow through from sides/angles are the "wrong way round". <br> Too many d.p. given: <br> Maximum 1 mark penalty in the complete question. (Deduct on first occurrence). |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 8. | (a) Centre $(5,0)$ <br> (or $x=5, y=0$ ) <br> (b) $(x \pm a)^{2} \pm b \pm 9+(y \pm c)^{2}=0 \Rightarrow r^{2}=\ldots$ or $r=\ldots \quad$, Radius $=4$ <br> (c) $(1,0),(9,0) \quad$ Allow just $x=1, x=9$ <br> (d) Gradient of $A T=-\frac{2}{7}$ $y=-\frac{2}{7}(x-5)$ | B1 B1 <br> M1, A1 <br> (2) B1ft, B1ft <br> (2) <br> B1 <br> M1 A1ft <br> (3) |
|  | (a) $(0,5)$ scores B1 B0. <br> (d) M1: Equation of straight line through centre, any gradient (except 0 or $\infty$ ) (The equation can be in any form). <br> A1ft: Follow through from centre, but gradient must be $-\frac{2}{7}$. |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 9. | (a) $\begin{array}{lcc} (S=) a+a r+\ldots+a r^{n-1} & " S=" \text { not required. } & \text { Addition required. } \\ (r S=) a r+a r^{2}+\ldots+a r^{n} & " r S=" \text { not required } \quad(\text { M: Multiply by } r) \\ S(1-r)=a\left(1-r^{n}\right) \quad S=\frac{a\left(1-r^{n}\right)}{1-r} \quad \text { (M: Subtract and factorise) } \quad\left(^{*}\right) \end{array}$ <br> (b) $a r^{n-1}=35000 \times 1.04^{3}=39400$ <br> (M: Correct $a$ and $r$, with $n=3,4$ or 5 ). <br> (c) $n=20$ <br> (Seen or implied) $S_{20}=\frac{35000\left(1-1.04^{20}\right)}{(1-1.04)}$ <br> (M1: Needs any $r$ value, $a=35000, n=19,20$ or 21). <br> (A1ft: ft from $n=19$ or $n=21$, but $r$ must be 1.04). $\text { = } 1042000$ | B1 <br> M1 <br> M1 A1cso (4) <br> M1 A1 (2) <br> B1 <br> M1 A1ft <br> A1 <br> (4) |
|  | (a) B1: At least the 3 terms shown above, and no extra terms. <br> A1: Requires a completely correct solution. <br> Alternative for the 2 M marks: <br> M1: Multiply numerator and denominator by $1-r$. <br> M1: Multiply out numerator convincingly, and factorise. <br> (b) M1 can also be scored by a "year by year" method. Answer only: 39400 scores full marks, 39370 scores M1 A0. <br> (c) M1 can also be scored by a "year by year" method, with terms added. <br> In this case the B 1 will be scored if the correct number of years is considered. <br> Answer only: Special case: 1042000 scores 2 B marks, scored as $1,0,0,1$ (Other answers score no marks). <br> Failure to round correctly in (b) and (c): <br> Penalise once only (first occurrence). |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 10. | (a) <br> $\int\left(2 x+8 x^{-2}-5\right) \mathrm{d} x=x^{2}+\frac{8 x^{-1}}{-1}-5 x$ <br> $\left[x^{2}+\frac{8 x^{-1}}{-1}-5 x\right]_{1}^{4}=(16-2-20)-(1-8-5)$ <br> $x=1: y=5$ and $x=4: y=3.5$ <br> Area of trapezium $=\frac{1}{2}(5+3.5)(4-1) \quad(=12.75)$ <br> Shaded area $=12.75-6=6.75$ <br> (M: Subtract either way round) <br> (b) $\frac{\mathrm{d} y}{\mathrm{~d} x}=2-16 x^{-3}$ <br> (Increasing where) $\frac{\mathrm{d} y}{\mathrm{~d} x}>0$; For $x>2, \frac{16}{x^{3}}<2, \therefore \frac{\mathrm{~d} y}{\mathrm{~d} x}>0$ <br> (Allow $\geq$ ) | M1 A1 A1 <br> M1 <br> B1 <br> M1 <br> M1 A1 <br> (8) <br> M1 A1 <br> dM1; A1 |
|  | (a) Integration: One term wrong M1 A1 A0; two terms wrong M1 A0 A0. Limits: M1 for substituting limits 4 and 1 into a changed function, and subtracting the right way round. <br> Alternative: $x=1: y=5 \text { and } x=4: y=3.5$ <br> Equation of line: $y-5=-\frac{1}{2}(x-1) \quad y=\frac{11}{2}-\frac{1}{2} x$, subsequently used in integration with limits. $\begin{aligned} & \left(\frac{11}{2}-\frac{1}{2} x\right)-\left(2 x+\frac{8}{x^{2}}-5\right) \\ & \int\left(\frac{21}{2}-\frac{5 x}{2}-8 x^{-2}\right) \mathrm{d} x=\frac{21 x}{2}-\frac{5 x^{2}}{4}-\frac{8 x^{-1}}{-1} \end{aligned}$ <br> (M: Subtract either way round) <br> (Penalise integration mistakes, not algebra for the ft marks) $\left[\frac{21 x}{2}-\frac{5 x^{2}}{4}-\frac{8 x^{-1}}{-1}\right]_{1}^{4}=(42-20+2)-\left(\frac{21}{2}-\frac{5}{4}+8\right)$ <br> (M: Right way round) <br> Shaded area $=6.75$ <br> (The follow through marks are for the subtracted version, and again deduct an accuracy mark for a wrong term: One wrong M1 A1 A0; two wrong M1 A0 A0.) <br> Alternative for the last 2 marks in (b): <br> M1: Show that $x=2$ is a minimum, using, e.g., $2^{\text {nd }}$ derivative. <br> A1: Conclusion showing understanding of "increasing", with accurate working. | $3^{\text {rd }} \mathrm{M} 1$ $4^{\text {th }} \text { M1 }$ <br> $1^{\text {st }}$ M1 A1ft A1ft $2^{\text {nd }} \mathrm{M} 1$ A1 |

## GCE <br> Edexcel GCE <br> Core Mathematics C2 (6664)

J anuary 2006

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| Question number | Scheme |  |  | Marks |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | (a) $2+1-5+c=0 \quad$ or | $-2+c=0$ |  | M1 |  |
|  | $\underline{c=2}$ |  |  | A1 | (2) |
|  | (b) $\mathrm{f}(\mathrm{x})=(\mathrm{x}-1)\left(2 x^{2}+3 x-2\right)$ |  | $(x-1)$ | B1 |  |
|  |  |  | division | M1 |  |
|  | $=\ldots(2 x-1)(x+2)$ |  |  | M1 A1 | (4) |
|  | (c) f $\left(\frac{3}{2}\right)=2 \times \frac{27}{8}+\frac{9}{4}-\frac{15}{2}+c$ |  |  | M1 |  |
|  | Remainder $=c+1.5 \quad \underline{3.5}$ |  | ft their c | A1ft | (2) |

(a) M1 for evidence of substituting $x=1$ leading to linear equation in $c$
(b) $\quad \mathrm{B} 1 \quad$ for identifying $(x-1)$ as a factor
$1^{\text {st }}$ M1 for attempting to divide.
Other factor must be at least $\left(2 x^{2}+\right.$ one other term $)$
$2^{\text {nd }}$ M1 for attempting to factorise a quadratic resulting from attempted division
A1 for just $(2 x-1)(x+2)$.
(c) M1 for attempting $\mathrm{f}\left( \pm \frac{3}{2}\right)$. If not implied by $1.5+c$, we must see some substitution of $\pm \frac{3}{2}$.

A1 follow through their $c$ only, but it must be a number.

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 2. | (a) $(1+p x)^{9}=1+9 p x ;+\binom{9}{2}(p x)^{2}$ <br> (b) $9 p=36$, so $p=4$ <br> $q=\frac{9 \times 8}{2} p^{2} \quad$ or $\quad 36 p^{2} \quad$ or $36 p$ if that follows from their (a) <br> So $q=576$ | B1 B1 <br> M1 A1 <br> M1 <br> A1cao |
| N.B. | (a) $2^{\text {nd }}$ B1 for $\binom{9}{2}(p x)^{2}$ or better. Condone "," not " + ". <br> (b) $1^{\text {st }} \mathrm{M} 1$ for a linear equation for $p$. <br> $2^{\text {nd }}$ M1 for either printed expression, follow through their $p$. <br> $1+9 p x+36 p x^{2}$ leading to $p=4, q=144$ scores B1B0 M1A1M1A0 i.e 4/6 |  |
| 3. | (a) $\begin{aligned} (A B)^{2} & =(4-3)^{2}+(5)^{2} \quad[=26] \\ A B & =\underline{\sqrt{26}} \end{aligned}$ <br> (b) $\begin{aligned} p & =\left(\frac{4+3}{2}, \frac{5}{2}\right) \\ & =\left(\frac{7}{2}, \frac{5}{2}\right) \end{aligned}$ <br> (c) $\quad\left(x-x_{p}\right)^{2}+\left(y-y_{p}\right)^{2}=\left(\frac{A B}{2}\right)^{2}$ $(x-3.5)^{2}+(y-2.5)^{2}=6.5$ | M1  <br> M1  <br> M1  <br> M1  <br> M1  <br> A1 c.a.o  |
|  | (a) M1 for an expression for $A B$ or $A B^{2}$ N.B. $\left(x_{1}+x_{2}\right)^{2}+\ldots$ is M0 <br> (b) M1 for a full method for $x_{p}$ <br> (c) $1^{\text {st }} \mathrm{M} 1 \quad$ for using their $x_{p}$ and $y_{p}$ in LHS <br> $2^{\text {nd }}$ M1 for using their $A B$ in RHS <br> N.B. $x^{2}+y^{2}-7 x-5 y+12=0$ scores, of course, $3 / 3$ for part (c). <br> Condone use of calculator approximations that lead to correct answer given. |  |




| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 6. | (a) $\quad t=15 \quad 25 \quad 30$ <br> (b) $\begin{aligned} S & \approx \frac{1}{2} \times 5 ;[0+15.37+2(1.22+2.28+3.80+6.11+9.72)] \\ & =\frac{5}{2}[61.63]=154.075=\text { AWRT } \underline{154} \end{aligned}$ | $\begin{aligned} & \text { B1 B1 B1 } \\ & \text { B1 [M1] } \\ & \text { A1 } \end{aligned}$ |
|  | (a) S.C. Penalise AWRT these values once at first offence, thus the following marks could be AWRT 2 dp (Max 2/3) |  |





## GENERAL PRINCIPLES FOR C1 \& C2 MARKING

## Method mark for solving 3 term quadratic:

1. Factorisation
$\left(x^{2}+b x+c\right)=(x+p)(x+q)$, where $|p q|=|c|$, leading to $x=\ldots$
$\left(a x^{2}+b x+c\right)=(m x+p)(n x+q)$, where $|p q|=|c|$ and $|m n|=|a|$, leading to $x=\ldots$

## 2. Formula

Attempt to use correct formula (with values for $a, b$ and $c$ ).
3. Completing the square

Solving $x^{2}+b x+c=0: \quad(x \pm p)^{2} \pm q \pm c, \quad p \neq 0, q \neq 0, \quad$ leading to $x=\ldots$

## Method marks for differentiation and integration:

## 1. Differentiation

Power of at least one term decreased by 1. $\left(x^{n} \rightarrow x^{n-1}\right)$

## 2. Integration

Power of at least one term increased by 1. $\left(x^{n} \rightarrow x^{n+1}\right)$

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.
Normal marking procedure is as follows:
Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.
Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but will be lost if there is any mistake in the working.

## Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

## Answers without working

The rubric says that these may gain no credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required. Most candidates do show working, but there are occasional awkward cases and if the mark scheme does not cover this, please contact your team leader for advice.

## Misreads

A misread must be consistent for the whole question to be interpreted as such.
These are not common. In clear cases, please deduct the first 2 A (or B) marks which would have been lost by following the scheme. (Note that 2 marks is the maximum misread penalty, but that misreads which alter the nature or difficulty of the question cannot be treated so generously and it will usually be necessary here to follow the scheme as written).
Sometimes following the scheme as written is more generous to the candidate than applying the misread rule, so in this case use the scheme as written.
If in doubt please send to review or refer to Team Leader.

## GCE

## Edexcel GCE

Core Mathematics C2 (6664)

## J une 2006

Mark Scheme
(Results)

J une 2006
6664 Core Mathematics C2
Mark Scheme

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 1. | $\begin{align*} (2+x)^{6}=64 & \ldots \\ & +\left(6 \times 2^{5} \times x\right)+\left(\frac{6 \times 5}{2} \times 2^{4} \times x^{2}\right), \quad+192 x,+240 x^{2} \tag{4} \end{align*}$ | B1 M1, A1, A1 |
|  | The terms can be 'listed' rather than added. <br> M1: Requires correct structure: ‘binomial coefficients’ (perhaps from Pascal’s triangle), increasing powers of one term, decreasing powers of the other term (this may be 1 if factor 2 has been taken out). Allow 'slips'. $\binom{6}{1} \text { and }\binom{6}{2} \text { or equivalent are acceptable, or even }\left(\frac{6}{1}\right) \text { and }\left(\frac{6}{2}\right) .$ <br> Decreasing powers of $x$ : <br> Can score only the M mark. <br> $64(1+\ldots . . . .$.$) , even if all terms in the bracket are correct, scores max. B1M1A0A0.$ |  |




| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 4. | (a) $\begin{aligned} f(-2) & =2(-2)^{3}+3(-2)^{2}-29(-2)-60 \\ & =-16+12+58-60=-6 \end{aligned}$ <br> (b) $f(-3)=2(-3)^{3}+3(-3)^{2}-29(-3)-60$ <br> M: Attempt $f(3)$ or $f(-3)$ $(=-54+27+87-60) \quad=0 \quad \therefore(x+3)$ is a factor <br> (c) $\begin{aligned} & (x+3)\left(2 x^{2}-3 x-20\right) \\ & =(x+3)(2 x+5)(x-4) \end{aligned}$ | M1  <br> A1 (2) <br> M1  <br> A1 (2) <br> M1 A1  <br> M1 A1 (4) <br>  8 |
|  | (a) Alternative (long division): <br> Divide by $(x+2)$ to get $\left(2 x^{2}+a x+b\right), a \neq 0, b \neq 0$. [M1] <br> $\left(2 x^{2}-x-27\right), \quad$ remainder $=-6$ <br> [A1] <br> (b) A1 requires zero and a simple conclusion (even just a tick, or Q.E.D.). <br> (c) First M requires division by $(x+3)$ to get $\left(2 x^{2}+a x+b\right), a \neq 0, b \neq 0$. <br> Second M for the attempt to factorise their quadratic. <br> Usual rule: $\left(2 x^{2}+a x+b\right)=(2 x+c)(x+d)$, where $\|c d\|=\|b\|$. <br> Alternative (first 2 marks): <br> $(x+3)\left(2 x^{2}+a x+b\right)=2 x^{3}+(6+a) x^{2}+(3 a+b) x+3 b=0$, then compare <br> coefficients to find values of $a$ and $b$. [M1] $\overline{a=-3}, b=-20 \quad[\mathrm{~A} 1]$ <br> Alternative: <br> Factor theorem: Finding that $\mathrm{f}\left(-\frac{5}{2}\right)=0 \therefore$ factor is, $(2 x+5) \quad$ [M1, A1] <br> Finding that $\mathrm{f}(4)=0 \therefore$ factor is, $\quad(x-4) \quad$ [M1, A1] <br> "Combining" all 3 factors is not required. <br> If just one of these is found, score the first 2 marks M1 A1 M0 A0. <br> Losing a factor of 2: $(x+3)\left(x+\frac{5}{2}\right)(x-4)$ scores M1 A1 M1 A0. <br> Answer only, one sign wrong: e.g. $(x+3)(2 x-5)(x-4)$ scores M1 A1 M1 A0. |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 5. | (a) <br> Shape $(0,1)$, or just 1 on the $y$-axis, or seen in table for (b) <br> (b) Missing values: $1.933,2.408$ <br> (Accept awrt) <br> (c) $\frac{1}{2} \times 0.2,\{(1+3)+2(1.246+1.552+1.933+2.408)\}$ $=1.8278 \quad \text { (awrt 1.83) }$ | B1  <br> B1  <br> B1, B1  <br> B1, M1 A1ft  <br> A1  <br> A1 $(4)$ <br>   <br>  8 |
|  | Beware the order of marks! <br> (a) Must be a curve (not a straight line). <br> Curve must extend to the left of the $y$-axis, and must be increasing. <br> Curve can 'touch' the $x$-axis, but must not go below it. <br> Otherwise, be generous in cases of doubt. <br> The B 1 for $(0,1)$ is independent of the sketch. <br> (c) Bracketing mistake: i.e. $\frac{1}{2} \times 0.2(1+3)+2(1.246+1.552+1.933+2.408)$ <br> scores B1 M1 A0 A0 unless the final answer implies that the calculation has been done correctly (then full marks can be given). |  |





| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 9. | (a) $a r=4, \quad \frac{a}{1-r}=25$ <br> (These can be seen elsewhere) $\begin{align*} & a=25(1-r) \quad 25 r(1-r)=4 \\ & 25 r^{2}-25 r+4=0 \tag{*} \end{align*}$ <br> (b) $(5 r-1)(5 r-4)=0 \quad r=\ldots$, <br> (c) $r=\ldots \Rightarrow a=\ldots$, <br> 20 or 5 <br> (d) $S_{n}=\frac{a\left(1-r^{n}\right)}{1-r}$, but $\frac{a}{1-r}=25$, so $S_{n}=25\left(1-r^{n}\right)$ <br> (e) $25\left(1-0.8^{n}\right)>24$ and proceed to $n=\ldots$ (or $>$, or $<$ ) with no unsound algebra. $\left(n>\frac{\log 0.04}{\log 0.8} \quad(=14.425 \ldots)\right) \quad n=15$ | B1, B1  <br> M1  <br> A1cso (4) <br> M1, A1  <br> M1, A1  <br> B1  <br> M1  <br> A1  |
|  | (a) The M mark is not dependent, but both expressions must contain both $a$ and $r$. <br> (b) Special case: <br> One correct $r$ value given, with no method (or perhaps trial and error): B1 B0. <br> (c) M1: Substitute one $r$ value back to find a value of $a$. <br> (d) Sufficient here to verify with just one pair of values of $a$ and $r$. <br> (e) Accept "=" rather than inequalities throughout, and also allow the wrong inequality to be used at any stage. <br> M1 requires use of their larger value of $r$. <br> A correct answer with no working scores both marks. <br> For "trial and error" methods, to score M1, a value of $n$ between 12 and 18 (inclusive) must be tried. |  |



## GENERAL PRINCIPLES FOR C2 MARKING

## Method mark for solving 3 term quadratic:

## 1. Factorisation

$\left(x^{2}+b x+c\right)=(x+p)(x+q)$, where $|p q|=|c|$, leading to $x=\ldots$
$\left(a x^{2}+b x+c\right)=(m x+p)(n x+q)$, where $|p q|=|c|$ and $|m n|=|a|$, leading to $x=\ldots$

## 2. Formula

Attempt to use correct formula (with values for $a, b$ and $c$ ).
3. Completing the square

Solving $x^{2}+b x+c=0: \quad(x \pm p)^{2} \pm q \pm c, \quad p \neq 0, q \neq 0, \quad$ leading to $x=\ldots$

## Method marks for differentiation and integration:

## 1. Differentiation

Power of at least one term decreased by 1. $\left(x^{n} \rightarrow x^{n-1}\right)$

## 2. Integration

Power of at least one term increased by $1 .\left(x^{n} \rightarrow x^{n+1}\right)$

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.
Normal marking procedure is as follows:
Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.
Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but will be lost if there is any mistake in the working.

## Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

## Answers without working

The rubric says that these may gain no credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required. Most candidates do show working, but there are occasional awkward cases and if the mark scheme does not cover this, please contact your team leader for advice.

## Misreads

(See the next sheet for a simple example).
A misread must be consistent for the whole question to be interpreted as such.
These are not common. In clear cases, please deduct the first 2 A (or B) marks which would have been lost by following the scheme. (Note that 2 marks is the maximum misread penalty, but that misreads which alter the nature or difficulty of the question cannot be treated so generously and it will usually be necessary here to follow the scheme as written).
Sometimes following the scheme as written is more generous to the candidate than applying the misread rule, so in this case use the scheme as written.

## MISREADS

Question 1. $\quad(2+x)^{6}$ misread as $(2+x)^{8}$

1. $(2+x)^{8}=256 \ldots$ B0

$$
+\left(8 \times 2^{7} \times x\right)+\left(\frac{8 \times 7}{2} \times 2^{6} \times x^{2}\right), \quad+1024 x,+1792 x^{2} \quad \text { M1, A0, A1 }
$$

# Mark Scheme (Results) J anuary 2007 

## GCE

## GCE Mathematics

Core Mathematics C2 (6664)

## J anuary 2007 <br> 6664 Core Mathematics C2 Mark Scheme

| Question <br> Number <br> 1. | Scheme | Marks |
| :---: | :--- | :--- |
| (a) | $\mathrm{f}^{\prime}(x)=3 x^{2}+6 x$ |  |
| $\mathrm{f}^{\prime \prime}(x)=6 x+6$ | B1 <br> M1, A1cao <br> (3) |  |

Notes cao = correct answer only

| $1(\mathrm{a})$ | B1 |
| :--- | :--- |
| Acceptable alternatives include |  |
| $3 x^{2}+6 x^{1} ; \quad 3 x^{2}+3 \times 2 x ; \quad 3 x^{2}+6 x+0$ |  |
| Ignore LHS (e.g. use [whether correct or not] of $\frac{\mathrm{d} y}{\mathrm{~d} x}$ and $\left.\frac{\mathrm{d}^{2} y}{\mathrm{~d} x^{2}}\right)$ |  |
| $3 x^{2}+6 x+c$ or $3 x^{2}+6 x+$ constant (i.e. the written word constant) is B0 |  |
| M1 Attempt to differentiate their $\mathrm{f}^{\prime}(x) ; x^{n} \rightarrow x^{n-1}$. <br> $x^{n} \rightarrow x^{n-1}$ seen in at least one of the terms. Coefficient of $x^{\cdots \cdots}$ ignored for the method mark. <br> $x^{2} \rightarrow x^{1}$ and $x \rightarrow x^{0}$ are acceptable. | M1 |
| Acceptable alternatives include | A1 |
| $6 x^{1}+6 x^{0} ; \quad 3 \times 2 x+3 \times 2$ | cao |
| $6 x+6+c$ or $6 x+6+$ constant is A0 |  |

## Examples

1(a) $\mathrm{f}^{\prime \prime}(x)=3 x^{2}+6 x \quad$ B1
M0 A0
1(a) $\quad \mathrm{f}^{\prime}(x)=3 x^{2}+6 x$
B1
$\mathrm{f}^{\prime \prime}(x)=6 x$
M1 A0

1(a) $y=x^{3}+3 x^{2}+5$

$$
\begin{array}{ll}
\frac{\mathrm{d} y}{\mathrm{~d} x}=3 x^{2}+3 x & \text { B0 } \\
\frac{\mathrm{d}^{2} y}{\mathrm{~d} x^{2}}=6 x+3 & \text { M1 A0 }
\end{array}
$$

1(a) $\mathrm{f}^{\prime}(x)=3 x^{2}+6 x+c \quad$ B0
$\mathrm{f}^{\prime \prime}(x)=6 x+6 \quad$ M1 A1

1(a) $\begin{array}{ll}\mathrm{f}^{\prime}(x)=x^{2}+3 x & \text { B0 } \\ & \mathrm{f}^{\prime \prime}(x)=x+3\end{array} \quad$ M1 A0

$$
\text { 1(a) } \begin{array}{lll} 
& x^{3}+3 x^{2}+5 & \\
& =3 x^{2}+6 x & \text { B1 } \\
& =6 x+6 & \text { M1 A1 }
\end{array}
$$

1(a) $\mathrm{f}^{\prime}(x)=3 x^{2}+6 x \quad+5 \quad \mathrm{~B} 0$
$\mathrm{f}^{\prime \prime}(x)=6 x+6 \quad$ M1 A1
1(a) $\mathrm{f}^{\prime}(x)=3 x^{2}+6 x \quad$ B1
$\mathrm{f}^{\prime \prime}(x)=6 x+6+c \quad$ M1 A0

| Question <br> Number | Scheme | Marks |
| :---: | :---: | :--- |
| 1. <br> (b) | $\int\left(x^{3}+3 x^{2}+5\right) \mathrm{d} x=\frac{x^{4}}{4}+\frac{3 x^{3}}{3}+5 x$ | M1, A1 |
| $\left[\frac{x^{4}}{4}+x^{3}+5 x\right]_{1}^{2}=4+8+10-\left(\frac{1}{4}+1+5\right)$ |  |  |
| $=15 \frac{3}{4}$ o.e. | M1 |  |
|  |  | A1 <br> (7) |

$\underline{\text { Notes }} \quad$ o.e. $=$ or equivalent

| 1 (b) |  |
| :--- | :--- |
| Attempt to integrate $\mathrm{f}(x) ; x^{n} \rightarrow x^{n+1}$ <br> Ignore incorrect notation (e.g. inclusion of integral sign) | M1 |
| o.e. <br> Acceptable alternatives include <br> $\frac{x^{4}}{4}+x^{3}+5 x ; \quad \frac{x^{4}}{4}+\frac{3 x^{3}}{3}+5 x^{1} ; \quad \frac{x^{4}}{4}+\frac{3 x^{3}}{3}+5 x+c ; \quad \int \frac{x^{4}}{4}+\frac{3 x^{3}}{3}+5 x$ <br> N.B. If the candidate has written the integral (either $\frac{x^{4}}{4}+\frac{3 x^{3}}{3}+5 x$ or what they think is the <br> integral) in part (a), it may not be rewritten in (b), but the marks may be awarded if the integral <br> is used in (b). |  |
| Substituting 2 and 1 into any function other than $x^{3}+3 x^{2}+5$ and subtracting either way round. <br> So using their $f^{\prime}(x)$ or $f^{\prime \prime}(x)$ or $\int$ their $\mathrm{f}^{\prime}(x) \mathrm{d} x$ or $\int$ their $\mathrm{f}^{\prime \prime}(x) \mathrm{d} x$ will gain the M mark <br> (because none of these will give $\left.x^{3}+3 x^{2}+5\right)$. <br> Must substitute for all $x$ s but could make a slip. <br> $4+8+10-\frac{1}{4}+1+5$ (for example) is acceptable for evidence of subtraction ('invisible' |  |
| brackets). | M1 |
| o.e. (e.g. $15 \frac{3}{4}, 15.75, \frac{63}{4}$ ) | A1 |
| Must be a single number (so $22-6 \frac{1}{4}$ is A0). |  |
| Answer only is M0A0M0A0 |  |

## Examples

1(b) $\frac{x^{4}}{4}+x^{3}+5 x+c$
M1 A1
1(b) $\frac{x^{4}}{4}+x^{3}+5 x+c \quad$ M1 A1
$4+8+10+c-\left(\frac{1}{4}+1+5+c\right)$
$x=2, \quad 22+c$
$=15 \frac{3}{4}$
A1
$x=1, \quad 6 \frac{1}{4}+c \quad$ M0 A0
(no subtraction)

1(b) $\int_{1}^{2} f(x) d x=2^{3}+3 \times 2^{2}+5-(1+3+5) \quad$ M0 A0, M0

$$
\begin{aligned}
& =25-9 \\
& =16
\end{aligned}
$$

(Substituting 2 and 1 into $x^{3}+3 x^{2}+5$, so 2nd M0)

1(b) $\int_{1}^{2}(6 x+6) \mathrm{d} x=\left[3 x^{2}+6 x\right]_{1}^{2}$ M0 A0
1(b) $\begin{array}{rlr}\int_{1}^{2}\left(3 x^{2}+6 x\right) \mathrm{d} x=\left[x^{3}+3 x^{2}\right]_{1}^{2} & \text { M0 A0 } \\ =8+12-(1+3) & \text { M1 A0 }\end{array}$
$=12+12-(3+6) \quad$ M1 A0
$=8+12-(1+3) \quad$ M1 A0

1(b) $\frac{x^{4}}{4}+x^{3}+5 x$
M1 A1

$$
\frac{2^{4}}{4}+2^{3}+5 \times 2-\frac{1^{4}}{4}+1^{3}+5 \quad \text { M1 }
$$

(one negative sign is sufficient for evidence of subtraction)
$=22-6 \frac{1}{4}=15 \frac{3}{4}$
A1
(allow 'recovery', implying student was using 'invisible brackets')

1(a) $\mathrm{f}(x)=x^{3}+3 x^{2}+5$

$$
\mathrm{f}^{\prime \prime}(x)=\frac{x^{4}}{4}+x^{3}+5 x \quad \text { B0 M0 A0 }
$$

(b) $\frac{2^{4}}{4}+2^{3}+5 \times 2-\frac{1^{4}}{4}-1^{3}-5 \quad$ M1 A1 M1

$$
=15 \frac{3}{4}
$$

A1
The candidate has written the integral in part (a). It is not rewritten in (b), but the marks may be awarded as the integral is used in (b).

| Question <br> Number <br> 2. <br> (a) | Scheme $\begin{aligned} (1-2 x)^{5} & =1+5 \times(-2 x)+\frac{5 \times 4}{2!}(-2 x)^{2}+\frac{5 \times 4 \times 3}{3!}(-2 x)^{3}+\ldots \\ & =1-10 x+40 x^{2}-80 x^{3}+\ldots \end{aligned}$ | Marks B1, M1, A1, <br> A1 <br> (4) |
| :---: | :---: | :---: |
| (b) | $\begin{align*} (1+x)(1-2 x)^{5} & =(1+x)(1-10 x+\ldots) \\ & =1+x-10 x+\ldots \\ & \approx 1-9 x \quad(*) \tag{*} \end{align*}$ | $\begin{array}{ll} \text { M1 } \\ \text { A1 } \end{array}$ |

## Notes

| $2(\mathrm{a})$ | B 1 |
| :--- | :--- |
| $1-10 x$ |  |
| $1-10 x$ must be seen in this simplified form in (a). |  |
| Correct structure: 'binomial coefficients' (perhaps from Pascal's triangle), increasing powers of $x$. <br> Allow slips. <br> Accept other forms: ${ }^{5} \mathrm{C}_{1},\binom{5}{1}$, also condone $\left(\frac{5}{1}\right)$ but must be attempting to use 5. <br> Condone use of invisible brackets and using $2 x$ instead of $-2 x$. <br> Powers of $x$ : at least 2 powers of the type $(2 x)^{a}$ or $2 x^{a}$ seen for $a \geq 1$. <br> $40 x^{2}(1$ st A1) |  |
| $-80 x^{3}(2$ nd A1) | A1 |
| Allow commas between terms. Terms may be listed rather than added <br> Allow 'recovery' from invisible brackets, so $1^{5}+\binom{5}{1} 1^{4} .-2 x+\binom{5}{2} 1^{3} .-2 x^{2}+\binom{5}{3} 1^{2} .-2 x^{3}$ <br> $=1-10 x+40 x^{2}-80 x^{3}+\ldots$ gains full marks. <br> $1+5 \times(2 x)+\frac{5 \times 4}{2!}(2 x)^{2}+\frac{5 \times 4 \times 3}{3!}(2 x)^{3}+\ldots=1+10 x+40 x^{2}+80 x^{3}+\ldots$ gains B0M1A1A0 <br> Misread: first 4 terms, descending terms: if correct, would score <br> B0, M1, 1 st A1: one of $40 x^{2}$ and $-80 x^{3}$ correct; 2 nd A1: both $40 x^{2}$ and $-80 x^{3}$ correct. |  |


| 2(a) Long multiplication |  |
| :--- | :--- |
| $(1-2 x)^{2}=1-4 x+4 x^{2},(1-2 x)^{3}=1-6 x+12 x^{2}-8 x^{3},(1-2 x)^{4}=1-8 x+24 x^{2}-32 x^{3}\left\{+16 x^{4}\right\}$ |  |
| $(1-2 x)^{5}=1-10 x+40 x^{2}+80 x^{3}+\ldots$ | B1 |
| $1-10 x$ | M1 |


| $40 x^{2}$ (1st A1) | A1 |
| :--- | :--- |
| $-80 x^{3}$ (2nd A1) | A1 |
|  |  |
| Misread: first 4 terms, descending terms: if correct, would score <br> B0, M1, 1st A1: one of $40 x^{2}$ and $-80 x^{3}$ correct; 2nd A1: both $40 x^{2}$ and $-80 x^{3}$ correct. |  |


| 2(b) |  |
| :--- | :--- |
| Use their (a) and attempt to multiply out; terms (whether correct or incorrect) in $x^{2}$ or higher | M1 |
| can be ignored. |  |
| If their (a) is correct an attempt to multiply out can be implied from the correct answer, so |  |
| $(1+x)(1-10 x)=1-9 x$ will gain M1 A1. <br> If their (a) is correct, the 2nd bracket must contain at least $(1-10 x)$ and an attempt to <br> multiply out for the M mark. An attempt to multiply out is an attempt at 2 out of the 3 <br> relevant terms (N.B. the 2 terms in $x^{1}$ may be combined - but this will still count as 2 terms). <br> If their (a) is incorrect their 2nd bracket must contain all the terms in $x^{0}$ and $x^{1}$ from their (a) <br> AND an attempt to multiply all terms that produce terms in $x^{0}$ and $x^{1}$. <br> N.B. $(1+x)(1-2 x)^{5}=(1+x)(1-2 x) \quad$ [where $1-2 x+\ldots$ is NOT the candidate's <br> answer to (a)] $\quad=1-x$ <br> i.e. candidate has ignored the power of 5: M0 <br> N.B. The candidate may start again with the binomial expansion for $(1-2 x)^{5}$ in (b). If correct <br> (only needs $1-10 x)$ may gain M1 A1 even if candidate did not gain B1 in part (a). <br> N.B. Answer given in question. |  |

## Example

Answer in (a) is $=1+10 x+40 x^{2}-80 x^{3}+\ldots$
(b) $(1+x)(1+10 x)=1+10 x+x \quad$ M1
$=1+11 x \quad$ A0

| Question | Scheme | Marks |
| :---: | :---: | :---: |
| 3. | $\begin{aligned} & \text { Centre }\left(\frac{-1+3}{2}, \frac{6+4}{2}\right) \text {, i.e. }(1,5) \\ & r=\sqrt{(3-(-1))^{2}+(6-4)^{2}} \end{aligned}$ | M1, A1 |
|  | or $r^{2}=(1-(-1))^{2}+(5-4)^{2}$ or $r^{2}=(3-1)^{2}+(6-5)^{2}$ o.e. | M1 |
|  | $(x-1)^{2}+(y-5)^{2}=5$ | M1,A1,A1 (6) |

## Notes

## Some use of correct formula in $x$ or $y$ coordinate. Can be implied.

Use of $\left(\frac{1}{2}\left(x_{A}-x_{B}\right), \frac{1}{2}\left(y_{A}-y_{B}\right)\right) \rightarrow(-2,-1)$ or $(2,1)$ is M0 A0 but watch out for use of $x_{A}+\frac{1}{2}\left(x_{A}-x_{B}\right)$ etc which is okay.
$(1,5)$
$(5,1)$ gains M1 A0.
Correct method to find $r$ or $r^{2}$ using given points or f.t. from their centre. Does not need to be $\quad$ M1 simplified.
Attempting radius $=\sqrt{\frac{(\text { diameter })^{2}}{2}}$ is an incorrect method, so M0.
N.B. Be careful of labelling: candidates may not use $d$ for diameter and $r$ for radius.

Labelling should be ignored.
Simplification may be incorrect - mark awarded for correct method.
Use of $\sqrt{\left(x_{1}-x_{2}\right)^{2}-\left(y_{1}-y_{2}\right)^{2}}$ is M0.
Write down $(x \pm a)^{2}+(y \pm b)^{2}=$ any constant (a letter or a number).
Numbers do not have to be substituted for $a, b$ and if they are they can be wrong.
LHS is $(x-1)^{2}+(y-5)^{2}$. Ignore RHS.
RHS is 5 .
A1

| Question <br> Number <br> 4. | $x \log 5=\log 17$ | or <br> $x=\frac{\log 17}{\log 5}$ <br> $=1.76$ | $x=\log _{5} 17$ | Marks |  |
| :---: | :---: | :---: | :---: | :--- | :---: |
|  |  |  | M1 |  |  |
|  |  |  | A1 |  |  |

Notes N.B. It is never possible to award an A mark after giving M0. If M0 is given then the marks will be M0 A0 A0.

| 4 |  |
| :---: | :---: |
| Acceptable alternatives include <br> $x \log 5=\log 17 ; \quad x \log _{10} 5=\log _{10} 17 ; \quad x \log _{\mathrm{e}} 5=\log _{\mathrm{e}} 17 ; \quad x \ln 5=\ln 17 ; \quad x=\log _{5} 17$ <br> Can be implied by a correct exact expression as shown on the first A1 mark | 1st M1 |
| Can be implied by a correct exact expression as shown on the first A1 mark <br> An exact expression for $x$ that can be evaluated on a calculator. Acceptable alternatives include $x=\frac{\log 17}{\log 5} ; x=\frac{\log _{10} 17}{\log _{10} 5} ; x=\frac{\log _{\mathrm{e}} 17}{\log _{\mathrm{e}} 5} ; x=\frac{\ln 17}{\ln 5} ; \quad x=\frac{\log _{q} 17}{\log _{q} 5}$ where $q$ is a number <br> This may not be seen (as, for example, $\log _{5} 17$ can be worked out directly on many calculators) so this A mark can be implied by the correct final answer or the right answer corrected to or truncated to a greater accuracy than 3 significant figures or 1.8 <br> Alternative: $x=\frac{\text { a number }}{\text { a number }}$ where this fraction, when worked out as a decimal rounds to 1.76. <br> (N.B. remember that this A mark cannot be awarded without the M mark). <br> If the line for the M mark is missing but this line is seen (with or without the $x=$ ) and is correct the method can be assumed and M1 1st A1 given. | 1st A1 |
| 1.76 cao | 2nd A1 |
| N.B. $\sqrt[5]{17}=1.76$ and $x^{5}=17, \therefore x=1.76$ are both M0 A0 A0 |  |
| Answer only 1.76: full marks (M1 A1 A1) <br> Answer only to a greater accuracy but which rounds to 1.76: M1 A1 A0 (e.g. 1.760, 1.7603, 1.7604, 1.76037 etc) <br> Answer only 1.8: M1 A1 A0 <br> Trial and improvement: award marks as for "answer only". |  |

## Examples

4. $x=\log 5^{17}$
M0 A0
$=1.76$
A0

Working seen, so scheme applied
4. $5^{1.8}=17$

M1 A1 A0
Answer only but clear that $x=1.8$
4. $\log _{5} 17=x$
M1
$x=1.760$
A1 A0
4. $x \log 5=\log 17$
M1

$$
x=\frac{1.2304 \ldots}{0.69897 \ldots} \quad \text { A1 }
$$

$$
x=1.76 \quad \text { A1 }
$$

4. $x \log 5=\log 17$
M1
$x=\frac{2.57890}{1.46497}$
A1
$x=1.83$
A0
5. $\quad 5^{1.8}=18.1,5^{1.75}=16.7$ $5^{1.761}=17 \quad$ M1 A1 A0
6. $x \log 5=\log 17$
M1

$$
x=1.8 \quad \text { A1 A } 0
$$

## N.B.

4. $x^{5}=17$
M0 A0
$x=1.76$
A0
5. $5^{1.76}=17 \quad$ M1 A1 A1

Answer only but clear that $x=1.76$
4. $5^{1.76} \quad$ M0 A0 A0
4. $\quad \log _{5} 17=x$ $x=1.76$
M1
A1 A1
4. $x \ln 5=\ln 17 \quad$ M1
$x=\frac{2.833212 \ldots}{1.609437 \ldots} \quad$ A1
$x=1.76 \quad$ A1
4. $\quad \log _{17} 5=x$
M0
$x=\frac{\log 5}{\log 17}$
A0
$x=0.568$
A0
4. $x=5^{1.76}$

M0 A0 A0
4. $x=\frac{\log 17}{\log 5}$

M1 A1

$$
x=1.8
$$

A0
4. $\sqrt[5]{17}$
$=1.76$
M0 A0
A0

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 5. <br> (a) | $\begin{aligned} \mathrm{f}(-2) & =(-2)^{3}+4(-2)^{2}+(-2)-6 \\ \{ & =-8+16-2-6\} \\ & =0, \therefore x+2 \text { is a factor } \end{aligned}$ | M1 <br> A1 <br> (2) |
| (b) | $\begin{aligned} x^{3}+4 x^{2}+x-6 & =(x+2)\left(x^{2}+2 x-3\right) \\ & =(x+2)(x+3)(x-1) \end{aligned}$ | M1, A1 M1, A1 <br> (4) |
| (c) | -3, -2, 1 | B1 (7) |

Notes Line in mark scheme in \{ \} does not need to be seen.

| $5(\mathrm{a})$ |  |
| :--- | :--- |
| Attempting $\mathrm{f}( \pm 2)$ : No $x$ s; allow invisible brackets for M mark | M1 |
| Long division: M0 A0. | A1 |
| $=0$ and minimal conclusion (e.g. factor, hence result, QED, $\checkmark, \square)$. |  |
| If result is stated first [i.e. If $x+2$ is a factor, $\mathrm{f}(-2)=0$ ] conclusion is not needed. |  |
| Invisible brackets used as brackets can get M1 A1, so |  |
| $\mathrm{f}(-2)=-2^{3}+4 \times-2^{2}+-2-6\{=-8+16-2-6\}=0, \therefore x+2$ is a factor M1 A1, but |  |
| $\mathrm{f}(-2)=-2^{3}+4 \times-2^{2}+-2-6=-8-16-2-6=0, \therefore x+2$ is a factor M1 A0 |  |
| Acceptable alternatives include: $x=-2$ is a factor, $\mathrm{f}(-2)$ is a factor. |  |


| 5(b) |  |
| :--- | :--- |
| 1st M1 requires division by $(x+2)$ to get $x^{2}+a x+b$ where $a \neq 0$ and $b \neq 0$ or equivalent <br> with division by $(x+3)$ or $(x-1)$. | M1 |
| $(x+2)\left(x^{2}+2 x-3\right)$ or $(x+3)\left(x^{2}+x-2\right)$ or $(x-1)\left(x^{2}+5 x+6\right)$ <br> [If long division has been done in (a), minimum seen in (b) to get first M1 A1 is to make <br> some reference to their quotient $\left.x^{2}+a x+b.\right]$ | A1 |
| Attempt to factorise their quadratic (usual rules). | M1 |
| "Combining" all 3 factors is not required. | A1 |
| Answer only: Correct M1 A1 M1 A1 <br> Answer only with one sign slip: $(x+2)(x+3)(x+1)$ scores 1st M1 1st A12nd M0 2nd A0 <br> $(x+2)(x-3)(x-1)$ scores 1st M0 1st A0 2nd M1 2nd A1 |  |
| Answer to (b) can be seen in (c). |  |


| $5(\mathrm{~b})$ Alternative comparing coefficients |  |
| :--- | :--- |
| $(x+2)\left(x^{2}+a x+b\right)=x^{3}+(2+a) x^{2}+(2 a+b) x+2 b$ | M1 |
| Attempt to compare coefficients of two terms to find values of $a$ and $b$ | A1 |
| $a=2, b=-3$ | M1 |
| Or $(x+2)\left(a x^{2}+b x+c\right)=a x^{3}+(2 a+b) x^{2}+(2 b+c) x+2 c$  <br> Attempt to compare coefficients of three terms to find values of $a, b$ and $c$. A1 <br> $a=1, b=2, c=-3$  <br> Then apply scheme as above  $\mathbf{l}$ |  |


| $5(\mathrm{~b})$ Alternative using factor theorem |  |
| :--- | :--- |
| Show $\mathrm{f}(-3)=0$; allow invisible brackets | M1 |
| $\therefore x+3$ is a factor | A1 |
| Show $\mathrm{f}(1)=0$ | M1 |
| $\therefore x-1$ is a factor | A1 |


| $5(\mathrm{c})$ | B1 |
| :--- | :--- |
| $-3,-2,1$ or $(-3,0),(-2,0),(1,0)$ only. Do not ignore subsequent working. |  |
| Ignore any working in previous parts of the question. Can be seen in (b) |  |


| Question <br> Number | Scheme | Marks |
| :---: | :---: | :--- |
| 6. | $2\left(1-\sin ^{2} x\right)+1=5 \sin x$ |  |
| $2 \sin ^{2} x+5 \sin x-3=0$ |  |  |
| $(2 \sin x-1)(\sin x+3)=0$ |  |  |
| $\sin x=\frac{1}{2}$ |  | M1 |
|  | $x=\frac{\pi}{6}, \frac{5 \pi}{6}$ | M1, A1 |
|  |  | M1, M1, |
|  | A1cso (6) |  |

## Notes

| Use of $\cos ^{2} x=1-\sin ^{2} x$. <br> Condone invisible brackets in first line if $2-2 \sin ^{2} x$ is present (or implied) in a subsequent line. <br> Must be using $\cos ^{2} x=1-\sin ^{2} x$. Using $\cos ^{2} x=1+\sin ^{2} x$ is M0. | M1 |
| :---: | :---: |
| Attempt to solve a 2 or 3 term quadratic in $\sin x$ up to $\sin x=\ldots$ Usual rules for solving quadratics. Method may be factorising, formula or completing the square | M1 |
| Correct factorising for correct quadratic and $\sin x=\frac{1}{2}$. So, e.g. $(\sin x+3)$ as a factor $\rightarrow \sin x=3$ can be ignored. | A1 |
| Method for finding any angle in any range consistent with (either of) their trig. equation(s) in degrees or radians (even if $x$ not exact). [Generous M mark] <br> Generous mark. Solving any trig. equation that comes from minimal working (however bad). So $x=\sin ^{-1} / \cos ^{-1} / \tan ^{-1}$ (number) $\rightarrow$ answer in degrees or radians correct for their equation (in any range) | M1 |
| Method for finding second angle consistent with (either of) their trig. equation(s) in radians. Must be in range $0 \leq x<2 \pi$. Must involve using $\pi$ (e.g. $\pi \pm \ldots, 2 \pi-\ldots$ ) but ... can be inexact. <br> Must be using the same equation as they used to attempt the 3rd M mark. <br> Use of $\pi$ must be consistent with the trig. equation they are using (e.g. if using $\cos ^{-1}$ then must be using $2 \pi-\ldots$ ) <br> If finding both angles in degrees: method for finding 2nd angle equivalent to method above in degrees and an attempt to change both angles to radians. | M1 |
| $\frac{\pi}{6}, \frac{5 \pi}{6} \text { c.s.o. } \quad \text { Recurring decimals are okay (instead of } \frac{1}{6} \text { and } \frac{5}{6} \text { ). }$ <br> Correct decimal values (corrected or truncated) before the final answer of $\frac{\pi}{6}, \frac{5 \pi}{6}$ is acceptable. | A1 cso |
| Ignore extra solutions outside range; deduct final A mark for extra solutions in range. |  |
| $\begin{aligned} & \text { Special case } \\ & \text { Answer only } \frac{\pi}{6}, \frac{5 \pi}{6} \quad \text { M0, M0, A0, M1, M1 A1 } \quad \text { Answer only } \frac{\pi}{6} \quad \text { M0, M0, A0, M1, } \\ & \text { M0 A0 } \end{aligned}$ |  |

Finding answers by trying different values (e.g. trying multiples of $\pi$ ) in $2 \cos ^{2} x+1=5 \sin x$ : as for answer only.

| Question Number <br> 7. | $\begin{aligned} & y=x\left(x^{2}-6 x+5\right) \\ & =x^{3}-6 x^{2}+5 x \\ & \int\left(x^{3}-6 x^{2}+5 x\right) \mathrm{d} x=\frac{x^{4}}{4}-\frac{6 x^{3}}{3}+\frac{5 x^{2}}{2} \\ & {\left[\frac{x^{4}}{4}-2 x^{3}+\frac{5 x^{2}}{2}\right]_{0}^{1}=\left(\frac{1}{4}-2+\frac{5}{2}\right)-0=\frac{3}{4}} \\ & {\left[\frac{x^{4}}{4}-2 x^{3}+\frac{5 x^{2}}{2}\right]_{1}^{2}=(4-16+10)-\frac{3}{4}=-\frac{11}{4}} \\ & \therefore \text { total area }=\frac{3}{4}+\frac{11}{4} \\ & =\frac{7}{2} \quad \text { o.e. } \end{aligned}$ | Marks <br> M1, A1 <br> M1, A1ft <br> M1 <br> M1, A1(both) <br> M1 <br> A1cso <br> (9) |
| :---: | :---: | :---: |

## Notes

| Attempt to multiply out, must be a cubic. | M1 |
| :---: | :---: |
| Award A mark for their final version of expansion (but final version does not need to have like terms collected). | A1 |
| Attempt to integrate; $x^{n} \rightarrow x^{n+1}$. Generous mark for some use of integration, so e.g. $\int x(x-1)(x-5) \mathrm{d} x=\frac{x^{2}}{2}\left(\frac{x^{2}}{2}-x\right)\left(\frac{x^{2}}{2}-5 x\right)$ would gain method mark. | M1 |
| Ft on their final version of expansion provided it is in the form $a x^{p}+b x^{q}+\ldots$. Integrand must have at least two terms and all terms must be integrated correctly. <br> If they integrate twice (e.g. $\int_{0}^{1}$ and $\int_{1}^{2}$ ) and get different answers, take the better of the two. | A1ft |
| Substitutes and subtracts (either way round) for one integral. Integral must be a 'changed' function. Either 1 and 0,2 and 1 or 2 and 0 . <br> For []$_{0}^{1}:-0$ for bottom limit can be implied (provided that it is 0 ). | M1 |
| M1 Substitutes and subtracts (either way round) for two integrals. Integral must be a 'changed' function. Must have 1 and 0 and 2 and 1 (or 1 and 2). <br> The two integrals do not need to be the same, but they must have come from attempts to integrate the same function. | M1 |
| $\frac{3}{4}$ and $-\frac{11}{4}$ o.e. (if using $\int_{1}^{2} \mathrm{f}(x)$ ) or $\frac{3}{4}$ and $\frac{11}{4}$ o.e. (if using $\int_{2}^{1} \mathrm{f}(x)$ or $-\int_{1}^{2} \mathrm{f}(x)$ or $\left.\int_{1}^{2}-\mathrm{f}(x)\right) \quad$ where $\mathrm{f}(x)=\frac{x^{4}}{4}-2 x^{3}+\frac{5 x^{2}}{2}$. <br> The answer must be consistent with the integral they are using (so $\int_{1}^{2} \mathrm{f}(x)=\frac{11}{4}$ loses this A and the final A). <br> $-\frac{11}{4}$ may not be seen explicitly. Can be implied by a subsequent line of working. | A1 |
| 5th M1 $\mid$ their value for []$_{0}^{1}\|+\|$ their value for []$_{1}^{2} \mid$ <br> Dependent on at least one of the values coming from integration (other may come from e.g. trapezium rules). <br> This can be awarded even if both values already positive. | M1 |
| $\frac{7}{2}$ o.e. $\quad$ N.B.c.s.o. | A1 cso |



## Notes

| $8(\mathrm{a})$ | M 1 |
| :--- | :--- |
| Attempt to differentiate $v^{n} \rightarrow v^{n-1}$. Must be seen and marked in part (a) not part (b). <br> Must be differentiating a function of the form $a v^{-1}+b v$. | A1 |
| o.e. <br> $\left(-1400 v^{-2}+\frac{2}{7}+c\right.$ is A0) | M1 |
| Their $\frac{\mathrm{d} C}{\mathrm{~d} v}=0$. Can be implied by their $\frac{\mathrm{d} C}{\mathrm{~d} v}=P+Q \rightarrow P= \pm Q$. | dM 1 |
| Dependent on both of the previous Ms. <br> Attempt to rearrange their $\frac{\mathrm{d} C}{\mathrm{~d} v}$ into the form $v^{n}=$ number or $v^{n}-$ number $=0, \quad n \neq 0$. | A1cso |
| $v=70$ cso but allow $v= \pm 70$. | $v=70$ km per h also acceptable. |
| Answer only is 0 out of 5. |  |
| Method of completing the square: send to review. |  |


| 8(a) Trial and improvement $\quad \mathrm{f}(v)=\frac{1400}{v}+\frac{2 v}{7}$ |  |
| :--- | :--- |
| Attempts to evaluate $\mathrm{f}(v)$ for 3 values $a, b, c$ where (i) $a<70, b=70$ and $c>70$ or (ii) $a, b<$ <br> 70 and $c>70$ or (iii) $a<70$ and $b, c>70$. | M1 |
| All 3 correct and states $v=70$ (exact) | A1 |
| Then 2nd M0, 3rd M0, 2nd A0. |  |


| 8(a) Graph |  |
| :--- | :--- |
| Correct shape (ignore anything drawn for $v<0$ ). | M1 |
|  | A1 |
|  |  |


| $8(\mathrm{~b})$ |  |
| :--- | :--- |
| Attempt to differentiate their $\frac{\mathrm{d} C}{\mathrm{~d} v} ; v^{n} \rightarrow v^{n-1}$ (including $v^{0} \rightarrow 0$ ). | M1 |
| $\frac{\mathrm{d}^{2} C}{\mathrm{~d} v^{2}}$ must be correct. Ft only from their value of $v$ and provided their value of $v$ is +ve. | A1ft |
| Must be some (minimal) indication that their value of $v$ is being used. |  |
| Statement: "When $v=$ their value of $v, \frac{\mathrm{~d}^{2} C}{\mathrm{~d} v^{2}}>0$ " is sufficient provided $2800 v^{-3}>0$ for their |  |
| value of $v$. |  |
| If substitution of their $v$ seen: correct substitution of their $v$ into $2800 v^{-3}$, but, provided |  |
| evaluation is +ve, ignore incorrect evaluation. |  |
| N.B. Parts in mark scheme in \{ do not need to be seen. |  |


| 8(c) |  |
| :--- | :--- |
| Substitute their value of $v$ that they think will give $C_{\min }$ (independent of the method of <br> obtaining this value of $v$ and independent of which part of the question it comes from). | M1 |
| 40 or $£ 40$ <br> Must have part (a) completely correct (i.e. all 5 marks) to gain this A1. | A1 |
| Answer only gains M1A1 provided part (a) is completely correct.. |  |

## Examples 8(b)

8(b) $\quad \frac{\mathrm{d}^{2} C}{\mathrm{~d} v^{2}}=2800 v^{-3} \quad$ M1

$$
v=70, \frac{\mathrm{~d}^{2} C}{\mathrm{~d} v^{2}}>0 \quad \mathrm{~A} 1
$$

8(b) $\quad \frac{\mathrm{d}^{2} C}{\mathrm{~d} v^{2}}=2800 v^{-3} \quad$ M1

$$
>0 \quad \text { A0 (no indication that a value of } v \text { is being used) }
$$

8(b) Answer from (a): $v=30$

$$
\begin{array}{ll}
\frac{\mathrm{d}^{2} C}{\mathrm{~d} v^{2}}=2800 v^{-3} \\
v=30, \frac{\mathrm{~d}^{2} C}{\mathrm{~d} v^{2}}>0 & \text { M1 }
\end{array}
$$

8(b) $\quad \frac{\mathrm{d}^{2} C}{\mathrm{~d} v^{2}}=2800 v^{-3} \quad$ M1

$$
v=70, \frac{\mathrm{~d}^{2} C}{\mathrm{~d} v^{2}}=2800 \times 70^{-3}
$$

$=8.16 \quad$ A1 (correct substitution of 70 seen, evaluation wrong but positive)
8(b) $\frac{\mathrm{d}^{2} C}{\mathrm{~d} v^{2}}=2800 v^{-3}$ M1
$v=70, \frac{\mathrm{~d}^{2} C}{\mathrm{~d} v^{2}}=0.00408 \quad$ A0 (correct substitution of 70 not seen)

| Question Number | Scheme |  |
| :---: | :---: | :---: |
| 9. <br> (a) | $\begin{aligned} \cos P Q R & =\frac{6^{2}+6^{2}-(6 \sqrt{3})^{2}}{2 \times 6 \times 6}\left\{=-\frac{1}{2}\right\} \\ P Q R & =\frac{2 \pi}{3} \end{aligned}$ | M1, A1 <br> A1 <br> (3) |
| (b) | $\begin{aligned} \text { Area } & =\frac{1}{2} \times 6^{2} \times \frac{2 \pi}{3} \mathrm{~m}^{2} \\ & =12 \pi \mathrm{~m}^{2}(*) \end{aligned}$ |  |
| (c) | $\text { Area of } \begin{aligned} \Delta & =\frac{1}{2} \times 6 \times 6 \times \sin \frac{2 \pi}{3} \mathrm{~m}^{2} \\ & =9 \sqrt{3} \mathrm{~m}^{2} \end{aligned}$ |  |
| (d) | $\begin{aligned} \text { Area of segment } & =12 \pi-9 \sqrt{3} \mathrm{~m}^{2} \\ & =22.1 \mathrm{~m}^{2} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { (2) } \end{aligned}$ |
| (e) | $\begin{aligned} \text { Perimeter } & =6+6+\left[6 \times \frac{2 \pi}{3}\right] \mathrm{m} \\ & =24.6 \mathrm{~m} \end{aligned}$ | M1 <br> A1ft <br> (2) <br> (11) |

Notes
9(a) N.B. $a^{2}=b^{2}+c^{2}-2 b c \cos A$ is in the formulae book.
Use of cosine rule for $\cos P Q R$. Allow $A, \theta$ or other symbol for angle.
(i) $(6 \sqrt{3})^{2}=6^{2}+6^{2}-2.6 .6 \cos P Q R$ : Apply usual rules for formulae: (a) formula not stated, must be correct, (b) correct formula stated, allow one sign slip when substituting.
or (ii) $\cos P Q R=\frac{ \pm 6^{2} \pm 6^{2} \pm(6 \sqrt{3})^{2}}{ \pm 2 \times 6 \times 6}$
Also allow invisible brackets [so allow $6 \sqrt{3}^{2}$ ] in (i) or (ii)
Correct expression $\frac{6^{2}+6^{2}-(6 \sqrt{3})^{2}}{2 \times 6 \times 6}$ o.e. (e.g. $-\frac{36}{72}$ or $-\frac{1}{2}$ )
$\frac{2 \pi}{3}$

| $9(\mathrm{a})$ Alternative |  |
| :--- | :--- |
| $\sin \theta=\frac{a \sqrt{3}}{6} \quad$ where $\theta$ is any symbol and $a<6$. | M1 |
| $\sin \theta=\frac{3 \sqrt{3}}{6} \quad$ where $\theta$ is any symbol. | A1 |
| $\frac{2 \pi}{3}$ | A1 |


| 9(b) |  |
| :---: | :---: |
| Use of $\frac{1}{2} r^{2} \theta$ with $r=6$ and $\theta=$ their (a). For M mark $\theta$ does not have to be exact. M0 if using degrees. | M1 |
| $12 \pi \quad$ c.s.o. $\quad(\Rightarrow$ (a) correct exact or decimal value) <br> N.B. Answer given in question | A1 |
| Special case: <br> Can come from an inexact value in (a) <br> $P Q R=2.09 \rightarrow$ Area $=\frac{1}{2} \times 6^{2} \times 2.09=37.6$ (or 37.7 ) $=12 \pi \quad$ (no errors seen, assume full values used on calculator) gets M1 A1. $P Q R=2.09 \rightarrow \text { Area }=\frac{1}{2} \times 6^{2} \times 2.09=37.6(\text { or } 37.7)=11.97 \pi=12 \pi \text { gets M1 A0. }$ |  |


| 9(c) |  |
| :--- | :--- |
| Use of $\frac{1}{2} r^{2} \sin \theta$ with $r=6$ and their (a). | M1 |
| $\theta=\cos ^{-1}$ (their $P Q R$ ) in degrees or radians |  |
| Method can be implied by correct decimal provided decimal is correct (corrected or truncated |  |
| to at least 3 decimal places). |  |
| 15.58845727 |  |
| $9 \sqrt{3}$ c.s.o. Must be exact, but correct approx. followed by $9 \sqrt{3}$ is okay (e.g. $\ldots=15.58845$ <br> $=9 \sqrt{3}$ ) | A1cso |


| 9 (c) Alternative (using $\frac{1}{2} b h$ ) |  |
| :--- | :--- |
| Attempt to find $h$ using trig. or Pythagoras and use this $h$ in $\frac{1}{2} b h$ form to find the area of <br> triangle $P Q R$ | M1 |
| $9 \sqrt{3}$ c.s.o. Must be exact, but correct approx. followed by $9 \sqrt{3}$ is okay (e.g. $\ldots=15.58845$ <br> $=9 \sqrt{3}$ ) | A1cso |


| $9(\mathrm{~d})$ |  |
| :--- | :--- |
| Use of area of sector - area of $\Delta$ or use of $\frac{1}{2} r^{2}(\theta-\sin \theta)$. | M1 |
| Any value to 1 decimal place or more which rounds to 22.1 | A1 |
| $9(\mathrm{e})$ M 1 <br> $6+6+[6 \times$ their (a) $]$. A1 ft <br> Correct for their (a) to 1 decimal place or more  |  |


| Question Number 10. (a) | Scheme $\begin{align*} & \left\{S_{n}=\right\} a+a r+\ldots+a r^{n-1} \\ & \left\{r S_{n}=\right\} a r+a r^{2}+\ldots+a r^{n} \\ & (1-r) S_{n}=a\left(1-r^{n}\right) \\ & S_{n}=\frac{a\left(1-r^{n}\right)}{1-r} \quad(*) \tag{*} \end{align*}$ | Marks <br> B1 <br> M1 <br> dM1 <br> A1cso <br> (4) |
| :---: | :---: | :---: |
| (b) | $a=200, r=2, n=10, \quad \begin{aligned} S_{10} & =\frac{200\left(1-2^{10}\right)}{1-2} \\ & =204,600 \end{aligned}$ | M1, A1 A1 (3) |
| (c) | $\begin{aligned} & a=\frac{5}{6}, r=\frac{1}{3} \\ & S_{\infty}=\frac{a}{1-r}, \quad S_{\infty}=\frac{\frac{5}{6}}{1-\frac{1}{3}} \\ &=\frac{5}{4} \text { o.e. } \end{aligned}$ | B1 <br> M1 <br> A1 <br> (3) |
| (d) | $-1<r<1 \quad$ (or $\|r\|<1)$ | $\begin{array}{\|ll} \hline \text { B1 } & \text { (1) } \\ \hline \mathbf{( 1 1 )} \\ \hline \end{array}$ |

## Notes

| $10($ a $)$ |  |
| :--- | :--- |
| $S_{n}$ not required. The following must be seen: at least one + sign, $a, a r^{n-1}$ and one other <br> intermediate term. No extra terms (usually $\left.a r^{n}\right)$. | B1 |
| Multiply by $r$; $r S_{n}$ not required. At least 2 of their terms on RHS correctly multiplied by $r$. | M1 |
| Subtract both sides: LHS must be $\pm(1-r) S_{n}$, RHS must be in the form $\pm a\left(1-r^{p n+q}\right)$. <br> Only award this mark if the line for $S_{n}=\ldots$ or the line for $r S_{n}=\ldots$ contains a term of the <br> form $a r^{c n+d}$ <br> Method mark, so may contain a slip but not awarded if last term of their $S_{n}=$ last term of their <br> $r S_{n}$. | dM1 |
| Completion c.s.o. $\quad$ N.B. Answer given in question | A1 cso |


| $10($ a) |  |
| :--- | :--- |
| $S_{n}$ not required. The following must be seen: at least one + sign, $a, a r^{n-1}$ and one other <br> intermediate term. No extra terms (usually $a r^{n}$ ). | B1 |
| On RHS, multiply by $\frac{1-r}{1-r}$ <br> Or Multiply LHS and RHS by $(1-r)$ | M1 |


| Multiply by (1-r) convincingly (RHS) and take out factor of $a$. <br> Method mark, so may contain a slip. | dM 1 |
| :--- | :--- |
| Completion c.s.o. N.B. Answer given in question | A1 cso |


| $10(\mathrm{~b})$ |  |
| :--- | :--- |
| Substitute $r=2$ with $a=100$ or 200 and $n=9$ or 10 into formula for $S_{n}$. | M1 |
| $\frac{200\left(1-2^{10}\right)}{1-2}$ or equivalent. | A1 |
| 204,600 | A1 |


| 10 (b) Alternative method: adding 10 terms |  |
| :--- | :--- |
| (i) Answer only: full marks. (M1 A1 A1) |  |
| (ii) $200+400+800+\ldots\{+102,400\}=204,600 \quad$ or $100(2+4+8+\ldots\{+1,024)\}=$ | M1 |
| 204,600 |  |
| M1 for two correct terms (as above o.e.) and an indication that the sum is needed (e.g. + sign |  |
| or the word sum). |  |
| 102,400 o.e. as final term. Can be implied by a correct final answer. | A1 |
| 204,600. | A1 |


| 10 (c) N.B. $S_{\infty}=\frac{a}{1-r}$ is in the formulae book. |  |
| :--- | :--- |
| $r=\frac{1}{3}$ seen or implied anywhere. | B1 |
| Substitute $a=\frac{5}{6}$ and their $r$ into $\frac{a}{1-r}$. Usual rules about quoting formula. | M1 |
| $\frac{5}{4}$ o.e. | A1 |


| $10(\mathrm{~d})$ N.B. $S_{\infty}=\frac{a}{1-r}$ for $\|r\|<1$ is in the formulae book. |  |
| :--- | :--- |
| $-1<r<1 \quad$ or $\|r\|<1 \quad$ In words or symbols. | B1 |
| Take symbols if words and symbols are contradictory. Must be $<$ not $\leq$. |  |

## Mark Scheme (Results)

## Summer 2007

## GCE

## GCE Mathematics

## Core Mathematics C2 (6664)

J une 2007

## 6664 Core Mathematics C2

Mark Scheme

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 1. | $\begin{aligned} & \int x^{-\frac{1}{2}} \mathrm{~d} x=\frac{x^{\frac{1}{2}}}{\left(\frac{1}{2}\right)} \quad \text { (Or equivalent, such as } 2 x^{\frac{1}{2}} \text {, or } 2 \sqrt{x} \text { ) } \\ & \left.\left[\frac{x^{\frac{1}{2}}}{\left(\frac{1}{2}\right)}\right]_{1}^{8}=2 \sqrt{ } 8-2=-2+4 \sqrt{ } 2 \quad \text { [or } 4 \sqrt{ } 2-2 \text {, or } 2(2 \sqrt{ } 2-1) \text {, or } 2(-1+2 \sqrt{ } 2)\right] \end{aligned}$ | M1 A1 <br> M1 A1 (4) $4$ |
|  | $1^{\text {st }} \mathrm{M}: x^{-\frac{1}{2}} \rightarrow k x^{\frac{1}{2}}, k \neq 0$ <br> $2^{\text {nd }} \mathrm{M}$ : Substituting limits 8 and 1 into a 'changed' function (i.e. not $\frac{1}{\sqrt{x}}$ or $x^{-\frac{1}{2}}$ ), and subtracting, either way round. <br> $2^{\text {nd }} A$ : This final mark is still scored if $-2+4 \sqrt{ } 2$ is reached via a decimal. <br> N.B. Integration constant $+C$ may appear, e.g. $\left[\frac{x^{\frac{1}{2}}}{\left(\frac{1}{2}\right)}+C\right]_{1}^{8}=(2 \sqrt{ } 8+C)-(2+C)=-2+4 \sqrt{ } 2$ <br> (Still full marks) <br> But... a final answer such as $-2+4 \sqrt{ } 2+C$ is A0. <br> N.B. It will sometimes be necessary to 'ignore subsequent working' (isw) after a correct form is seen, e.g. $\int x^{-\frac{1}{2}} \mathrm{~d} x=\frac{x^{\frac{1}{2}}}{\left(\frac{1}{2}\right)}$ (M1 A1), followed by incorrect simplification $\int x^{-\frac{1}{2}} \mathrm{~d} x=\frac{x^{\frac{1}{2}}}{\left(\frac{1}{2}\right)}=\frac{1}{2} x^{\frac{1}{2}}$ (still M1 A1).... The second M mark is still available for substituting 8 and 1 into $\frac{1}{2} x^{\frac{1}{2}}$ and subtracting. |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 2. | (a) $f(2)=24-20-32+12=-16$ <br> (M: Attempt $f(2)$ or $f(-2)$ ) <br> (If continues to say 'remainder $=16$ ', isw) <br> Answer must be seen in part (a), not part (b). <br> (b) $\begin{aligned} & (x+2)\left(3 x^{2}-11 x+6\right) \\ & (x+2)(3 x-2)(x-3) \end{aligned}$ <br> (If continues to 'solve an equation', isw) | M1 A1 <br> M1 A1 <br> M1 A1 <br> (4) |
|  | (a) Answer only (if correct) scores both marks. (16 as 'answer only' is M0 A0). <br> Alternative (long division): <br> Divide by $(x-2)$ to get $\left(3 x^{2}+a x+b\right), \quad a \neq 0, b \neq 0$. [M1] <br> ( $3 x^{2}+x-14$ ), and -16 seen. <br> (If continues to say 'remainder $=16$ ', isw) <br> (b) First M requires division by $(x+2)$ to get $\left(3 x^{2}+a x+b\right), a \neq 0, b \neq 0$. <br> Second M for attempt to factorise their quadratic, even if wrongly obtained, perhaps with a remainder from their division. <br> Usual rule: $\left(k x^{2}+a x+b\right)=(p x+c)(q x+d)$, where $\|p q\|=\|k\|$ and $\|c d\|=\|b\|$. <br> Just solving their quadratic by the formula is M0. <br> "Combining" all 3 factors is not required. <br> Alternative (first 2 marks): <br> $(x+2)\left(3 x^{2}+a x+b\right)=3 x^{3}+(6+a) x^{2}+(2 a+b) x+2 b=0$, then compare <br> coefficients to find values of $a$ and $b$. [M1] $\begin{equation*} a=-11, b=6 \tag{A1} \end{equation*}$ <br> Alternative: <br> Factor theorem: Finding that $\mathrm{f}(3)=0 \therefore$ factor is, $\quad(x-3) \quad[\mathrm{M} 1, \mathrm{~A} 1]$ <br> Finding that $\mathrm{f}\left(\frac{2}{3}\right)=0 \therefore$ factor is, $\quad(3 x-2) \quad$ [M1, A1] <br> If just one of these is found, score the first 2 marks M1 A1 M0 A0. <br> Losing a factor of 3: $(x+2)\left(x-\frac{2}{3}\right)(x-3)$ scores M1 A1 M1 A0. <br> Answer only, one sign wrong: e.g. $(x+2)(3 x-2)(x+3)$ scores M1 A1 M1 A0. |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 3. | (a) $1+6 \mathrm{kx} \quad$ [Allow unsimplified versions, e.g. $1^{6}+6\left(1^{5}\right) k x,{ }^{6} C_{0}+{ }^{6} C_{1} k x$ ] $+\frac{6 \times 5}{2}(k x)^{2}+\frac{6 \times 5 \times 4}{3 \times 2}(k x)^{3} \quad$ [See below for acceptable versions] N.B. THIS NEED NOT BE SIMPLIFIED FOR THE A1 (isw is applied) <br> (b) $6 k=15 k^{2} \quad k=\frac{2}{5}$ (or equiv. fraction, or 0.4 ) <br> (Ignore $k=0$, if seen) <br> (c) $c=\frac{6 \times 5 \times 4}{3 \times 2}\left(\frac{2}{5}\right)^{3}=\frac{32}{25} \quad$ (or equiv. fraction, or 1.28) <br> (Ignore $x^{3}$, so $\frac{32}{25} x^{3}$ is fine) | B1 <br> M1 A1 <br> (3) <br> M1 A1cso <br> (2) <br> A1cso <br> (1) |
|  | (a) The terms can be 'listed' rather than added. <br> M1: Requires correct structure: ‘binomial coefficients’ (perhaps from Pascal’s triangle), increasing powers of $x$. Allow a 'slip' or 'slips' such as: $\begin{array}{ll} +\frac{6 \times 5}{2} k x^{2}+\frac{6 \times 5 \times 4}{3 \times 2} k x^{3}, & +\frac{6 \times 5}{2}(k x)^{2}+\frac{6 \times 5}{3 \times 2}(k x)^{3} \\ +\frac{5 \times 4}{2} k x^{2}+\frac{5 \times 4 \times 3}{3 \times 2} k x^{3}, & +\frac{6 \times 5}{2} x^{2}+\frac{6 \times 5 \times 4}{3 \times 2} x^{3} \end{array}$ <br> But: $15+k^{2} x^{2}+20+k^{3} x^{3}$ or similar is M0. <br> Both $x^{2}$ and $x^{3}$ terms must be seen. <br> $\binom{6}{2}$ and $\binom{6}{3}$ or equivalent such as ${ }^{6} C_{2}$ and ${ }^{6} C_{3}$ are acceptable, and <br> even $\left(\frac{6}{2}\right)$ and $\left(\frac{6}{3}\right)$ are acceptable for the method mark. <br> A1: Any correct (possibly unsimplified) version of these 2 terms. $\binom{6}{2} \text { and }\binom{6}{3} \text { or equivalent such as }{ }^{6} C_{2} \text { and }{ }^{6} C_{3} \text { are acceptable. }$ <br> Descending powers of $x$ : <br> Can score the M mark if the required first 4 terms are not seen. <br> Multiplying out $(1+k x)(1+k x)(1+k x)(1+k x)(1+k x)(1+k x)$ : <br> M1: A full attempt to multiply out (power 6) B1 and A1 as on the main scheme. <br> (b) M: Equating the coefficients of $x$ and $x^{2}$ (even if trivial, e.g. $6 k=15 k$ ). <br> Allow this mark also for the 'misread': equating the coefficients of $x^{2}$ and $x^{3}$ An equation in $k$ alone is required for this M mark, although... $\ldots \text { condone } 6 k x=15 k^{2} x^{2} \Rightarrow\left(6 k=15 k^{2} \Rightarrow\right) k=\frac{2}{5}$ |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 4. | (a) $\begin{align*} & 4^{2}=5^{2}+6^{2}-(2 \times 5 \times 6 \cos \theta) \\ & \cos \theta=\frac{5^{2}+6^{2}-4^{2}}{2 \times 5 \times 6} \\ & \quad\left(=\frac{45}{60}\right)=\frac{3}{4} \tag{*} \end{align*}$ <br> (b) $\sin ^{2} A+\left(\frac{3}{4}\right)^{2}=1$ <br> (or equiv. Pythag. method) <br> $\left(\sin ^{2} A=\frac{7}{16}\right) \quad \sin A=\frac{1}{4} \sqrt{ } 7 \quad$ or equivalent exact form, e.g. $\sqrt{\frac{7}{16}}, \sqrt{0.4375}$ | M1 <br> A1 <br> A1cso <br> (3) <br> M1 <br> A1 <br> (2) |
|  | (a) M: Is also scored for $5^{2}=4^{2}+6^{2}-(2 \times 4 \times 6 \cos \theta)$ <br> or $\quad 6^{2}=5^{2}+4^{2}-(2 \times 5 \times 4 \cos \theta)$ <br> or $\cos \theta=\frac{4^{2}+6^{2}-5^{2}}{2 \times 4 \times 6}$ or $\cos \theta=\frac{5^{2}+4^{2}-6^{2}}{2 \times 5 \times 4}$. <br> $1^{\text {st }} \mathrm{A}$ : Rearranged correctly and numerically correct (possibly unsimplified), in the form $\cos \theta=\ldots$ or $60 \cos \theta=45$ (or equiv. in the form $p \cos \theta=q$ ). <br> Alternative (verification): $\begin{equation*} 4^{2}=5^{2}+6^{2}-\left(2 \times 5 \times 6 \times \frac{3}{4}\right) \tag{M1} \end{equation*}$ <br> Evaluate correctly, at least to $16=25+36-45$ [A1] <br> Conclusion (perhaps as simple as a tick). <br> [A1cso] <br> (Just achieving $16=16$ is insufficient without at least a tick). <br> (b) M: Using a correct method to find an equation in $\sin ^{2} A$ or $\sin A$ which would give an exact value. <br> Correct answer without working (or with unclear working or decimals): Still scores both marks. |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 5. | (a) 1.414 (allow also exact answer $\sqrt{ } 2$ ), <br> 3.137 <br> Allow awrt <br> (b) $\frac{1}{2}(0.5) \ldots$. $\ldots .\{0+6+2(0.530+1.414+3.137)\}$ <br> $=4.04 \quad$ (Must be 3 s.f.) <br> (c) Area of triangle $=\frac{1}{2}(2 \times 6)$ <br> (Could also be found by integration, or even by the trapezium rule on $y=3 x$ ) <br> Area required = Area of triangle - Answer to (b) (Subtract either way round) <br> $6-4.04=1.96$ <br> Allow awrt <br> (ft from (b), dependent on the B1, and on answer to (b) less than 6) | B1, B1 <br> B1 <br> M1 A1ft <br> A1 <br> B1 <br> M1 <br> A1ft |
|  | (a) If answers are given to only 2 d.p. (1.41 and 3.14), this is B0 B0, but full marks can be given in part (b) if 4.04 is achieved. <br> (b) Bracketing mistake: i.e. $\frac{1}{2}(0.5)(0+6)+2(0.530+1.414+3.137)$ <br> scores B1 M1 A0 A0 unless the final answer implies that the calculation has been done correctly (then full marks can be given). <br> Alternative (finding and adding separate areas): $\frac{1}{2} \times \frac{1}{2}$ (Triangle/trapezium formulae, and height of triangle/trapezium)[B1] Fully correct method for total area, with values from table. <br> [M1, A1ft] 4.04 <br> (c) B1: Can be given for 6 with no working, but should not be given for 6 obtained from wrong working. <br> A1ft: This is a dependent follow-through: the B1 for 6 must have been scored, and the answer to (b) must be less than 6 . |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 6. | (a) $x=\frac{\log 0.8}{\log 8}$ or $\log _{8} 0.8, \quad=-0.107 \quad$ Allow awrt <br> (b) $2 \log x=\log x^{2}$ $\log x^{2}-\log 7 x=\log \frac{x^{2}}{7 x}$ <br> "Remove logs" to form equation in $x$, using the base correctly: $\quad \frac{x^{2}}{7 x}=3$ $x=21 \quad \text { (Ignore } x=0, \text { if seen) }$ | M1, A1 B1 M1 M1 A1cso |
|  | (a) Allow also the 'implicit' answer $8^{-0.107}$ (M1 A1). <br> Answer only: -0.107 or awrt: Full marks. <br> Answer only: -0.11 or awrt (insufficient accuracy): M1 A0 <br> Trial and improvement: Award marks as for "answer only". <br> (b) Alternative: $\begin{aligned} & 2 \log x=\log x^{2} \\ & \log 7 x+1=\log 7 x+\log 3=\log 21 x \end{aligned}$ <br> "Remove logs" to form equation in $x$ : $x^{2}=21 x$ <br> Alternative: $\begin{array}{lll} \hline \log 7 x=\log 7+\log x & & \text { B1 } \\ 2 \log x-(\log 7+\log x)=1 & & \\ \log _{3} x=1+\log _{3} 7 & & \text { M1 } \\ x=3^{\left(1+\log _{3} 7\right)} \quad\left(=3^{2.771 \ldots}\right) & \text { or } & \log _{3} x=\log _{3} 3+\log _{3} 7 \\ x=21 & \text { M1 } \\ x= & & \text { A1 } \end{array}$ <br> Attempts using change of base will usually require the same steps as in the main scheme or alternatives, so can be marked equivalently. <br> A common mistake: $\begin{array}{ll} \log x^{2}-\log 7 x=\frac{\log x^{2}}{\log 7 x} & \text { B1 M0 } \\ \frac{x^{2}}{7 x}=3 & x=21 \end{array} \text { M1(‘Recovery'), but A0 }$ |  |


| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 7. | (a) Gradient of AM: $\frac{1-(-2)}{3-1}=\frac{3}{2} \quad$ or $\frac{-3}{-2}$ <br> Gradient of $l: \quad=-\frac{2}{3} \quad$ M: use of $m_{1} m_{2}=-1$, or equiv. <br> $y-1=-\frac{2}{3}(x-3)$ or $\frac{y-1}{x-3}=-\frac{2}{3} \quad[3 y=-2 x+9] \quad$ (Any equiv. form) <br> (b) $x=6: \quad 3 y=-12+9=-3 \quad y=-1 \quad$ (or show that for $y=-1, x=6$ ) $\quad(*)$ <br> (A conclusion is not required). <br> (c) $\left(r^{2}=\right)(6-1)^{2}+(-1-(-2))^{2}$ <br> M: Attempt $r^{2}$ or $r$ <br> N.B. Simplification is not required to score M1 A1 <br> $(x \pm 6)^{2}+(y \pm 1)^{2}=k, \quad k \neq 0 \quad$ (Value for $k$ not needed, could be $r^{2}$ or $r$ ) $(x-6)^{2}+(y+1)^{2}=26$ (or equiv.) <br> Allow $(\sqrt{26})^{2}$ or other exact equivalents for 26. <br> (But... $(x-6)^{2}+(y--1)^{2}=26$ scores M1 A0) <br> (Correct answer with no working scores full marks) | B1 <br> M1 <br> M1 A1 <br> (4) <br> B1 <br> (1) <br> M1 A1 <br> M1 <br> A1 <br> (4) |
|  | (a) $2^{\text {nd }} \mathrm{M} 1$ : eqn. of a straight line through $(3,1)$ with any gradient except 0 or $\infty$. <br> Alternative: Using $(3,1)$ in $y=m x+c$ to find a value of $c$ scores M1, but an equation (general or specific) must be seen. <br> Having coords the wrong way round, e.g. $y-3=-\frac{2}{3}(x-1)$, loses the $2^{\text {nd }} \mathrm{M}$ mark unless a correct general formula is seen, e.g. $y-y_{1}=m\left(x-x_{1}\right)$. <br> If the point $P(6,-1)$ is used to find the gradient of $M P$, maximum marks are (a) B0 M0 M1 A1 (b) B0. <br> (c) $1^{\text {st }} \mathrm{M} 1$ : Condone one slip, numerical or sign, inside a bracket. <br> Must be attempting to use points $P(6,-1)$ and $A(1,-2)$, or perhaps $P$ and $B$. (Correct coordinates for $B$ are $(5,4)$ ). <br> $1^{\text {st }} \mathrm{M}$ alternative is to use a complete Pythag. method on triangle MAP, n.b. $M P=M A=\sqrt{13}$. <br> Special case: <br> If candidate persists in using their value for the $y$-coordinate of $P$ instead of the given -1 , allow the M marks in part (c) if earned. |  |




| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 10. | (a) $4 x^{2}+6 x y=600$ $\begin{equation*} V=2 x^{2} y=2 x^{2}\left(\frac{600-4 x^{2}}{6 x}\right) \quad V=200 x-\frac{4 x^{3}}{3} \tag{*} \end{equation*}$ <br> (b) $\frac{\mathrm{d} V}{\mathrm{~d} x}=200-4 x^{2}$ <br> Equate their $\frac{\mathrm{d} V}{\mathrm{~d} x}$ to 0 and solve for $x^{2}$ or $x: x^{2}=50$ or $x=\sqrt{50 \quad(7.07 \ldots)}$ <br> Evaluate $V: \quad V=200(\sqrt{ } 50)-\frac{4}{3}(50 \sqrt{ } 50)=943 \mathrm{~cm}^{3} \quad$ Allow awrt <br> (c) $\frac{\mathrm{d}^{2} V}{\mathrm{~d} x^{2}}=-8 x \quad$ Negative, <br> $\therefore$ Maximum | M1 A1  <br> M1 A1cso (4) <br> B1  <br> M1 A1  <br> M1 A1 (5) <br> M1, A1ft (2) <br>  $\mathbf{1 1}$ |
|  | (a) $1^{\text {st }} \mathrm{M}$ : Attempting an expression in terms of $x$ and $y$ for the total surface area (the expression should be dimensionally correct). <br> $1^{\text {st }} \mathrm{A}$ : Correct expression (not necessarily simplified), equated to 600 . <br> $2^{\text {nd }} \mathrm{M}$ : Substituting their $y$ into $2 x^{2} y$ to form an expression in terms of $x$ only. (Or substituting $y$ from $2 x^{2} y$ into their area equation). <br> (b) $1^{\text {st }} \mathrm{A}$ : Ignore $x=-\sqrt{50}$, if seen. <br> The $2^{\text {nd }} \mathrm{M}$ mark (for substituting their $x$ value into the given expression for $V$ ) is dependent on the $1^{\text {st }} \mathrm{M}$. <br> Final A: Allow also exact value $\frac{400 \sqrt{ } 50}{3}$ or $\frac{2000 \sqrt{ } 2}{3}$ or equiv. single term. <br> (c) Allow marks if the work for (c) is seen in (b) (or vice-versa). <br> M: Find second derivative and consider its sign. <br> A: Second derivative following through correctly from their $\frac{d V}{d x}$, and correct reason/conclusion (it must be a maximum, not a minimum). <br> An actual value of $x$ does not have to be used... this mark can still be awarded if no $x$ value has been found or if a wrong $x$ value is used. <br> Alternative: <br> M: Find value of $\frac{\mathrm{d} V}{\mathrm{~d} x}$ on each side of " $x=\sqrt{ } 50$ " and consider sign. <br> A: Indicate sign change of positive to negative for $\frac{\mathrm{d} V}{\mathrm{~d} x}$, and conclude max. <br> Alternative: <br> M: Find value of $V$ on each side of " $x=\sqrt{ } 50$ " and compare with " 943 ". <br> A: Indicate that both values are less than 943 , and conclude max. |  |

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## Mark Scheme (Results) J anuary 2008

## GCE

## GCE Mathematics (6664/ 01)

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 1. <br> a)i) <br> ii) <br> (b) | $\begin{aligned} & f(3)=3^{3}-2 \times 3^{2}-4 \times 3+8 \quad ;=5 \\ & f(-2)=(-8-8+8+8)=0 \end{aligned}$ <br> ( B1 on Epen, but A1 in fact) M1 is for attempt at either $f(3)$ or $f(-3)$ in (i) or $f(-2)$ or $f(2)$ in (ii). $\begin{array}{cl} {[(x+2)]\left(x^{2}-4 x+4\right)} & (=0 \text { not required) [must be seen or used in (b) }] \\ (x+2)(x-2)^{2} & (=0) \quad(\text { can imply previous } 2 \text { marks }) \end{array}$ <br> Solutions: $x=2$ or -2 (both) or ( $-2,2,2$ ) A1 (4) | M1; A1 <br> A1 <br> (3) <br> M1 A1 <br> M1 |
| Notes: (a) ${ }^{\text {(b) }}$ (b) | No working seen: Both answers correct scores full marks <br> One correct ;M1 then A1B0 or A0B1, whichever appropriate. <br> Alternative (Long division) <br> Divide by $(x-3) \mathrm{OR}(x+2)$ to get $x^{2}+a x+b$, a may be zero [M1] $x^{2}+x-1 \text { and }+5 \text { seen i.s.w. (or "remainder }=5 \text { ") } \quad[A 1]$ $\begin{equation*} x^{2}-4 x+4 \text { and } 0 \text { seen } \quad \text { (or "no remainder") } \tag{B1} \end{equation*}$ <br> First M1 requires division by a found factor ; e.g $(x+2),(x-2)$ or what candidate thinks is a factor to get $\left(x^{2}+a x+b\right), \quad a$ may be zero. <br> First A1 for $[(x+2)]\left(x^{2}-4 x+4\right)$ or $(x-2)\left(x^{2}-4\right)$ <br> Second M1:attempt to factorise their found quadratic. (or use formula correctly) <br> [Usual rule: $x^{2}+a x+b=(x+c)(x+d)$, where $\|c d\|=\|b\|$.] <br> N.B. Second A1 is for solutions, not factors <br> Alternative (first two marks) <br> $(x+2)\left(x^{2}+b x+c\right)=x^{3}+(2+b) x^{2}+(2 b+c) x+2 c=0$ and then compare $\begin{align*} & \text { with } x^{3}-2 x^{2}-4 x+8=0 \text { to find } b \text { and } c . \quad \text { [M1] } \\ & b=-4, c=4 \tag{A1} \end{align*}$ <br> Method of grouping $\begin{array}{r} x^{3}-2 x^{2}-4 x+8=x^{2}(x-2), 4(x \pm 2) \mathrm{M} 1 ;=x^{2}(x-2)-4(x-2) \mathrm{A} 1 \\ {\left[=\left(x^{2}-4\right)(x-2)\right]=(x+2)(x-2)^{2} \mathrm{M} 1} \end{array}$ <br> Solutions: $x=2, x=-2$ both A1 <br> Complete method, using terms of form $a r^{k}$, to find $r$ [e.g. Dividing $a r^{6}=80$ by $a r^{3}=10$ to find $r ; r^{6}-r^{3}=8$ is MO] $r=2$ <br> Complete method for finding a [e.g. Substituting value for $r$ into equation of form $\operatorname{ar}^{k}=10$ or 80 and finding a value for $a$.] | M1 <br> A1 (2) <br> M1 |


| (c) | $(8 a=10) \quad a=\frac{5}{4}=1 \frac{1}{4} \quad$ (equivalent single fraction or 1.25 ) <br> Substituting their values of $a$ and $r$ into correct formula for sum. $S=\frac{a\left(r^{n}-1\right)}{r-1}=\frac{5}{4}\left(2^{20}-1\right) \quad(=1310718.75) \quad 1310719 \text { (only this) }$ | A1 (2) <br> M1 <br> A1 (2) [6] |
| :---: | :---: | :---: |
| Notes: | (a) M1: Condone errors in powers, e.g. $a r^{4}=10$ and/or $a r^{7}=80$, <br> A1: For $r=2$, allow even if $a r^{4}=10$ and $a r^{7}=80$ used (just these) <br> ( M mark can be implied from numerical work, if used correctly) <br> (b) M1: Allow for numerical approach: e.g. $\frac{10}{r_{c}{ }^{3}} \leftarrow \frac{10}{r_{c}{ }^{2}} \leftarrow \frac{10}{r_{c}} \leftarrow 10$ <br> In (a) and (b) correct answer, with no working, allow both marks. <br> (c) Attempt 20 terms of series and add is M1 (correct last term 655360) If formula not quoted, errors in applying their a and/or $r$ is M0 Allow full marks for correct answer with no working seen. |  |
| 3. <br> (a) <br> (b) | $\begin{aligned} & \left(1+\frac{1}{2} x\right)^{10}=1+\frac{\binom{10}{1}\left(\frac{1}{2} x\right)+\binom{10}{2}\left(\frac{1}{2} x\right)^{2}+\binom{10}{3}\left(\frac{1}{2} x\right)^{3}}{} \\ & =1+5 x ;+\frac{45}{4}(\text { or } 11.25) x^{2}+15 x^{3}(\text { coeffs need to be these, i.e, simplified }) \end{aligned}$ <br> [Allow A1A0, if totally correct with unsimplified, single fraction coefficients) $\begin{aligned} \left(1+\frac{1}{2} \times 0.01\right)^{10} & =1+5(0.01)+\left(\frac{45}{4} \text { or } 11.25\right)(0.01)^{2}+15(0.01)^{3} \\ & =1+0.05+0.001125+0.000015 \\ & =1.05114 \quad \text { cao } \end{aligned}$ | M1 A1 <br> A1; A1 (4) <br> M1 A1 $\sqrt{ }$ <br> A1 (3) [7] |
| Notes: | (a) For M1 first A1: Consider underlined expression only. <br> M1 Requires correct structure for at least two of the three terms: <br> (i) Must be attempt at binomial coefficients. <br> (ii) Must have increasing powers of $x$, <br> (iii) May be listed, need not be added; this applies for all marks. <br> First A1: Requires all three correct terms but need not be simplified, allow $1{ }^{10}$ etc, ${ }^{10} C_{2}$ etc, and condone omission of brackets around powers of $1 / 2 x$ Second A1: Consider as B1 for $1+5 x$ <br> (b) For M1: Substituting their (0.01) into their (a) result First A1 (f.t.): Substitution of (0.01) into their 4 termed expression in (a) Answer with no working scores no marks (calculator gives this answer) |  |


| 4. (a) <br> (b) |  | M1 <br> A1 (2) <br> M1 <br> A1 <br> M1; A1 $\sqrt{ }$ <br> M1A1 (7) <br> [9] |
| :---: | :---: | :---: |

Notes: (a) N.B: AG; need to see at least one line of working after substituting $\cos ^{2} \theta$.
(b) First M1: Using $5 \sin ^{2} \theta=3$ to find value for $\sin \theta$ or $\theta$

Second M1: Considering the - value for $\sin \theta$. (usually later)
First A1: Given for awrt $50.8^{\circ}$. Not dependent on second M.
Third M1: For (180-50.8c) ${ }^{\circ}$, need not see written down
Final M1: Dependent on second M (but may be implied by answers) For ( $180+$ candidate' s 50.8$)^{\circ}$ or $(360-50.8 \mathrm{c})^{\circ}$ or equiv.
Final A1: Requires both values. (no follow through)
[ Finds $\cos ^{2} \theta=k \quad(k=2 / 5)$ and so $\cos \theta=( \pm) \ldots \mathrm{M} 1$, then mark equivalently]

| 5. | Method 1 (Substituting $\mathrm{a}=3 \mathrm{~b}$ into second equation at some stage) <br> Using a law of logs correctly (anywhere) <br> Substitution of $3 b$ for $a$ (or $a / 3$ for $b$ ) $\begin{aligned} & \text { e.g. } \log _{3} a b=2 \\ & \text { e.g. } \quad \log _{3} 3 b^{2}=2 \end{aligned}$ <br> Using base correctly on correctly derived $\log _{3} p=q \quad$ e.g. $3 b^{2}=3^{2}$ <br> First correct value $b=\sqrt{ } 3\left(\text { allow } 3^{1 / 2}\right)$ <br> Correct method to find other value ( dep. on at least first $M$ mark) <br> Second answer $a=3 b=3 \sqrt{ } 3 \text { or } \sqrt{ } 27$ <br> Method 2 (Working with two equations in $\log _{3} a$ and $\log _{3} b$ ) <br> " Taking logs" of first equation and " separating" $\begin{aligned} & \log _{3} a=\log _{3} 3+\log _{3} b \\ & \left(=1+\log _{3} b\right) \end{aligned}$ <br> Solving simultaneous equations to find $\log _{3} a$ or $\log _{3} b$ $\left[\log _{3} a=11 / 2, \quad \log _{3} b=1 / 2\right]$ <br> Using base correctly to find a or b <br> Correct value for $a$ or $b$ $a=3 \sqrt{ } 3 \text { or } b=\sqrt{ } 3$ <br> Correct method for second answer, dep. on first M ; correct second answer [lgnore negative values] | M1 <br> M1 <br> M1 <br> A1 <br> M1 <br> A1 <br> M1 <br> M1 <br> M1 <br> A1 <br> M1;A1[6] |
| :---: | :---: | :---: |
| Notes: | Answers must be exact; decimal answers lose both A marks <br> There are several variations on Method 1, depending on the stage at which <br> $a=3 b$ is used, but they should all mark as in scheme. <br> In this method, the first three method marks on Epen are for <br> (i) First M1: correct use of log law, <br> (ii) Second M1: substitution of $a=3 b$, <br> (iii) Third M1: requires using base correctly on correctly derived $\log _{3} \mathrm{p}=\mathrm{q}$ |  |


| 6. <br> (a) <br> (b) |  $\begin{aligned} B C^{2} & =700^{2}+500^{2}-2 \times 500 \times 700 \cos 15^{\circ} \\ ( & =63851.92 \ldots) \\ B C & =253 \text { awrt } \\ \frac{\sin B}{700} & =\frac{\sin 15}{\text { candidate's } B C} \end{aligned}$ <br> $\sin B=\sin 15 \times 700 / 253_{\mathrm{c}}=0.716 .$. and giving an obtuse $B \quad\left(134.2^{\circ}\right)$ dep <br> $\theta=180^{\circ}$ - candidate's angle $B \quad$ (Dep. on first M only, B can be acute) $\theta=180-134.2=(0) 45.8 \quad$ (allow 46 or awrt 45.7, 45.8, 45.9) <br> [46 needs to be from correct working] | M1 A1 A1 (3) M1 M1 A1 (4) [7] |
| :---: | :---: | :---: |
| Notes: | (a) If use $\cos 15^{\circ}=\ldots .$. , then A 1 not scored until written as $\mathrm{BC}^{2}=\ldots$ correctly <br> Splitting into 2 triangles BAX and CAX, where $X$ is foot of perp. from $B$ to $A C$ <br> Finding value for $B X$ and $C X$ and using Pythagoras <br> M1 $\begin{aligned} & B C^{2}=\left(500 \sin 15^{\circ}\right)^{2}+\left(700-500 \cos 15^{\circ}\right)^{2} \\ & B C=253 \text { awrt } \end{aligned}$ A1 <br> (b) Several alternative methods: (Showing the M marks, $3^{\text {rd }} \mathrm{M}$ dep. on first M )) <br> (i) $\cos B=\frac{500^{2}+\text { candidate's } B C^{2}-700^{2}}{2 \times 500 x c a n d i d a t e ' s B C}$ or $700^{2}=500^{2}+B C_{c}{ }^{2}-2 \times 500 x B C_{c}$ M1 <br> Finding angle $B$ M1, then M1 as above <br> (ii) 2 triangle approach, as defined in notes for (a) $\tan C B X=\frac{700-\text { valueforAX }}{\text { valuefor } B X}$ <br> Finding value for $\angle C B X \quad\left(\approx 59^{\circ}\right) \quad$ M1 $\theta=\left[180^{\circ}-\left(75^{\circ}+\text { candidate's } \angle C B X\right)\right]$ M1 <br> (iii) Using sine rule (or cos rule) to find $C$ first: <br> Correct use of sine or cos rule for C M1, <br> (iv) $700 \cos 15^{\circ}=500+B C \cos \theta \quad$ M2 \{first two Ms earned in this case\} <br> Solving for $\theta ; \theta=45.8$ (allow 46 or5.7, 45.8, 45.9 M1;A1 |  |


| $7$ <br> (a) <br> (b) <br> (c) | Either solving $0=x(6-x)$ and showing $x=6($ and $x=0)$ <br> or showing $(6,0)$ (and $x=0$ ) satisfies $y=6 x-x^{2} \quad$ [allow for showing $x=6$ ] <br> Solving $\quad 2 x=6 x-x^{2} \quad\left(x^{2}=4 x\right) \quad$ to $x=.$. $x=4 \quad(\text { and } x=0)$ <br> Conclusion: when $x=4, y=8$ and when $x=0, y=0$, <br> (Area $=) \int_{(0)}^{(4)}\left(6 x-x^{2}\right) \mathrm{d} x \quad$ Limits not required <br> Correct integration $\quad 3 x^{2}-\frac{x^{3}}{3} \quad(+\mathrm{c})$ <br> Correct use of correct limits on their result above (see notes on limits) <br> [" $3 x^{2}-\frac{x^{3}}{3}$ "] $]^{4}-\left[\text { " } 3 x^{2}-\frac{x^{3}}{3} \text { " }\right]_{0}$ with limits substituted $\left[=48-21 \frac{1}{3}=26 \frac{2}{3}\right.$ ] <br> Area of triangle $=2 \times 8=16 \quad$ (Can be awarded even if no $M$ scored, i.e. B1) <br> Shaded area $= \pm$ (area under curve - area of triangle ) applied correctly $\left(=26 \frac{2}{3}-16\right) \quad=10 \frac{2}{3} \quad(\text { awrt 10.7 })$ | B 1 $(1)$ <br> M 1  <br> A1  <br> A1 $(3)$ <br> M1  <br> A1  <br> M1  <br> A1  <br> M1  <br> A1 (6)[10]  |
| :---: | :---: | :---: |
| Notes | (b) In scheme first A1: need only give $x=4$ <br> If verifying approach used: <br> Verifying $(4,8)$ satisfies both the line and the curve M 1 (attempt at both), <br> Both shown successfully <br> For final A1, $(0,0)$ needs to be mentioned ; accept " clear from diagram" <br> (c) Alternative Using Area $= \pm \int_{(0)}^{(4)}\left\{\left(6 x-x^{2}\right) ;-2 x\right\} \mathrm{d} x \quad$ approach <br> (i) If candidate integrates separately can be marked as main scheme If combine to work with $= \pm \int_{(0)}^{(4)}\left(4 x-x^{2}\right) \mathrm{d} x, \quad$ first $M$ mark and third $M$ mark $=( \pm)\left[2 x^{2}-\frac{x^{3}}{3}(+\mathrm{c})\right] \quad \mathrm{A} 1$ <br> Correct use of correct limits on their result second M1, <br> Totally correct, unsimplified $\pm$ expression (may be implied by correct ans.) A1 <br> $10^{2 / 3}$ A1 [Allow this if, having given - $10^{2} / 3$, they correct it] <br> M1 for correct use of correct limits: Must substitute correct limits for their strategy into a changed expression and subtract, either way round, e.g $\pm\left\{[]^{4}-[]_{0}\right.$ <br> If a long method is used, e,g, finding three areas, this mark only gained for correct strategy and all limits need to be correct for this strategy. <br> Use of trapezium rule: MOAOMAO, possibleA1for triangle M1(if correct application of trap. rule from $x=0$ to $x=4$ ) A0 |  |



| (a) <br> (b) <br> (c) <br> (d) | $($ Total area $)=3 x y+2 x^{2}$ <br> (Vol: ) $\quad x^{2} y=100 \quad\left(y=\frac{100}{x^{2}}, x y=\frac{100}{x}\right)$ <br> Deriving expression for area in terms of $x$ only <br> (Substitution, or clear use of, $y$ or $x y$ into expression for area) <br> $($ Area $=) \frac{300}{x}+2 x^{2}$ <br> AG $\frac{\mathrm{d} A}{\mathrm{~d} x}=-\frac{300}{x^{2}}+4 x$ <br> Setting $\frac{\mathrm{d} A}{\mathrm{~d} x}=0$ and finding a value for correct power of $x$, for cand. M1 [ $\left.\quad x^{3}=75\right]$ <br> $x=4.2172$ awrt $4.22 \quad$ (allow exact $\sqrt[3]{75}$ ) $\frac{\mathrm{d}^{2} A}{\mathrm{~d} x^{2}}=\frac{600}{x^{3}}+4=\text { positive } \quad \text { therefore minimum }$ <br> Substituting found value of $x$ into (a) <br> (Or finding $y$ for found $x$ and substituting both in $3 x y+2 x^{2}$ ) $\left[y=\frac{100}{4.2172^{2}}=5.6228\right]$ <br> Area $=106.707$ | B1 <br> B1 <br> M1 <br> A1 cso (4) <br> M1A1 <br> A1 (4) <br> M1A1 (2) <br> M1 <br> A1 (2) <br> [12] |
| :---: | :---: | :---: |
| Notes | (a) First B1: Earned for correct unsimplified expression, isw. <br> (c) For M1: Find $\frac{\mathrm{d}^{2} A}{\mathrm{~d} x^{2}}$ and explicitly consider its sign, state $>0$ or "positive" <br> A1: Candidate's $\frac{\mathrm{d}^{2} A}{\mathrm{~d} x^{2}}$ must be correct for their $\frac{\mathrm{d} A}{\mathrm{~d} x}$, sign must be +ve and conclusion "so minimum", (allow QED, $\sqrt{ }$ ). ( may be wrong $x$, or even no value of $x$ found) <br> Alternative: M1: Find value of $\frac{\mathrm{d} A}{\mathrm{~d} x}$ on either side of " $x=\sqrt[3]{75}$ " and consider sign <br> A1: Indicate sign change of negative to positive for $\frac{\mathrm{d} A}{\mathrm{~d} x}$, and conclude minimum. <br> OR M1: Consider values of A on either side of " $x=\sqrt[3]{75}$ " and compare with" 107 " <br> A1: Both values greater than " $x=107$ " and conclude minimum. <br> Allow marks for (c) and (d) where seen; even if part labelling confused. |  |

$\square$

# Mark Scheme (Results) 

## Summer 2008

## GCE Mathematics (6664/ 01)

GCE

## J une 2008 <br> Core Mathematics C2 Mark Scheme

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 1. | (a) Attempt to find $\mathrm{f}(-4)$ or $\mathrm{f}(4) . \quad\left(\mathrm{f}(-4)=2(-4)^{3}-3(-4)^{2}-39(-4)+20\right)$ $(=-128-48+156+20)=0$, so $(x+4)$ is a factor. <br> (b) $2 x^{3}-3 x^{2}-39 x+20=(x+4)\left(2 x^{2}-11 x+5\right)$ <br> ..... $(2 x-1)(x-5)$ <br> (The 3 brackets need not be written together) or ..... $\left(x-\frac{1}{2}\right)(2 x-10)$ or equivalent | M1 <br> M1 A1 M1 A1cso |
|  | (a) Long division scores no marks in part (a). The factor theorem is required. However, the first two marks in (b) can be earned from division seen in (a)... ... but if a different long division result is seen in (b), the work seen in (b) takes precedence for marks in (b). <br> A1 requires zero and a simple conclusion (even just a tick, or Q.E.D.), or may be scored by a preamble, e.g. 'If $\mathrm{f}(-4)=0,(x+4)$ is a factor.....' <br> (b) First M requires use of $(x+4)$ to obtain $\left(2 x^{2}+a x+b\right), a \neq 0, b \neq 0$, even with a remainder. Working need not be seen... this could be done 'by inspection' Second M for the attempt to factorise their three-term quadratic. <br> Usual rule: $\left(k x^{2}+a x+b\right)=(p x+c)(q x+d)$, where $\|c d\|=\|b\|$ and $\|p q\|=\|k\|$. If 'solutions' appear before or after factorisation, ignore... ... but factors must be seen to score the second M mark. <br> Alternative (first 2 marks): <br> $(x+4)\left(2 x^{2}+a x+b\right)=2 x^{3}+(8+a) x^{2}+(4 a+b) x+4 b=0$, then compare <br> coefficients to find values of $a$ and $b$. [M1] $\begin{equation*} \overline{a=-11}, b=5 \tag{A1} \end{equation*}$ <br> Alternative: <br> Factor theorem: Finding that $\mathrm{f}\left(\frac{1}{2}\right)=0 \therefore$ factor is, $(2 x-1) \quad$ [M1, A1] <br> Finding that $\mathrm{f}(5)=0 \therefore$ factor is, $\quad(x-5) \quad$ [M1, A1] <br> "Combining" all 3 factors is not required. <br> If just one of these is found, score the first 2 marks M1 A1 M0 A0. <br> Losing a factor of 2: $(x+4)\left(x-\frac{1}{2}\right)(x-5)$ scores M1 A1 M1 A0. <br> Answer only, one sign wrong: e.g. $(x+4)(2 x-1)(x+5)$ scores M1 A1 M1 A0 |  |

## J une 2008 <br> Core Mathematics C2 <br> Mark Scheme



## J une 2008 <br> Core Mathematics C2 <br> Mark Scheme

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 3. | (a) $(1+a x)^{10}=1+10 a x \ldots . . \quad$ (Not unsimplified versions) $+\frac{10 \times 9}{2}(a x)^{2}+\frac{10 \times 9 \times 8}{6}(a x)^{3} \quad$ Evidence from one of these terms is sufficient $+45(a x)^{2},+120(a x)^{3}$ or $+45 a^{2} x^{2},+120 a^{3} x^{3}$ <br> (b) $120 a^{3}=2 \times 45 a^{2} \quad a=\frac{3}{4}$ or equiv. (e.g. $\left.\frac{90}{120}, 0.75\right) \quad$ Ignore $a=0$, if seen | B1  <br> M1  <br> A1, A1 (4) <br> M1 A1 (2) <br>  6 <br>   |
|  | (a) The terms can be 'listed' rather than added. <br> M1: Requires correct structure: ‘binomial coefficient’ (perhaps from Pascal’s triangle) and the correct power of $x$. <br> (The M mark can also be given for an expansion in descending powers of $x$ ). Allow 'slips' such as: $\frac{10 \times 9}{2} a x^{2}, \quad \frac{10 \times 9}{3 \times 2}(a x)^{3}, \quad \frac{10 \times 9}{2} x^{2}, \quad \frac{9 \times 8 \times 7}{3 \times 2} a^{3} x^{3}$ <br> However, $45+a^{2} x^{2}+120+a^{3} x^{3}$ or similar is M0. <br> $\binom{10}{2}$ and $\binom{10}{3}$ or equivalent such as ${ }^{10} C_{2}$ and ${ }^{10} C_{3}$ are acceptable, and <br> even $\left(\frac{10}{2}\right)$ and $\left(\frac{10}{3}\right)$ are acceptable for the method mark. <br> $1^{\text {st }} \mathrm{A} 1$ : Correct $x^{2}$ term. $2^{\text {nd }} \mathrm{A} 1$ : Correct $x^{3}$ term (These must be simplified). If simplification is not seen in (a), but correct simplified terms are seen in (b), these marks can be awarded. However, if wrong simplification is seen in (a), this takes precedence. <br> Special case: <br> If $(a x)^{2}$ and $(a x)^{3}$ are seen within the working, but then lost... <br> ... A1 A0 can be given if $45 a x^{2}$ and120ax ${ }^{3}$ are both achieved. <br> (b) M: Equating their coefficent of $x^{3}$ to twice their coefficient of $x^{2} \ldots$ <br> $\cdots$ or equating their coefficent of $x^{2}$ to twice their coefficient of $x^{3}$. <br> ( $\ldots$ or coefficients can be correct coefficients rather than their coefficients) <br> Allow this mark even if the equation is trivial, e.g. $120 a=90 a$. <br> An equation in $a$ alone is required for this M mark, although... <br> ...condone, e.g. $120 a^{3} x^{3}=90 a^{2} x^{2} \Rightarrow\left(120 a^{3}=90 a^{2} \Rightarrow\right) a=\frac{3}{4}$. <br> Beware: $a=\frac{3}{4}$ following $120 a=90 a$, which is A0. |  |

## J une 2008 <br> Core Mathematics C2 Mark Scheme



## J une 2008 <br> Core Mathematics C2 Mark Scheme

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 5. |  | M1 A1 <br> M1 <br> A1 <br> (4) <br> B1 <br> M1 <br> M1 A1ft <br> A1 <br> (5) |
|  | (a) For the M mark, condone one slip inside a bracket, e.g. $(8-3)^{2}+(3+1)^{2}$, $(8-1)^{2}+(1-3)^{2}$ <br> The first two marks may be gained implicitly from the circle equation. <br> (b) $2^{\text {nd }} \mathrm{M}$ : Eqn. of line through ( 8,3 ), in any form, with any grad.(except 0 or $\infty$ ). If the 8 and 3 are the 'wrong way round', this M mark is only given if a correct general formula, e.g. $y-y_{1}=m\left(x-x_{1}\right)$, is quoted. <br> Alternative: $2^{\text {nd }} \mathrm{M}$ : Using $(8,3)$ and an $m$ value in $y=m x+c$ to find a value of $c$. <br> A1ft: as in main scheme. <br> (Correct substitution of 8 and 3, then a wrong $c$ value will still score the A1ft) <br> (b) Alternatives for the first 2 marks: (but in these 2 cases the $1^{\text {st }} \mathrm{A}$ mark is not ft ) <br> (i) Finding gradient of tangent by implicit differentiation $2(x-3)+2(y-1) \frac{\mathrm{d} y}{\mathrm{~d} x}=0 \quad \text { (or equivalent) }$ <br> Subs. $x=8$ and $y=3$ into a 'derived' expression to find a value for $\mathrm{d} y / \mathrm{d} x$ <br> (ii) Finding gradient of tangent by differentiation of $y=1+\sqrt{20+6 x-x^{2}}$ $\frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{1}{2}\left(20+6 x-x^{2}\right)^{-\frac{1}{2}}(6-2 x) \quad \text { (or equivalent) }$ <br> Subs. $x=8$ into a 'derived' expression to find a value for $\mathrm{d} y / \mathrm{d} x$ <br> Another alternative: $\begin{array}{ll} \text { Using } x x_{1}+y y_{1}+g\left(x+x_{1}\right)+f\left(y+y_{1}\right)+c=0 \\ x^{2}+y^{2}-6 x-2 y-19=0 & \text { B1 }  \tag{B1}\\ 8 x+3 y,-3(x+8)-(y+3)-19=0 & \text { M1, M1 A1ft (ft from circle eqn.) } \\ 5 x+2 y-46=0 & \text { A1 } \end{array}$ |  |

## J une 2008 <br> Core Mathematics C2 <br> Mark Scheme



## J une 2008 <br> Core Mathematics C2 Mark Scheme

\begin{tabular}{|c|c|c|c|}
\hline Question number \& Scheme \& \multicolumn{2}{|l|}{Marks} \\
\hline 7. \& \begin{tabular}{l}
(a) \(r \theta=7 \times 0.8=5.6(\mathrm{~cm})\) \\
(b) \(\frac{1}{2} r^{2} \theta=\frac{1}{2} \times 7^{2} \times 0.8=19.6\left(\mathrm{~cm}^{2}\right)\) \\
(c) \(B D^{2}=7^{2}+(\text { their } A D)^{2}-(2 \times 7 \times(\) their \(A D) \times \cos 0.8)\)
\[
\begin{aligned}
\& B D^{2}=7^{2}+3.5^{2}-(2 \times 7 \times 3.5 \times \cos 0.8) \quad \text { (or awrt } 46^{\circ} \text { for the angle) } \\
\& (B D=5.21)
\end{aligned}
\] \\
Perimeter \(=(\) their \(D C)+" 5.6 "+" 5.21 "=14.3(\mathrm{~cm})\) \\
(Accept awrt) \\
(d) \(\triangle A B D=\frac{1}{2} \times 7 \times(\) their \(A D) \times \sin 0.8 \quad\) (or awrt \(46^{\circ}\) for the angle) (ft their \(A D\) ) (=8.78...) \\
(If the correct formula \(\frac{1}{2} a b \sin C\) is quoted the use of any two of the sides of \(\triangle A B D\) as \(a\) and \(b\) scores the M mark). \\
Area \(=\) "19.6" - "8.78 ..." = \(10.8\left(\mathrm{~cm}^{2}\right)\) (Accept awrt)
\end{tabular} \& \begin{tabular}{l}
M1 A1 \\
M1 A1 \\
M1 \\
A1 \\
M1 A1 \\
M1 A1ft \\
M1 A1
\end{tabular} \& (2)
(2)
(4)

(4) <br>

\hline \& | Units ( cm or $\mathrm{cm}^{2}$ ) are not required in any of the answers. |
| :--- |
| (a) and (b): Correct answers without working score both marks. |
| (a) M: Use of $r \theta$ (with $\theta$ in radians), or equivalent (could be working in degrees with a correct degrees formula). |
| (b) M: Use of $\frac{1}{2} r^{2} \theta$ (with $\theta$ in radians), or equivalent (could be working in degrees with a correct degrees formula). |
| (c) $1^{\text {st }} \mathrm{M}$ : Use of the (correct) cosine rule formula to find $B D^{2}$ or $B D$. |
| Any other methods need to be complete methods to find $B D^{2}$ or $B D$. $2^{\text {nd }} \mathrm{M}$ : Adding their $D C$ to their arc $B C$ and their $B D$. |
| Beware: If 0.8 is used, but calculator is in degree mode, this can still earn M1 A1 (for the required expression), but this gives $B D=3.50 \ldots$ so the perimeter may appear as $3.5+5.6+3.5$ (earning M1 A0). |
| (d) $1^{\text {st }} \mathrm{M}$ : Use of the (correct) area formula to find $\triangle A B D$. |
| Any other methods need to be complete methods to find $\triangle A B D$. $2^{\text {nd }} \mathrm{M}$ : Subtracting their $\triangle A B D$ from their sector $A B C$. |
| Using segment formula $\frac{1}{2} r^{2}(\theta-\sin \theta)$ scores no marks in part (d). | \& \& <br>

\hline
\end{tabular}

## J une 2008 <br> Core Mathematics C2 Mark Scheme

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 8. | (a) $\left(\frac{\mathrm{d} y}{\mathrm{~d} x}=\right) 8+2 x-3 x^{2} \quad$ (M: $x^{n} \rightarrow x^{n-1}$ for one of the terms, not just $\left.10 \rightarrow 0\right)$ <br> $3 x^{2}-2 x-8=0 \quad(3 x+4)(x-2)=0 \quad x=2 \quad$ (Ignore other solution) (*) <br> (b) Area of triangle $=\frac{1}{2} \times 2 \times 22 \quad$ (M: Correct method to find area of triangle) <br> (Area $=22$ with no working is acceptable) <br> $\begin{array}{lcc}\int 10+8 x+x^{2}-x^{3} \mathrm{~d} x=10 x+\frac{8 x^{2}}{2}+\frac{x^{3}}{3}-\frac{x^{4}}{4} & \left(\mathrm{M}: x^{n} \rightarrow x^{n+1} \text { for one of the terms) }\right. \\ \begin{array}{llc}\text { Only one term correct: } & \text { M1 A0 A0 } & \text { Integrating the gradient function } \\ 2 \text { or } 3 \text { terms correct: } & \text { M1 A1 A0 } & \text { loses this M mark. } \\ \end{array}\end{array}$ $\begin{aligned} & {\left[10 x+\frac{8 x^{2}}{2}+\frac{x^{3}}{3}-\frac{x^{4}}{4}\right]_{0}^{2}=\ldots . .} \\ & \left(=20+16+\frac{8}{3}-4\right) \\ & \text { (This M can be awarded even if the other limit is wrong) } \end{aligned}$ <br> Area of $R=34 \frac{2}{3}-22=\frac{38}{3}\left(=12 \frac{2}{3}\right)($ Or 12. $\dot{6})$ <br> M: Dependent on use of calculus in (b) and correct overall 'strategy': subtract either way round. <br> A: Must be exact, not 12.67 or similar. <br> A negative area at the end, even if subsequently made positive, loses the A mark. | M1 A1 M1 A1 18 M1 A1 A1 M1 M1 A1 |
|  | (a) The final mark may also be scored by verifying that $\frac{\mathrm{d} y}{\mathrm{~d} x}=0$ at $x=2$. <br> (b) Alternative: <br> Eqn. of line $y=11 x$. <br> (Marks dependent on subsequent use in integration) <br> (M1: Correct method to find equation of line. A1: Simplified form $y=11 x$ ) $\int 10+k x+x^{2}-x^{3} \mathrm{~d} x=10 x+\frac{k x^{2}}{2}+\frac{x^{3}}{3}-\frac{x^{4}}{4} \quad(k \text { perhaps }-3)$ $\left[10 x+\frac{k x^{2}}{2}+\frac{x^{3}}{3}-\frac{x^{4}}{4}\right]_{0}^{2}=\ldots .$. <br> (Substitute limit 2 into a 'changed function') Area of $R=\left[10 x-\frac{3 x^{2}}{2}+\frac{x^{3}}{3}-\frac{x^{4}}{4}\right]_{0}^{2}=20-6+\frac{8}{3}-4=\frac{38}{3} \quad\left(=12 \frac{2}{3}\right)$ <br> Final M1 for $\int$ (curve) $-\int($ line $)$ or $\int($ line $)-\int$ (curve). | M1 A1 M1 A1 A1 M1 M1 A1 |

## J une 2008 <br> Core Mathematics C2 Mark Scheme

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 9. |  | B1 <br> M1, M1 <br> A1 <br> (4) <br> B1 <br> M1, M1 <br> M1 <br> A1 A1 |
|  | (a) Extra solution(s) in range: Loses the A mark. <br> Extra solutions outside range: Ignore (whether correct or not). <br> Common solutions: <br> 65 (only correct solution) will score B1 M0 M1 A0 (2 marks) <br> 65 and 115 will score <br> B1 M0 M1 A0 (2 marks) <br> 44.99 (or similar) for $\alpha$ is B 0 , and 64.99, 155.01 (or similar) is A 0 . <br> (b) Extra solution(s) in range: Loses the final A mark. <br> Extra solutions outside range: Ignore (whether correct or not). <br> Common solutions: <br> 40 (only correct solution) will score <br> B1 M0 M0 M1 A0 A0 (2 marks) <br> 40 and 80 (only correct solutions) <br> B1 M1 M0 M1 A0 A0 (3 marks) <br> 40 and 320 (only correct solutions) <br> B1 M0 M0 M1 A0 A0 (2 marks) <br> Answers without working: <br> Full marks can be given (in both parts), B and M marks by implication. <br> Answers given in radians: <br> Deduct a maximum of 2 marks (misread) from B and A marks. (Deduct these at first and second occurrence.) <br> Answers that begin with statements such as $\sin (x-20)=\sin x-\sin 20$ or $\cos x=-\frac{1}{6}$, then go on to find a value of ' $\alpha$ ' or ' $\beta$ ', however badly, can continue to earn the first M mark in either part, but will score no further marks. <br> Possible misread: $\cos 3 x=\frac{1}{2}$, giving 20, 100, 140, 220, 260, 340 <br> Could score up to 4 marks B0 M1 M1 M1 A0 A1 for the above answers. |  |

# Mark Scheme (Results) J anuary 2009 

## GCE

## GCE Mathematics (6664/ 01)

## J anuary 2009 6664 Core Mathematics C2 Mark Scheme

| Question Number | Scheme Marks |
| :---: | :---: |
| 1 | $\begin{aligned} & (3-2 x)^{5}=243, \quad \ldots \ldots+5 \times(3)^{4}(-2 x)=-810 x \quad \ldots \ldots \\ & +\frac{5 \times 4}{2}(3)^{3}(-2 x)^{2}=\quad+1080 x^{2} \end{aligned}$ B1, B1 |
| Notes | First term must be 243 for B1, writing just $3^{5}$ is B0 (Mark their final answers except in second line of special cases below). <br> Term must be simplified to $-810 x$ for $\mathbf{B 1}$ <br> The $x$ is required for this mark. <br> The method mark (M1) is generous and is awarded for an attempt at Binomial to get the third term. <br> There must be an $x^{2}$ (or no $x$-i.e. not wrong power) and attempt at Binomial Coefficient and at dealing with powers of 3 and 2 . The power of 3 should not be one, but the power of 2 may be one (regarded as bracketing slip). <br> So allow $\binom{5}{2}$ or $\binom{5}{3}$ or ${ }^{5} C_{2}$ or ${ }^{5} C_{3}$ or even $\left(\frac{5}{2}\right)$ or $\left(\frac{5}{3}\right)$ or use of ' 10 ' (maybe from <br> Pascal's triangle) <br> May see ${ }^{5} C_{2}(3)^{3}(-2 x)^{2}$ or ${ }^{5} C_{2}(3)^{3}\left(-2 x^{2}\right)$ or ${ }^{5} C_{2}(3)^{5}\left(-\frac{2}{3} x^{2}\right)$ or $10(3)^{3}(2 x)^{2}$ which would each score the M1 <br> A1is c.a.o and needs $1080 x^{2}$ (if $1080 x^{2}$ is written with no working this is awarded both marks i.e. M1 A1.) |
| Special cases | $243+810 x+1080 x^{2}$ is B1B0M1A1 (condone no negative signs) <br> Follows correct answer with $27-90 x+120 x^{2}$ can isw here (sp case)- full marks for correct answer <br> Misreads ascending and gives $-32 x^{5}+240 x^{4}-720 x^{3}$ is marked as B1B0M1A0 special case and must be completely correct. (If any slips could get B0B0M1A0) Ignores 3 and expands $(1 \pm 2 x)^{5}$ is $\mathbf{0} / 4$ 243, $-810 x, 1080 x^{2}$ is full marks but 243, $-810,1080$ is B1,B0,M1,A0 NB Alternative method $3^{5}\left(1-\frac{2}{3} x\right)^{5}=3^{5}-5 \times 3^{5} \times\left(\frac{2}{3} x\right)+\binom{5}{3} 3^{5}\left(-\frac{2}{3} x\right)^{2}+.$. is B0B0M1A0 - answers must be simplified to $243-810 x+1080 x^{2}$ for full marks (awarded as before) Special case $3\left(1-\frac{2}{3} x\right)^{5}=3-5 \times 3 \times\left(\frac{2}{3} x\right)+\binom{5}{3} 3\left(-\frac{2}{3} x\right)^{2}+.$. is B0, B0, M1, A0 Or $\quad 3(1-2 x)^{5}$ is B0B0M0A0 |


| Question <br> Number | Scheme Marks |
| :---: | :---: |
| 2 | $y=(1+x)(4-x)=4+3 x-x^{2}$ M: Expand, giving 3 (or 4) terms M1 <br> $\int\left(4+3 x-x^{2}\right) \mathrm{d} x=4 x+\frac{3 x^{2}}{2}-\frac{x^{3}}{3}$ M: Attempt to integrate M1 A1 <br> $=[\ldots \ldots \ldots \ldots \ldots .]_{-1}^{4}=\left(16+24-\frac{64}{3}\right)-\left(-4+\frac{3}{2}+\frac{1}{3}\right)=\frac{125}{6} \quad\left(=20 \frac{5}{6}\right)$ M1 A1 (5) <br>    |
| Notes | M1 needs expansion, there may be a slip involving a sign or simple arithmetical error e.g. $1 \times 4=5$, but there needs to be a 'constant' an ' $x$ term' and an ' $x^{2}$ term'. The $x$ terms do not need to be collected. (Need not be seen if next line correct) <br> Attempt to integrate means that $x^{n} \rightarrow x^{n+1}$ for at least one of the terms, then M1 is awarded ( even 4 becoming $4 x$ is sufficient) - one correct power sufficient. <br> A1 is for correct answer only, not follow through. But allow $2 x^{2}-\frac{1}{2} x^{2}$ or any correct equivalent. Allow $+\boldsymbol{c}$, and even allow an evaluated extra constant term. <br> M1: Substitute limit 4 and limit -1 into a changed function (must be -1 ) and indicate subtraction (either way round). <br> A1 must be exact, not 20.83 or similar. If recurring indicated can have the mark. Negative area, even if subsequently positive loses the A mark. |
| Special cases | (i) Uses calculator method: M1 for expansion (if seen) M1 for limits if answer correct, so 0,1 or 2 marks out of 5 is possible (Most likely M0 M0 A0 M1 A0 ) <br> (ii) Uses trapezium rule : not exact, no calculus - 0/5 unless expansion mark M1 gained. <br> (iii) Using original method, but then change all signs after expansion is likely to lead to: <br> M1 M1 A0, M1 A0 i.e. 3/5 |


| Question Number | Scheme Marks |
| :---: | :---: |
| (a) <br> (b) |  |
| (a) <br> (b) | B1 for one answer correct Second $\mathbf{B 1}$ for all three correct <br> Accept awrt ones given or exact answers so $\sqrt{21}, \sqrt{\left(\frac{369}{25}\right)}$ or $\frac{3 \sqrt{41}}{5}$, and $\sqrt{\left(\frac{429}{25}\right)}$ or <br> $\frac{\sqrt{429}}{5}$, score the marks. <br> B1 is for using 0.2 or $\frac{0.4}{2}$ as $\frac{1}{2} h$. <br> M1 requires first bracket to contain first plus last values and second bracket to include no additional values from those in the table. <br> If the only mistake is to omit one value from $2^{\text {nd }}$ bracket this may be regarded as a slip ar can be allowed ( An extra repeated term forfeits the $\mathbf{M}$ mark however) <br> $x$ values: M0 if values used in brackets are $x$ values instead of $y$ values. <br> Separate trapezia may be used : B1 for 0.2, M1 for $\frac{1}{2} h(a+b)$ used 4 or 5 times ( and A1ft all <br> e.g.. $0.2(3+3.47)+0.2(3.47+3.84)+0.2(3.84+4.14)+0.2(4.14+4.58)$ is M1 A0 <br> equivalent to missing one term in $\}$ in main scheme <br> A1ft follows their answers to part (a) and is for \{correct expression\} <br> Final A1 must be correct. (No follow through) <br> Bracketing mistake: i.e. $\frac{1}{2} \times 0.4(3+4.58)+2(3.47+3.84+4.14+4.39)$ <br> scores B1 M1 A0 A0 unless the final answer implies that the calculation has been done correctly (then full marks can be given). <br> Need to see trapezium rule - answer only (with no working) is 0/4. |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 4 | $\begin{array}{lc} 2 \log _{5} x=\log _{5}\left(x^{2}\right), & \log _{5}(4-x)-\log _{5}\left(x^{2}\right)=\log _{5} \frac{4-x}{x^{2}} \\ \log \left(\frac{4-x}{x^{2}}\right)=\log 5 & 5 x^{2}+x-4=0 \text { or } 5 x^{2}+x=4 \text { o.e. } \\ (5 x-4)(x+1)=0 & x=\frac{4}{5} \end{array} \quad(x=-1) \quad .$ | B1, M1 <br> M1 A1 <br> dM1 A1 <br> (6) <br> [6] |
| Notes | $\mathbf{B} 1$ is awarded for $2 \log x=\log x^{2}$ anywhere. <br> M1 for correct use of $\log A-\log B=\log \frac{A}{B}$ <br> M1 for replacing 1 by $\log _{k} k$. A1 for correct quadratic <br> $\left(\log (4-x)-\log x^{2}=\log 5 \Rightarrow 4-x-x^{2}=5\right.$ is B1M0M1A0 M0A0) <br> dM1 for attempt to solve quadratic with usual conventions. (Only award if previous two M marks have been awarded) <br> A1 for $4 / 5$ or 0.8 or equivalent (Ignore extra answer). |  |
| Alternative 1 | $\begin{aligned} & \log _{5}(4-x)-1=2 \log _{5} x \text { so } \log _{5}(4-x)-\log _{5} 5=2 \log _{5} x \\ & \log _{5} \frac{4-x}{5}=2 \log _{5} x \end{aligned}$ <br> then could complete solution with $2 \log _{5} x=\log _{5}\left(x^{2}\right)$ $\left(\frac{4-x}{5}\right)=x^{2} \quad 5 x^{2}+x-4=0$ <br> Then as in first method $(5 x-4)(x+1)=0 \quad x=\frac{4}{5} \quad(x=-1)$ | M1 <br> M1 <br> B1 <br> A1 <br> dM1 A1 <br> (6) <br> [6] |
| Special cases | Complete trial and error yielding 0.8 is M3 and $\mathbf{B 1}$ for 0.8 A1, A1 awarded for each of two tries evaluated. i.e. 6/6 Incomplete trial and error with wrong or no solution is $0 / 6$ Just answer 0.8 with no working is B1 |  |



| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Further alternatives | (i) A number of methods find gradient of $\mathrm{PQ}=2 / 3$ then give perpendicular gradient is $-3 / 2$ This is M1 <br> They then proceed using equations of lines through point $Q$ or by using gradient $Q R$ to obtain equation such as $\frac{4-10}{a-9}=-\frac{3}{2} \mathbf{M 1}$ (may still have $x$ in this equation rather than $a$ and there may be a small slip) <br> They then complete to give ( $a$ )=13 A1 <br> (ii) A long involved method has been seen finding the coordinates of the centre of the circle first. <br> This can be done by a variety of methods Giving centre as (c, 3) and using an equation such as $(c-9)^{2}+7^{2}=(c+3)^{2}+1^{2}$ (equal radii) or $\frac{3-6}{c-3}=-\frac{3}{2} \mathbf{M 1}$ (perpendicular from centre to chord bisects chord) <br> Then using $c(=5)$ to find $a$ is M1 <br> Finally $a=13$ A1 <br> (iii) Vector Method: <br> States $\mathbf{P Q} . \mathbf{Q R}=0$, with vectors stated $12 \mathrm{i}+8 \mathrm{j}$ and $(9-a) \mathbf{i}+\mathbf{6 j}$ is $\mathbf{M 1}$ Evaluates scalar product so $108-12 a+48=0$ (M1) solves to give $a=13$ (A1) | M1 <br> M1 <br> A1 <br> M1 <br> M1 <br> A1 <br> M1 <br> M1 <br> A1 |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 6 (a) | $f(2)=16+40+2 a+b \text { or } f(-1)=1-5-a+b$ <br> Finds 2nd remainder and equates to 1 st $\Rightarrow 16+40+2 a+b=1-5-a+b$ $\begin{align*} & a=-20  \tag{5}\\ & \mathrm{f}(-3)=(-3)^{4}+5(-3)^{3}-3 a+b=0 \\ & 81-135+60+b=0 \text { gives } b=-6 \end{align*}$ | M1 A1 <br> M1 A1 <br> Alcso <br> M1 Alft <br> A1 cso <br> (3) |
| Alternative for (a) <br> Alternative for (b) | (a) Uses long division, to get remainders as $b+2 a+56$ or $b-a-4$ or correct equivalent <br> Uses second long division as far as remainder term, to get $b+2 a+56=b-a-4$ or correct equivalent $a=-20$ <br> (b) Uses long division of $x^{4}+5 x^{3}-20 x+b$ by $(x+3)$ to obtain $x^{3}+2 x^{2}-6 x+a+18$ ( with their value for $a$ ) <br> Giving remainder $b+6=0$ and so $b=-6$ | M1 A1 <br> M1 A1 <br> Alcso <br> (5) <br> M1 A1ft <br> A1 cso |
| $\begin{array}{rr}\text { Notes } & \text { (a) } \\ & \\ & \text { (b) }\end{array}$ | M1 : Attempts $f( \pm 2)$ or $f( \pm 1)$ <br> A1 is for the answer shown (or simplified with terms collected ) for one remainder <br> M1: Attempts other remainder and puts one equal to the other <br> A1: for correct equation in $a$ (and $b$ ) then A1 for $a=-20$ cso <br> M1: Puts $\mathrm{f}( \pm 3)=0$ <br> A1 is for $f(-3)=0$, (where f is original function), with no sign or substitution errors (follow through on ' $a$ ' and could still be in terms of $a$ ) <br> A1: $b=-6$ is cso. |  |
| Alternatives | (a) M1: Uses long division of $x^{4}+5 x^{3}+a x+b$ by $(x \pm 2)$ or by $(x \pm 1)$ as far as three term quotient <br> A1: Obtains at least one correct remainder <br> M1: Obtains second remainder and puts two remainders (no $x$ terms) equal <br> A1: correct equation A1: correct answer $a=-20$ following correct work. <br> (b) M1: complete long division as far as constant (ignore remainder) <br> A1ft: needs correct answer for their $a$ <br> A1: correct answer |  |
| Beware: It is possible to get correct answers with wrong working. If remainders are equated to 0 in part (a) both correct answers are obtained fortuitously. This could score M1A1M0A0A0M1A1A0 |  |  |


| Question <br> Number | Scheme Marks |
| :---: | :---: |
| 7 (a) <br> (b) | $\frac{1}{2} r^{2} \theta=\frac{1}{2} \times 6^{2} \times 2.2=39.6 \quad\left(\mathrm{~cm}^{2}\right)$ M1 A1 (2)  <br> $\left(\frac{2 \pi-2.2}{2}=\right) \pi-1.1=2.04 \quad(\mathrm{rad})$ M1 A1 (2)  <br> (c) $\triangle D A C=\frac{1}{2} \times 6 \times 4 \sin 2.04 \quad(\approx 10.7)$    <br> Total area $=$ sector +2 triangles $=61$ $\left(\mathrm{~cm}^{2}\right)$ M1 A1ft  <br>   M1 A1 (4) <br>    [8] |
| (a) <br> (b) <br> (c) | M1: Needs $\theta$ in radians for this formula. Could convert to degrees and use degrees formula. <br> A1: Does not need units. Answer should be 39.6 exactly. Answer with no working is M1 A1. <br> This M1A1 can only be awarded in part (a). <br> M1: Needs full method to give angle in radians <br> A1: Allow answers which round to 2.04 (Just writes 2.04 - no working is 2/2) <br> M1: Use $\frac{1}{2} \times 6 \times 4 \sin A$ (if any other triangle formula e.g. $\frac{1}{2} b \times h$ is used the method must be complete for this mark) (No value needed for $A$, but should not be using 2.2) <br> A1: ft the value obtained in part (b) - need not be evaluated- could be in degrees <br> M1: Uses Total area $=$ sector +2 triangles or other complete method <br> A1: Allow answers which round to 61. (Do not need units) <br> Special case degrees: Could get M0A0, M0A0, M1A1M1A0 <br> Special case: Use $\triangle B D C-\triangle B A C$ Both areas needed for first M1 <br> Total area $=$ sector + area found is second $\mathbf{M 1}$ <br> NB Just finding lengths $\mathrm{BD}, \mathrm{DC}$, and angle BDC then assuming area BDC is a sector to find area $\operatorname{BDC}$ is $0 / 4$ |


| Question Number | Scheme Marks |
| :---: | :---: |
| 8 <br> (a) <br> (b) |  |
| (a) <br> (b) | M1: Uses $\sin ^{2} x=1-\cos ^{2} x$ (may omit bracket) not $\sin ^{2} x=\cos ^{2} x-1$ <br> A1: Obtains the printed answer without error - must have $=\mathbf{0}$ <br> M1: Solves the quadratic with usual conventions <br> A1: Obtains $1 / 4$ accurately- ignore extra answer 2 but penalise e.g. -2 . <br> B1: allow answers which round to 75.5 <br> M1: $360-\alpha \mathrm{ft}$ their value, M1: $360+\alpha \mathrm{ft}$ their value or $720-\alpha \mathrm{ft}$ <br> A1: Three and only three correct exact answers in the range achieves the mark |
| Special cases | In part (b) Error in solving quadratic (4cosx-1)( $\cos x+2)$ <br> Could yield, M1A0B1M1M1A1 losing one mark for the error <br> Works in radians: <br> Complete work in radians :Obtains 1.3 B0. Then allow M1 M1 for $2 \pi-\alpha, 2 \pi+\alpha$ or $4 \pi-\alpha$ Then gets $5.0,7.6,11.3$ A0 so $2 / 4$ <br> Mixed answer 1.3, $360-1.3,360+1.3,720-1.3$ still gets B0M1M1A0 |


| Question Number | Scheme Marks |
| :---: | :---: |
| (b) <br> (c) <br> (d) | Initial step: Two of: $a=k+4$, $a r=k, a r^{2}=2 k-15$ <br> Or one of: $r=\frac{k}{k+4}, \quad r=\frac{2 k-15}{k}, \quad r^{2}=\frac{2 k-15}{k+4}$, <br> Or $k=\sqrt{(k+4)(2 k-15)}$ or even $k^{3}=(k+4) k(2 k-15)$ $\begin{equation*} k^{2}=(k+4)(2 k-15), \text { so } k^{2}=2 k^{2}+8 k-15 k-60 \tag{} \end{equation*}$ <br> M1, A1 <br> Proceed to $k^{2}-7 k-60=0$ <br> A1 $\begin{equation*} (k-12)(k+5)=0 \quad k=12 \tag{*} \end{equation*}$ <br> Common ratio: $\frac{k}{k+4}$ or $\frac{2 k-15}{k}=\frac{12}{16}\left(=\frac{3}{4}\right.$ or 0.75$)$ $\frac{a}{1-r}=\frac{16}{(1 / 4)}=64$ |
| (a) (b) (c) (d) | M1: The 'initial step', scoring the first M mark, may be implied by next line of proof <br> M1: Eliminates $a$ and $r$ to give valid equation in $k$ only. Can be awarded for equation involving fractions. <br> A1 : need some correct expansion and working and answer equivalent to required quadratic but with uncollected terms. Equations involving fractions do not get this mark. (No fractions, no brackets - could be a cubic equation) <br> A1: as answer is printed this mark is for cso (Needs $=0$ ) <br> All four marks must be scored in part (a) <br> M1: Attempt to solve quadratic <br> A1: This is for correct factorisation or solution and $k=12$. Ignore the extra solution ( $k=$ -5 or even $k=5$ ), if seen. <br> Substitute and verify is M1 A0 <br> Marks must be scored in part (b) <br> M1: Complete method to find $r$ Could have answer in terms of $k$ <br> A1: 0.75 or any correct equivalent <br> Both Marks must be scored in (c) <br> M1: Tries to use $\frac{a}{1-r}$, (even with $r>1$ ). Could have an answer still in terms of $k$. <br> A1: This answer is 64 cao. |


| Question <br> Number | Scheme ${ }^{\text {S }}$ Marks |
| :---: | :---: |
| (a) <br> (b) <br> (c) |  |
| Other methods for part (c): | Either:M: Find value of $\frac{\mathrm{d} V}{\mathrm{~d} r}$ on each side of " $r=\sqrt{\frac{400}{3 \pi}}$ " and consider sign. <br> A: Indicate sign change of positive to negative for $\frac{\mathrm{d} V}{\mathrm{~d} r}$, and conclude max. <br> Or: M: Find value of $V$ on each side of " $r=\sqrt{\frac{400}{3 \pi}}$ " and compare with " 1737 ". <br> A: Indicate that both values are less than 1737 or 1737.25 , and conclude max. |
| Notes <br> (a) <br> (b) | B1: For any correct form of this equation (may be unsimplified, may be implied by $1^{\text {st }}$ M1) <br> M1 : Making $h$ the subject of their three or four term formula <br> M1: Substituting expression for $h$ into $\pi r^{2} h$ (independent mark) Must now be expression in $r$ only. <br> A1: cso <br> M1: At least one power of $r$ decreased by 1 A1: cao <br> M1: Setting $\frac{\mathrm{d} V}{\mathrm{~d} r}=0$ and finding a value for correct power of $r$ for candidate <br> A1 : This mark may be credited if the value of $V$ is correct. Otherwise answers should round to 6.5 (allow <br> $\pm 6.5$ ) or be exact answer <br> M1: Substitute a positive value of $r$ to give $V$ A1: 1737 or $1737.25 \ldots .$. or exact answer |

(c)

M1: needs complete method e.g.attempts differentiation (power reduced) of their first derivative and
considers its sign
A1(first method) should be $-6 \pi r$ (do not need to substitute $r$ and can condone wrong $r$ if found in (b))

Need to conclude maximum or indicate by a tick that it is maximum.
Throughout allow confused notation such as $\mathrm{d} y / \mathrm{d} x$ for $\mathrm{d} V / \mathrm{d} r$
Alternative
for (a)
$A=2 \pi r^{2}+2 \pi r h, \frac{A}{2} \times r=\pi r^{3}+\pi r^{2} h$ is M1 Equate to $400 r$ B1
Then $V=400 r-\pi r^{3}$ is M1 A1

## J une 2009

## 6664 Core Mathematics C2

Mark Scheme

| Question Number | Scheme ${ }^{\text {S }}$ |
| :---: | :---: |
| Q1 | $\begin{align*} & \int\left(2 x+3 x^{\frac{1}{2}}\right) \mathrm{d} x=\frac{2 x^{2}}{2}+\frac{3 x^{\frac{3}{2}}}{\frac{3}{2}} \\ & \begin{aligned} \int_{1}^{4}\left(2 x+3 x^{\frac{1}{2}}\right) \mathrm{d} x & =\left[x^{2}+2 x^{\frac{3}{2}}\right]_{1}^{4}=(16+2 \times 8)-(1+2) \\ & =29 \end{aligned} \end{align*}$ |
|  | $1^{\text {st }}$ M1 for attempt to integrate $x \rightarrow k x^{2}$ or $x^{\frac{1}{2}} \rightarrow k x^{\frac{3}{2}}$. <br> $1^{\text {st }} \mathrm{A} 1$ for $\frac{2 x^{2}}{2}$ or a simplified version. <br> $2^{\text {nd }}$ A1 for $\frac{3 x^{\frac{3}{2}}}{(3 / 2)}$ or $\frac{3 x \sqrt{x}}{(3 / 2)}$ or a simplified version. <br> Ignore $+C$, if seen, but two correct terms and an extra non-constant term scores M1A1A0. <br> $2^{\text {nd }}$ M1 for correct use of correct limits ('top' - 'bottom'). Must be used in a 'changed function', not just the original. (The changed function may have been found by differentiation). <br> Ignore 'poor notation' (e.g. missing integral signs) if the intention is clear. <br> No working: <br> The answer 29 with no working scores M0A0A0M1A0 (1 mark). |


| Question Number | Scheme Marks |
| :---: | :---: |
| (a) <br> (b) | $(7 \times \ldots \times x)$ or $\left(21 \times \ldots \times x^{2}\right)$ The 7 or 21 can be in 'unsimplified' form. $\begin{aligned} (2+k x)^{7} & =2^{7}+2^{6} \times 7 \times k x+2^{5} \times\binom{ 7}{2} k^{2} x^{2} \\ & =128 ; \quad+448 k x, \quad+672 k^{2} x^{2}\left[\text { or } 672(k x)^{2}\right] \end{aligned}$ <br> (If $672 k x^{2}$ follows $672(k x)^{2}$, isw and allow A1) $\begin{aligned} 6 \times 448 k & =672 k^{2} \\ k & =4 \end{aligned}$ <br> (Ignore $k=0$, if seen) |
| (a) | The terms can be 'listed' rather than added. Ignore any extra terms. <br> M1 for either the $x$ term or the $x^{2}$ term. Requires correct binomial coefficient in any form with the correct power of $x$, but the other part of the coefficient (perhaps including powers of 2 and/or $k$ ) may be wrong or missing. <br> Allow binomial coefficients such as $\binom{7}{1},\binom{7}{1},\binom{7}{2},{ }^{7} C_{1},{ }^{7} C_{2}$. <br> However, $448+k x$ or similar is M0. <br> B1, A1, A1 for the simplified versions seen above. <br> Alternative: <br> Note that a factor $2^{7}$ can be taken out first: $2^{7}\left(1+\frac{k x}{2}\right)^{7}$, but the mark scheme still applies. <br> Ignoring subsequent working (isw): <br> Isw if necessary after correct working: <br> e.g. $128+448 k x+672 k^{2} x^{2} \quad$ M1 B1 A1 A1 <br> $=4+14 k x+21 k^{2} x^{2} \quad$ isw <br> (Full marks are still available in part (b)). <br> M1 for equating their coefficient of $x^{2}$ to 6 times that of $x \ldots$ to get an equation in $k$, $\ldots$ or equating their coefficient of $x$ to 6 times that of $x^{2}$, to get an equation in $k$. <br> Allow this M mark even if the equation is trivial, providing their coefficients from part (a) have been used, e.g. $6 \times 448 k=672 k$, but beware $k=4$ following from this, which is A0. <br> An equation in $k$ alone is required for this M mark, so... <br> e.g. $6 \times 448 k x=672 k^{2} x^{2} \Rightarrow k=4$ or similar is M0 A0 (equation in coefficients only is never seen), but ... <br> e.g. $6 \times 448 k x=672 k^{2} x^{2} \Rightarrow 6 \times 448 k=672 k^{2} \Rightarrow k=4$ will get M1 A1 <br> (as coefficients rather than terms have now been considered). <br> The mistake $2\left(1+\frac{k x}{2}\right)^{7}$ would give a maximum of 3 marks: M1B0A0A0, M1A1 |



| Question Number | Scheme Marks |
| :---: | :---: |
| Q4 (a) <br> (b) <br> (c) |  |
| (b) | B1 for $\frac{1}{2} \times \frac{1}{2}$ or equivalent. <br> For the M mark, the first bracket must contain the 'first and last' values, and the second bracket (which must be multiplied by 2 ) must have no additional values. If the only mistake is to omit one of the values from the second bracket, this can be considered as a slip and the M mark can be allowed. <br> Bracketing mistake: i.e. $\left(\frac{1}{2} \times \frac{1}{2}\right)(1.414+3)+2(1.554+1.732+1.957+2.236+2.580)$ <br> scores B1 M1 A0 A0 unless the final answer implies that the calculation has been done correctly (then full marks can be given). <br> Alternative: <br> Separate trapezia may be used, and this can be marked equivalently. $\left[\frac{1}{4}(1.414+1.554)+\frac{1}{4}(1.554+1.732)+\ldots \ldots . . . . . . . . . . .+\frac{1}{4}(2.580+3)\right]$ <br> $1^{\text {st }} \mathrm{A} 1 \mathrm{ft}$ for correct expression, ft their 2.236 and their 2.580 <br> $1^{\text {st }} \mathrm{B} 1$ for 'overestimate', ignoring earlier mistakes and ignoring any reasons given. <br> $2^{\text {nd }} \mathrm{B} 1$ is dependent upon the $1^{\text {st }} \mathrm{B} 1$ (overestimate). |


| Question Number | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| Q5 (a) | $324 r^{3}=96 \quad$ or $\quad r^{3}=\frac{96}{324} \quad$ or $\quad r^{3}=\frac{8}{27}$ |  | M1 |
|  | $r=\frac{2}{3}$ | (*) | Alcso (2) |
| (b) | $a\left(\frac{2}{3}\right)^{2}=324 \quad \text { or } \quad a\left(\frac{2}{3}\right)^{5}=96 \quad a=\ldots,$ | 729 | M1, A1 (2) |
| (c) | $\mathrm{S}_{15}=\frac{729\left(1-\left[\frac{2}{3}\right]^{15}\right)}{1-\frac{2}{3}},=2182.00 \ldots$ | (AWRT 2180) | M1A1ft, (3) |
| (d) | $\mathrm{S}_{\infty}=\frac{729}{1-\frac{2}{3}}, \quad=2187$ |  | $\begin{array}{ll} \mathrm{M} 1, \mathrm{Al} & (2) \\ & {[9]} \end{array}$ |

(a) M1 for forming an equation for $r^{3}$ based on 96 and 324 (e.g. $96 r^{3}=324$ scores M1). The equation must involve multiplication/division rather than addition/subtraction.
A1 Do not penalise solutions with working in decimals, providing these are correctly rounded or truncated to at least 2 dp and the final answer $2 / 3$ is seen.
Alternative: (verification)
M1 Using $r^{3}=\frac{8}{27}$ and multiplying 324 by this (or multiplying by $r=\frac{2}{3}$ three times).
A1 Obtaining 96 (cso). (A conclusion is not required).
$324 \times\left(\frac{2}{3}\right)^{3}=96$ (no real evidence of calculation) is not quite enough and scores M1 A0.
(b)

M1 for the use of a correct formula or for 'working back' by dividing by $\frac{2}{3}$ (or by their $r$ ) twice from 324 (or 5 times from 96).
Exceptionally, allow M1 also for using $a r^{3}=324$ or $a r^{6}=96$ instead of $a r^{2}=324$ or $a r^{5}=96$, or for dividing by $r$ three times from 324 (or 6 times from 96)... but no other exceptions are allowed.
(c)

M1 for use of sum to 15 terms formula with values of $a$ and $r$. If the wrong power is used, e.g. 14, the M mark is scored only if the correct sum formula is stated.
$1^{\text {st }}$ A1ft for a correct expression or correct ft their $a$ with $r=\frac{2}{3}$.
$2^{\text {nd }}$ A1 for awrt 2180, even following 'minor inaccuracies'.
Condone missing brackets round the $\frac{2}{3}$ for the marks in part (c).
Alternative:
M1 for adding 15 terms and $1^{\text {st }}$ A1ft for adding the 15 terms that ft from their $a$ and $r=\frac{2}{3}$.
(d) M1 for use of correct sum to infinity formula with their $a$. For this mark, if a value of $r$ different from the given value is being used, M1 can still be allowed providing $|r|<1$.

| Question Number | Scheme Marks |
| :---: | :---: |
| (a) <br> (b) <br> (c) |  |
| (a) | $1^{\text {st }} \mathrm{M} 1$ for attempt to complete square. Allow $(x \pm 3)^{2} \pm k$, or $(y \pm 2)^{2} \pm k, k \neq 0$. <br> $1^{\text {st }}$ A1 $x$-coordinate 3, $2^{\text {nd }}$ A1 $y$-coordinate -2 <br> $2^{\text {nd }}$ M1 for a full method leading to $r=\ldots$, with their 9 and their 4, $3^{\text {rd }}$ A1 5 or $\sqrt{25}$ <br> The $1^{\text {st }} \mathrm{M}$ can be implied by $( \pm 3, \pm 2)$ but a full method must be seen for the $2^{\text {nd }} \mathrm{M}$. <br> Where the 'diameter' in part (b) has clearly been used to answer part (a), no marks in (a), but in this case the M1 (not the A1) for part (b) can be given for work seen in (a). <br> Alternative <br> $1^{\text {st }} \mathrm{M} 1$ for comparing with $x^{2}+y^{2}+2 g x+2 f y+c=0$ to write down centre $(-g,-f)$ directly. Condone sign errors for this M mark. <br> $2^{\text {nd }}$ M1 for using $r=\sqrt{g^{2}+f^{2}-c}$. Condone sign errors for this M mark. <br> $1^{\text {st }} \mathrm{M} 1$ for setting $x=0$ and getting a 3TQ in $y$ by using eqn. of circle. <br> $2^{\text {nd }} \mathrm{M} 1$ (dep.) for attempt to solve a 3 TQ leading to at least one solution for $y$. <br> Alternative 1: (Requires the B mark as in the main scheme) <br> $1^{\text {st }} \mathrm{M}$ for using $(3,4,5)$ triangle with vertices $(3,-2),(0,-2),(0, y)$ to get a linear or <br> quadratic equation in $y\left(\right.$ e.g. $\left.3^{2}+(y+2)^{2}=25\right)$. <br> $2^{\text {nd }} \mathrm{M}$ (dep.) as in main scheme, but may be scored by simply solving a linear equation. <br> Alternative 2: (Not requiring realisation that $R$ is on the circle) <br> B1 for attempt at $m_{P R} \times m_{Q R}=-1$, (NOT $m_{P Q}$ ) or for attempt at Pythag. in triangle $P Q R$. <br> $1^{\text {st }}$ M1 for setting $x=0$, i.e. $(0, y)$, and proceeding to get a 3TQ in $y$. Then main scheme. <br> Alternative 2 by 'verification': <br> B1 for attempt at $m_{P R} \times m_{Q R}=-1$, (NOT $m_{P Q}$ ) or for attempt at Pythag. in triangle $P Q R$. <br> $1^{\text {st }}$ M1 for trying ( 0,2 ). <br> $2^{\text {nd }} \mathrm{M} 1$ (dep.) for performing all required calculations. <br> A1 for fully correct working and conclusion. |


| Question Number | Scheme Marks |
| :---: | :---: |
| Q7 <br> (i) <br> (ii) |  |
| (i) | $1^{\text {st }} \mathrm{B} 1$ for -45 seen $\quad(\alpha$, where $\|\alpha\|<90)$ <br> $2^{\text {nd }} \mathrm{B} 1$ for 135 seen, or $\mathrm{ft}(180+\alpha)$ if $\alpha$ is negative, or $(\alpha-180)$ if $\alpha$ is positive. <br> If $\tan \theta=k$ is obtained from wrong working, $2^{\text {nd }} \mathrm{B} 1 \mathrm{ft}$ is still available. <br> $3^{\text {rd }} \mathrm{B} 1$ for awrt $24 \quad(\beta$, where $\|\beta\|<90)$ <br> $4^{\text {th }} \mathrm{B} 1$ for awrt 156 , or $\mathrm{ft}(180-\beta)$ if $\beta$ is positive, or $-(180+\beta)$ if $\beta$ is negative. <br> If $\sin \theta=k$ is obtained from wrong working, $4^{\text {th }} \mathrm{B} 1 \mathrm{ft}$ is still available. <br> $1^{\text {st }}$ M1 for use of $\tan x=\frac{\sin x}{\cos x}$. Condone $\frac{3 \sin x}{3 \cos x}$. <br> $2^{\text {nd }} \mathrm{M} 1$ for correct work leading to 2 factors (may be implied). <br> $1^{\text {st }}$ B1 for $0,2^{\text {nd }}$ B1 for 180 . <br> $3^{\text {rd }} \mathrm{B} 1$ for awrt $41 \quad(\gamma$, where $\|\gamma\|<180)$ <br> $4^{\text {th }}$ B1 for awrt 319, or ft $(360-\gamma)$. <br> If $\cos \theta=k$ is obtained from wrong working, $4^{\text {th }} \mathrm{B} 1 \mathrm{ft}$ is still available. <br> N.B. Losing $\sin x=0$ usually gives a maximum of 3 marks M1M0B0B0B1B1 <br> Alternative: (squaring both sides) <br> $1^{\text {st }} \mathrm{M} 1$ for squaring both sides and using a 'quadratic' identity. <br> e.g. $16 \sin ^{2} \theta=9\left(\sec ^{2} \theta-1\right)$ <br> $2^{\text {nd }} \mathrm{M} 1$ for reaching a factorised form. <br> e.g. $\left(16 \cos ^{2} \theta-9\right)\left(\cos ^{2} \theta-1\right)=0$ <br> Then marks are equivalent to the main scheme. Extra solutions, if not rejected, are penalised as in the main scheme. <br> For both parts of the question: <br> Extra solutions outside required range: Ignore <br> Extra solutions inside required range: <br> For each pair of B marks, the $2^{\text {nd }} \mathrm{B}$ mark is lost if there are two correct values and one or more extra solution(s), e.g. $\tan \theta=-1 \Rightarrow \theta=45,-45,135$ is B 1 B 0 <br> Answers in radians: <br> Loses a maximum of 2 B marks in the whole question (to be deducted at the first and second occurrence). |

\begin{tabular}{|c|c|}
\hline Question Number \& Scheme Marks \\
\hline (b) \& \begin{tabular}{l}
\[
\begin{equation*}
\log _{2} y=-3 \Rightarrow y=2^{-3} \tag{a}
\end{equation*}
\]
\[
y=\frac{1}{8} \quad \text { or } \quad 0.125
\] \\
\(32=2^{5}\) or \(16=2^{4}\) or \(512=2^{9}\) \\
[or \(\log _{2} 32=5 \log _{2} 2 \quad\) or \(\quad \log _{2} 16=4 \log _{2} 2\) or \(\left.\quad \log _{2} 512=9 \log _{2} 2\right]\) \\
[or \(\log _{2} 32=\frac{\log _{10} 32}{\log _{10} 2}\) or \(\log _{2} 16=\frac{\log _{10} 16}{\log _{10} 2}\) or \(\log _{2} 512=\frac{\log _{10} 512}{\log _{10} 2}\) ]
\[
\log _{2} 32+\log _{2} 16=9
\] \\
\((\log x)^{2}=\ldots \quad\) or \(\quad(\log x)(\log x)=\ldots \quad(\) May not be seen explicitly, so \\
M1 may be implied by later work, and the base may be 10 rather than 2)
\[
\begin{aligned}
\& \log _{2} x=3 \Rightarrow x=2^{3}=8 \\
\& \log _{2} x=-3 \Rightarrow x=2^{-3}=\frac{1}{8}
\end{aligned}
\]
\end{tabular} \\
\hline (a)

(b) \& | M1 for getting out of logs correctly. |
| :--- |
| If done by change of base, $\log _{10} y=-0.903 \ldots$ is insufficient for the M 1 , but $y=10^{-0.903}$ scores M1. |
| A1 for the exact answer, e.g. $\log _{10} y=-0.903 \Rightarrow y=0.12502 .$. scores M1 (implied) A0. |
| Correct answer with no working scores both marks. |
| Allow both marks for implicit statements such as $\log _{2} 0.125=-3$. |
| $1^{\text {st }}$ M1 for expressing 32 or 16 or 512 as a power of 2 , or for a change of base enabling evaluation of $\log _{2} 32, \log _{2} 16$ or $\log _{2} 512$ by calculator. (Can be implied by 5,4 or 9 respectively). |
| $1^{\text {st }} \mathrm{A} 1$ for 9 (exact). |
| $2^{\text {nd }}$ M1 for getting $\left(\log _{2} x\right)^{2}=$ constant. The constant can be a log or a sum of logs. |
| If written as $\log _{2} x^{2}$ instead of $\left(\log _{2} x\right)^{2}$, allow the $M$ mark only if subsequent work implies correct interpretation. |
| $2^{\text {nd }}$ A1 for 8 (exact). Change of base methods leading to a non-exact answer score A0. $3^{\text {rd }}$ A1ft for an answer of $\frac{1}{\text { their } 8}$. An ft answer may be non-exact. |
| Possible mistakes: |
| $\log _{2}\left(2^{9}\right)=\log _{2}\left(x^{2}\right) \Rightarrow x^{2}=2^{9} \Rightarrow x=\ldots$ scores M1A1(implied by 9)M0A0A0 |
| $\log _{2} 512=\log _{2} x \times \log _{2} x \Rightarrow x^{2}=512 \Rightarrow x=\ldots$ scores M0A0(9 never seen)M1A0A0 |
| $\log _{2} 48=\left(\log _{2} x\right)^{2} \Rightarrow\left(\log _{2} x\right)^{2}=5.585 \Rightarrow x=5.145, x=0.194$ scores M0A0M1A0A1ft |
| No working (or 'trial and improvement'): |
| $x=8$ scores M0 A0 M1 A1 A0 | <br>

\hline
\end{tabular}

\begin{tabular}{|c|c|}
\hline Question Number \& Scheme Marks \\
\hline Q9 (a) \& \begin{tabular}{l}
(Arc length =) \(r \theta=r \times 1=r\). Can be awarded by implication from later work, e.g. \\
3rh or \((2 r h+r h)\) in the \(S\) formula. (Requires use of \(\theta=1\) ). \\
(Sector area \(=\) ) \(\frac{1}{2} r^{2} \theta=\frac{1}{2} r^{2} \times 1=\frac{r^{2}}{2}\). Can be awarded by implication from later \\
work, e.g. the correct volume formula. (Requires use of \(\theta=1\) ). \\
Surface area \(=2\) sectors +2 rectangles + curved face \\
( \(\left.=r^{2}+3 r h\right) \quad\) (See notes below for what is allowed here) \\
Volume \(=300=\frac{1}{2} r^{2} h\) \\
Sub for \(h: S=r^{2}+3 \times \frac{600}{r}=r^{2}+\frac{1800}{r}\) \\
\(\frac{\mathrm{d} S}{\mathrm{~d} r}=2 r-\frac{1800}{r^{2}}\) or \(2 r-1800 r^{-2}\) or \(2 r+-1800 r^{-2}\) \\
\(\frac{\mathrm{d} S}{\mathrm{~d} r}=0 \Rightarrow r^{3}=\ldots, \quad r=\sqrt[3]{900}\), or AWRT 9.7 \(\quad(\) NOT -9.7 or \(\pm 9.7)\) \\
\(\frac{\mathrm{d}^{2} S}{\mathrm{~d} r^{2}}=\ldots . \quad\) and consider sign, \(\frac{\mathrm{d}^{2} S}{\mathrm{~d} r^{2}}=2+\frac{3600}{r^{3}}>0\) so point is a minimum \(S_{\min }=(9.65 \ldots)^{2}+\frac{1800}{9.65 \ldots}\) \\
(Using their value of \(r\), however found, in the given \(S\) formula) \\
\(=279.65 \ldots\) (AWRT: 280) (Dependent on full marks in part (b))
\end{tabular} \\
\hline (a)
(b)

(c) \& | M1 for attempting a formula (with terms added) for surface area. May be incomplete or wrong and may have extra term(s), but must have an $r^{2}$ (or $r^{2} \theta$ ) term and an $r h$ (or $r h \theta$ ) term. |
| :--- |
| In parts (b), (c) and (d), ignore labelling of parts |
| $1^{\text {st }} \mathrm{M} 1$ for attempt at differentiation (one term is sufficient) $r^{n} \rightarrow k r^{n-1}$ |
| $2^{\text {nd }} \mathrm{M} 1$ for setting their derivative (a 'changed function') $=0$ and solving as far as $r^{3}=\ldots$ (depending upon their 'changed function', this could be $r=\ldots$ or $r^{2}=\ldots$, etc., but the algebra must deal with a negative power of $r$ and should be sound apart from possible sign errors, so that $r^{n}=\ldots$ is consistent with their derivative). |
| M1 for attempting second derivative (one term is sufficient) $r^{n} \rightarrow k r^{n-1}$, and considering its sign. Substitution of a value of $r$ is not required. (Equating it to zero is M0). |
| A1ft for a correct second derivative (or correct ft from their first derivative) and a valid reason (e.g. > 0), and conclusion. The actual value of the second derivative, if found, can be ignored. To score this mark as ft , their second derivative must indicate a minimum. |
| Alternative: |
| M1: Find value of $\frac{\mathrm{d} S}{\mathrm{~d} r}$ on each side of their value of $r$ and consider sign. |
| A1ft: Indicate sign change of negative to positive for $\frac{\mathrm{d} S}{\mathrm{~d} r}$, and conclude minimum. |
| Alternative: |
| M1: Find value of $S$ on each side of their value of $r$ and compare with their 279.65. |
| A1ft: Indicate that both values are more than 279.65 , and conclude minimum. | <br>

\hline
\end{tabular}

## Mark Scheme (Results) J anuary 2010

## GCE

## Core Mathematics C2 (6664)

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J anuary 2010
Core Mathematics C2 6664 Mark Scheme

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q1 | $\begin{gathered} {\left[(3-x)^{6}=\right] 3^{6}+3^{5} \times 6 \times(-x)+3^{4} \times\binom{ 6}{2} \times(-x)^{2}} \\ \\ =729, \quad-1458 x, \quad+1215 x^{2} \end{gathered}$ | M1 B1,A1, A1 [4] |
| Notes | M1 for either the $x$ term or the $x^{2}$ term. Requires correct binomial coefficient in any form with the correct power of $x$ - condone lack of negative sign and wrong power of 3. This mark may be given if no working is shown, but one of the terms including $x$ is correct. Allow $\frac{6}{1}$, or $\frac{6}{2}$ (must have a power of 3 , even if only power 1 ) <br> First term must be 729 for $\mathbf{B 1}$, ( writing just $3^{6}$ is $\mathbf{B 0}$ ) can isw if numbers added to this constant later. Can allow 729(1... <br> Term must be simplified to $-1458 x$ for A1cao. The $x$ is required for this mark. <br> Final A1is c.a.o and needs to be $+1215 x^{2}$ (can follow omission of negative sign in working) <br> Descending powers of $x$ would be $x^{6}+3 \times 6 \times(-x)^{5}+3^{2} \times\binom{ 6}{4} \times(-x)^{4}+$.. <br> i.e. $x^{6}-18 x^{5}+135 x^{4}+$. This is M1B1A0A0 if completely "correct" or M1 B0A0A0 for correct binomial coefficient in any form with the correct power of $x$ as before |  |
| Alternative | NB Alternative method: $(3-x)^{6}=3^{6}\left(1+6 \times\left(-\frac{x}{3}\right)+\binom{6}{2} \times\left(-\frac{x}{3}\right)^{2}+..\right)$ is M1B0A0A0 - answers must be simplified to 729, $-1458 x, \quad+1215 x^{2}$ for full marks (awarded as before) <br> The mistake $(3-x)^{6}=3\left(1-\frac{x}{3}\right)^{6}=3\left(1+6 \times\left(-\frac{x}{3}\right)+\times\binom{ 6}{2} \times\left(-\frac{x}{3}\right)^{2}+..\right)$ may also be awarded M1B0A0A0 <br> Another mistake $3^{6}\left(1-6 x+15 x^{2} \ldots\right)=729 \ldots$ would be M1B1A0A0 |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q2 (a) <br> (b) | $\begin{align*} & 5 \sin x=1+2\left(1-\sin ^{2} x\right) \\ & 2 \sin ^{2} x+5 \sin x-3=0  \tag{*}\\ & (2 s-1)(s+3)=0 \text { giving } s= \\ & {\left[\sin x=-3 \text { has no solution] so } \sin x=\frac{1}{2}\right.} \\ & \therefore \quad x=30,150 \end{align*}$ | M1  <br> A1cso (2)  <br> M1  <br> A1  <br>   <br> B1, B1ft (4)  <br>   |
| (a) <br> (b) | M1 for a correct method to change $\cos ^{2} x$ into $\sin ^{2} x$ (must use $\cos ^{2} x=1-\sin ^{2} x$ ) <br> A1 need 3 term quadratic printed in any order with $=0$ included <br> M1 for attempt to solve given quadratic (usual rules for solving quadratics) (can use any variable here, $s, y, x$, or $\sin x$ ) <br> A1 requires no incorrect work seen and is for $\sin x=\frac{1}{2} \quad$ or $x=\sin ^{-1} \frac{1}{2}$ $y=\frac{1}{2}$ is A0 (unless followed by $x=30$ ) <br> B1 for $30(\alpha)$ not dependent on method $2^{\text {nd }} \mathrm{B} 1$ for $180-\alpha \quad$ provided in required range (otherwise 540- $\alpha$ ) <br> Extra solutions outside required range: Ignore <br> Extra solutions inside required range: Lose final B1 <br> Answers in radians: Lose final B1 <br> S.C. Merely writes down two correct answers is M0A0B1B1 <br> Or $\sin x=\frac{1}{2} \quad \therefore \quad x=30,150$ is M1A1B1B1 <br> Just gives one answer : 30 only is M0A0B1B0 or 150 only is M0A0B0B1 <br> NB Common error is to factorise wrongly giving $(2 \sin x+1)(\sin x-3)=0$ [ $\sin x=3$ gives no solution] $\sin x=-\frac{1}{2} \quad \Rightarrow \quad x=210,330$ <br> This earns M1 A0 B0 B1ft <br> Another common error is to factorise correctly $(2 \sin x-1)(\sin x+3)=0$ and follow this with $\sin x=\frac{1}{2}, \sin x=3$ then $x=30^{\circ}, 150^{\circ}$ <br> This would be M1 A0 B1 B1 |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q3 (a) <br> (b) | $\begin{aligned} & \mathrm{f}\left(\frac{1}{2}\right)=2 \times \frac{1}{8}+a \times \frac{1}{4}+b \times \frac{1}{2}-6 \\ & \mathrm{f}\left(\frac{1}{2}\right)=-5 \Rightarrow \frac{1}{4} a+\frac{1}{2} b=\frac{3}{4} \quad \text { or } a+2 b=3 \\ & \mathrm{f}(-2)=-16+4 a-2 b-6 \\ & \mathrm{f}(-2)=0 \Rightarrow 4 a-2 b=22 \end{aligned}$ <br> Eliminating one variable from 2 linear simultaneous equations in $a$ and $b$ $a=5$ and $b=-1$ $\begin{aligned} 2 x^{3}+5 x^{2}-x-6 & =(x+2)\left(2 x^{2}+x-3\right) \\ & =(x+2)(2 x+3)(x-1) \end{aligned}$ <br> NB $(x+2)\left(x+\frac{3}{2}\right)(2 x-2)$ is A0 But $2(x+2)\left(x+\frac{3}{2}\right)(x-1)$ is A1 | M1  <br> A1  <br> M1  <br> A1  <br> M1  <br> A1 (6) <br> M1  <br> M1A1 (3) <br>  [9] |
| (a) | $1^{\text {st }}$ M1 for attempting $f\left( \pm \frac{1}{2}\right)$ Treat the omission of the -5 here as a slip and allow the M mark. <br> $1^{\text {st }}$ A1 for first correct equation in $a$ and $b$ simplified to three non zero terms (needs -5 used) <br> s.c. If it is not simplified to three terms but is correct and is then used correctly with second equation to give correct answers- this mark can be awarded later. <br> $2^{\text {nd }}$ M1 for attempting $f(\mp 2)$ <br> $2^{\text {nd }}$ A1 for the second correct equation in $a$ and $b$. simplified to three terms (needs 0 used) s.c. If it is not simplified to three terms but is correct and is then used correctly with first equation to give correct answers - this mark can be awarded later. <br> $3^{\text {rd }}$ M1 for an attempt to eliminate one variable from 2 linear simultaneous equations in $a$ and $b$ <br> $3^{\text {rd }} \mathrm{A} 1$ for both $a=5$ and $b=-1$ (Correct answers here imply previous two A marks) <br> $1^{\text {st }}$ M1 for attempt to divide by $(x+2)$ leading to a 3TQ beginning with correct term usually $2 x^{2}$ <br> $2^{\text {nd }} \mathrm{M} 1$ for attempt to factorize their quadratic provided no remainder <br> A1 is cao and needs all three factors <br> Ignore following work (such as a solution to a quadratic equation). |  |
| (a) | Alternative; <br> M1 for dividing by $(2 x-1)$, to get $x^{2}+\left(\frac{a+1}{2}\right) x+$ constant with remainder as a <br> function of $\boldsymbol{a}$ and $\boldsymbol{b}$, and A1 as before for equations stated in scheme. <br> M1 for dividing by $(x+2)$, to get $2 x^{2}+(a-4) x \ldots$ (No need to see remainder as it is zero and comparison of coefficients may be used) with A1 as before <br> Alternative; <br> M1 for finding second factor correctly by factor theorem, usually $(x-1)$ <br> M1 for using two known factors to find third factor, usually ( $2 x \pm 3$ ) <br> Then A1 for correct factorisation written as product $(x+2)(2 x+3)(x-1)$ |  |


| Question Number | Scheme ${ }_{\text {S }}$ Marks |
| :---: | :---: |
| Q4 <br> (a) <br> (b) | Either $\frac{\sin (A \hat{C} B)}{5}=\frac{\sin 0.6}{4}$ <br> $\therefore A \hat{C} B=\arcsin (0.7058 . .)$. <br> $=[0.7835 .$. or 2.358$]$ <br> Use angles of triangle <br> $A \hat{B} C=\pi-0.6-A \hat{C} B$ <br> $(B u t$ as $A C$ is the longest side so $)$ <br> $A \hat{B} C=1.76 \quad\left(^{*}\right)(3 \mathrm{sf})\left[\right.$ Allow $\left.100.7^{\circ} \rightarrow 1.76\right]$ <br> In degrees $0.6=34.377^{\circ}, \mathrm{AC} B=44.9^{\circ}$$\begin{aligned} & \text { or } 4^{2}=b^{2}+5^{2}-2 \times b \times 5 \cos 0.6 \\ & \therefore b=\frac{10 \cos 0.6 \pm \sqrt{\left(100 \cos ^{2} 0.6-36\right)}}{2} \\ & =[6.96 \text { or } 1.29] \end{aligned}$ <br> Use sine / cosine rule with value for $b$ $\sin B=\frac{\sin 0.6}{4} \times b \text { or } \cos B=\frac{25+16-b^{2}}{40}$ <br> (But as $A C$ is the longest side so) $A \hat{B} C=1.76\left({ }^{*}\right)(3 \mathrm{sf})$ <br> $\lfloor C \hat{B} D=\pi-1.76=1.38\rfloor$ Sector area $=\frac{1}{2} \times 4^{2} \times(\pi-1.76)=[11.0 \sim 11.1] \frac{1}{2} \times 4^{2} \times 79.3$ is M0 <br> Area of $\triangle A B C=\frac{1}{2} \times 5 \times 4 \times \sin (1.76)=[9.8]$ or $\frac{1}{2} \times 5 \times 4 \times \sin 101$ <br> Required area $=$ awrt 20.8 or 20.9 or 21.0 or gives 21 (2sf) after correct work. |
| (a) (b) | $1^{\text {st }} \mathrm{M} 1$ for correct use of sine rule to find $A C B$ or cosine rule to find $b$ ( M 0 for ABC here or for use of $\sin \mathrm{x}$ where $x$ could be $A B C$ ) <br> $2^{\text {nd }} \mathrm{M} 1$ for a correct expression for angle $A C B$ (This mark may be implied by .7835 or by arcsin (.7058)) and needs accuracy. In second method this M1 is for correct expression for $b$ - may be implied by 6.96. [Note $10 \cos 0.6 \approx 8.3$ ] (do not need two answers) <br> $3^{\text {rd }} \mathrm{M} 1$ for a correct method to get angle $A B C$ in method (i) or $\sin A B C$ or $\cos A B C$, in method (ii) (If $\sin B>1$, can have M1A0) <br> A1cso for correct work leading to 1.76 3sf . Do not need to see angle 0.1835 considered and rejected. <br> $1^{\text {st }} \mathrm{M} 1$ for a correct expression for sector area or a value in the range $11.0-11.1$ <br> $2^{\text {nd }} \mathrm{M} 1$ for a correct expression for the area of the triangle or a value of 9.8 <br> Ignore 0.31 (working in degrees) as subsequent work. <br> A1 for answers which round to 20.8 or 20.9 or 21.0 . No need to see units. |
| (a) | Special case If answer 1.76 is assumed then usual mark is M0 M0 M0 A0. A Fully checked method may be worth M1 M1 M0 A0. A maximum of 2 marks. The mark is either 2 or 0 . <br> Either M1 for $A \hat{C} B$ is found to be 0,7816 (angles of triangle) then <br> M1 for checking $\frac{\sin (A \hat{C} B)}{5}=\frac{\sin 0.6}{4}$ with conclusion giving numerical answers <br> This gives a maximum mark of $\mathbf{2 / 4}$ <br> OR M1 for $b$ is found to be 6.97 (cosine rule) <br> M1 for checking $\frac{\sin (A B C)}{b}=\frac{\sin 0.6}{4}$ with conclusion giving numerical answers <br> This gives a maximum mark of $\mathbf{2 / 4}$ <br> Candidates making this assumption need a complete method. They cannot earn M1M0. <br> So the score will be 0 or 2 for part (a). Circular arguments earn 0/4. |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q5 (a) <br> (b) | $\begin{aligned} & \log _{x} 64=2 \Rightarrow 64=x^{2} \\ & \log _{2}(11-6 x)=\log _{2}(x-1)^{2}+3 \\ & \log _{2}\left[\frac{11-6 x}{(x-1)^{2}}\right]=3 \\ & \frac{11-6 x}{(x-1)^{2}}=2^{3} \\ &\{11-6 x\left.=8\left(x^{2}-2 x+1\right)\right\} \text { and so } 0=8 x^{2}-10 x-3 \\ & 0=(4 x+1)(2 x-3) \Rightarrow x=\ldots \\ & x=\frac{3}{2},\left[-\frac{1}{4}\right] \end{aligned}$ | M1 <br> A1 <br> (2) <br> M1 <br> M1 <br> M1 <br> A1 <br> dM1 <br> A1 <br> (6) <br> [8] |
| (a) (b) | M1 for getting out of logs <br> A1 Do not need to see $x=-8$ appear and get rejected. Ignore $x=-8$ as extra solution. $x=8$ with no working is M1 A1 <br> $1^{\text {st }}$ M1 for using the nlog$x$ rule <br> $2^{\text {nd }} \mathrm{M} 1$ for using the $\log x-\log y$ rule or the $\log x+\log y$ rule as appropriate <br> $3^{\text {rd }}$ M1 for using 2 to the power- need to see $2^{3}$ or 8 (May see $3=\log _{2} 8$ used) <br> If all three $M$ marks have been earned and logs are still present in equation <br> do not give final M1. So solution stopping at $\log _{2}\left[\frac{11-6 x}{(x-1)^{2}}\right]=\log _{2} 8$ would earn <br> M1M1M0 <br> $1^{\text {st }} \mathrm{A} 1$ for a correct 3 TQ <br> $4^{\text {th }}$ dependent M1 for attempt to solve or factorize their 3TQ to obtain $x=\ldots$ (mark depends on three previous M marks) <br> $2^{\text {nd }} \mathrm{A} 1$ for 1.5 (ignore -0.25 ) <br> s.c 1.5 only - no working - is 0 marks |  |
| (a) | Alternatives <br> Change base : (i) $\frac{\log _{2} 64}{\log _{2} x}=2$, so $\log _{2} x=3$ and $x=2^{3}$, is M1 or (ii) $\frac{\log _{10} 64}{\log _{10} x}=2, \log x=\frac{1}{2} \log 64$ so $x=64^{\frac{1}{2}}$ is M1 then $x=8$ is A1 BUT $\log x=0.903$ so $x=8$ is M1A0 (loses accuracy mark) <br> (iii) $\log _{64} x=\frac{1}{2}$ so $x=64^{\frac{1}{2}}$ is M1 then $x=8$ is A1 |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q6 (a) <br> (b) <br> (c) <br> (d) | $\begin{aligned} & \begin{aligned} & 18000 \times(0.8)^{3} \quad=£ 9216 * \quad \text { [may see } \frac{4}{5} \text { or } 80 \% \text { or equivalent]. } \\ & 18000 \times(0.8)^{n}<1000 \\ & n \log (0.8)<\log \left(\frac{1}{18}\right) \text { so } n=13 . \\ & n>\frac{\log \left(\frac{1}{18}\right)}{\log (0.8)}=12.952 \ldots .=£ 314.70 \text { or } £ 314.71 \\ & u_{5}=200 \times(1.12)^{4}, \quad \text { awrt } £ 7460 \end{aligned} \\ & S_{15}=\frac{200\left(1.12^{15}-1\right)}{1.12-1} \text { or } \frac{200\left(1-1.12^{15}\right)}{1-1.12},=7455.94 \ldots . . \quad \end{aligned}$ | B1cso (1) <br> M1 <br> M1 <br> A1 cso <br> (3) <br> M1, A1 (2) <br> M1A1, A1 <br> (3) <br> [9] |
| (a) <br> (b) <br> (c) <br> (d) | B1 NB Answer is printed so need working. May see as above or $\times 0.8$ in three steps giving 14400, 11520, 9216. Do not need to see $£$ sign but should see 9216 . <br> $1^{\text {st }} \mathrm{M} 1$ for an attempt to use $n$th term and 1000. Allow $n$ or $n-1$ and allow $>$ or $=$ $2^{\text {nd }}$ M1 for use of logs to find $n$ Allow $n$ or $n-1$ and allow $>$ or $=$ <br> A1 Need $n=13$ This is an accuracy mark and must follow award of both M marks but should not follow incorrect work using $n-1$ for example. <br> Condone slips in inequality signs here. <br> M1 for use of their $a$ and $r$ in formula for $5^{\text {th }}$ term of GP <br> A1 cao need one of these answers - answer can imply method here <br> NB 314.7 - A0 <br> M1 for use of sum to 15 terms of GP using their $a$ and their $r$ ( allow if formula stated correctly and one error in substitution, but must use $n$ not $n-1$ ) <br> $1^{\text {st }}$ A1 for a fully correct expression ( not evaluated) |  |
| (b) (c) (d) | Alternative Methods <br> Trial and Improvement <br> See 989.56 ( or 989 or 990 ) identified with 12, 13 or 14 years for first M1 <br> See 1236.95 ( or 1236 or 1237) identified with 11,12 or 13 years for second M1 <br> Then $n=13$ is A1 (needs both Ms) <br> Special case $18000 \times(0.8)^{n}<1000$ so $n=13$ as $989.56<1000$ is M1M0A0 (not discounted $n=12$ ) <br> May see the terms 224, 250.88, 280.99, 314.71 with a small slip for M1 A0, or done accurately for M1A1 <br> Adds 15 terms $200+224+250.88+\ldots \quad+(977.42) \quad$ M1 <br> Seeing 977... is A1 <br> Obtains answer 7455.94 A1 or awrt £7460 NOT 7450 |  |

\begin{tabular}{|c|c|}
\hline Question Number \& Scheme \(\quad\) Marks \\
\hline \begin{tabular}{l}
Q7 \\
(a) \\
(b) \\
(c) \\
(d)
\end{tabular} \&  \\
\hline (a)
(b)
(c)

(d) \& | M1 for attempt to find $L$ and $M$ |
| :--- |
| A1 Accept $x=1$ and $x=4$, then isw or accept $L=(1,0), M=(4,0)$ |
| Do not accept $L=1, M=4$ nor $(0,1),(0,4)$ (unless subsequent work) |
| Do not need to distinguish $L$ and $M$. Answers imply M1A1. |
| See substitution, working should be shown, need conclusion which could be just $y=4$ or a tick. Allow $y=25-25+4=4$ But not $25-25+4=4$. ( $y=4$ may appear at start $)$ |
| Usually $0=0$ or $4=4$ is B0 |
| M1 for attempt to integrate $x^{2} \rightarrow k x^{3}, x \rightarrow k x^{2}$ or $4 \rightarrow 4 x$ |
| A1 for correct integration of all three terms (do not need constant) isw. |
| Mark correct work when seen. So e.g. $\frac{1}{3} x^{3}-\frac{5}{2} x^{2}+4 x$ is A1 then $2 x^{3}-15 x^{2}+24 x$ would be ignored as subsequent work. |
| B1 for this triangle only (not triangle $L M N$ ) |
| $1^{\text {st }} \mathrm{M} 1$ for substituting 5 into their changed function |
| $2^{\text {nd }} \mathrm{M} 1$ for substituting 4 into their changed function | <br>

\hline (d) \& | Alternative method: $\quad \int_{1}^{5}(x-1)-\left(x^{2}-5 x+4\right) \mathrm{d} x+\int_{1}^{4} x^{2}-5 x+4 \mathrm{~d} x$ can lead to correct answer Constructs $\int_{1}^{5}(x-1)-\left(x^{2}-5 x+4\right) \mathrm{d} x$ is B1 |
| :--- |
| M1 for substituting 5 and 1 and subtracting in first integral M1 for substituting 4 and 1 and subtracting in second integral A1 for answer to first integral i.e. $\frac{32}{3}$ (allow 10.7) and A1 for final answer as before.. | <br>

\hline
\end{tabular}

| (d) | Another alternative |
| :--- | :--- |
|  | $\int_{4}^{5}(x-1)-\left(x^{2}-5 x+4\right) \mathrm{d} x+$ area of triangle $L M P$ |
|  | Constructs $\int_{4}^{5}(x-1)-\left(x^{2}-5 x+4\right) \mathrm{d} x \quad$ is B1 |
|  | M1 for substituting 5 and 4 and subtracting in first integral |
|  | M1 for complete method to find area of triangle (4.5) |
| A1 for answer to first integral i.e. $\frac{5}{3}$ and A1 for final answer as before. |  |
| (d) | Could also use <br>  <br>  <br>  <br> $\int_{4}^{5}(4 x-16)-\left(x^{2}-5 x+4\right) \mathrm{d} x+$ area of triangle $L M N$ <br> Similar scheme to previous one. Triangle has area 6 <br> A1 for finding Integral has value $\frac{1}{6}$ and A1 for final answer as before. |



| Question Number | Scheme ${ }_{\text {a }}$ Marks |
| :---: | :---: |
| Q9 (a) <br> (b) <br> (c) | $\left[y=12 x^{\frac{1}{2}}-x^{\frac{3}{2}}-10\right]$ <br> $\left[y^{\prime}=\right] \quad 6 x^{-\frac{1}{2}}-\frac{3}{2} x^{\frac{1}{2}}$ <br> Puts their $\frac{6}{x^{\frac{1}{2}}}-\frac{3}{2} x^{\frac{1}{2}}=0$ <br> So $x=\quad, \frac{12}{3}=4 \quad$ (If $x=0$ appears also as solution then lose A1) <br> $x=4, \quad \Rightarrow y=12 \times 2-4^{\frac{3}{2}}-10, \quad$ so $y=6$ <br> $y^{\prime \prime}=-3 x^{-\frac{3}{2}}-\frac{3}{4} x^{-\frac{1}{2}}$ <br> [Since $x>0$ ] It is a maximum |
| (a) <br> (b) <br> (c) | $1^{\text {st }}$ M1 for an attempt to differentiate a fractional power $x^{n} \rightarrow x^{n-1}$ <br> A1 a.e.f - can be unsimplified <br> $2^{\text {nd }}$ M1 for forming a suitable equation using their $y^{\prime}=0$ <br> $3^{\text {rd }}$ M1 for correct processing of fractional powers leading to $x=\ldots$ (Can be implied by $x=4$ ) <br> A1 is for $x=4$ only. If $x=0$ also seen and not discarded they lose this mark only. <br> $4^{\text {th }}$ M1 for substituting their value of $x$ back into $y$ to find $y$ value. Dependent on three previous M marks. Must see evidence of the substitution with attempt at fractional powers to give M1A0, but $y=6$ can imply M1A1 <br> M1 for differentiating their $y^{\prime}$ again <br> A1 should be simplified <br> B1 . Clear conclusion needed and must follow correct $y^{\prime \prime \prime}$ It is dependent on previous A mark (Do not need to have found $x$ earlier). <br> (Treat parts (a),(b) and (c) together for award of marks) |

## Mark Scheme (Results) Summer 2010

## GCE

## Core Mathematics C2 (6664)

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## SOME GENERAL PRINCIPLES FOR C2 MARKING

(But the particular mark scheme always takes precedence)

## Method mark for solving 3 term quadratic:

1. Factorisation
$\left(x^{2}+b x+c\right)=(x+p)(x+q)$, where $|p q|=|c|, \quad$ leading to $x=\ldots$
$\left(a x^{2}+b x+c\right)=(m x+p)(n x+q)$, where $|p q|=|c|$ and $|m n|=|a|, \quad$ leading to $x=\ldots$
2. Formula

Attempt to use correct formula (with values for $a, b$ and $c$ ).
3. Completing the square

Solving $x^{2}+b x+c=0: \quad\left(x \pm \frac{b}{2}\right)^{2} \pm q \pm c=0, \quad q \neq 0, \quad$ leading to $x=\ldots$

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first. Normal marking procedure is as follows:
Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values (but refer to the mark scheme first... the application of this principle may vary). Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but will be lost if there is any mistake in the working.

## Equation of a straight line

Apply the following conditions to the $M$ mark for the equation of a line through $(a, b)$ :
If the $a$ and $b$ are the wrong way round the $M$ mark can still be given if a correct formula is seen, (e.g. $y-y_{1}=m\left(x-x_{1}\right)$ ) otherwise M0.

If $(\mathrm{a}, \mathrm{b})$ is substituted into $y=m x+c$ to find $c$, the $M$ mark is for attempting this.

## Answers without working

The rubric says that these may gain no credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required. Most candidates do show working, but there are occasional awkward cases and if the mark scheme does not cover this, please contact your team leader for advice.

## Misreads

A misread must be consistent for the whole question to be interpreted as such.
These are not common. In clear cases, please deduct the first 2 A (or B) marks which would have been lost by following the scheme. (Note that 2 marks is the maximum misread penalty, but that misreads which alter the nature or difficulty of the question cannot be treated so generously and it will usually be necessary here to follow the scheme as written).
Sometimes following the scheme as written is more generous to the candidate than applying the misread rule, so in this case use the scheme as written.
If in doubt, send the response to Review.

## J une 2010 <br> Core Mathematics C2 6664 <br> Mark Scheme

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 1. | (a) 2.35, 3.13, 4.01 (One or two correct B1 B0, all correct B1 B1) Important: If part (a) is blank, or if answers have been crossed out and no replacement answers are visible, please send to Review as 'out of clip'. | B1 B1 |
|  | (b) $\frac{1}{2} \times 0.2 \ldots \ldots$ <br> (or equivalent numerical value) <br> $k\{(1+5)+2(1.65+p+q+r)\}, k$ constant, $k \neq 0 \quad$ (See notes below) $=2.828 \quad$ (awrt 2.83, allowed even after minor slips in values) <br> The fractional answer $\frac{707}{250}$ (or other fraction wrt 2.83) is also acceptable. Answers with no working score no marks. | B1 <br> M1 A1 <br> A1 <br> (4) <br> 6 |
|  | (a) Answers must be given to 2 decimal places. <br> No marks for answers given to only 1 decimal place. <br> (b) The $p, q$ and $r$ below are positive numbers, none of which is equal to any of: $1,5,1.65,0.2,0.4,0.6$ or 0.8 <br> M1 A1: $k\{(1+5)+2(1.65+p+q+r)\}$ <br> M1 A0: $k\{(1+5)+2(1.65+p+q)\}$ or $k\{(1+5)+2(p+q+r)\}$ <br> M0 A0: $k\{(1+5)+2(1.65+p+q+r+$ other value $(s))\}$ <br> Note that if the only mistake is to omit a value from the second bracket, this is considered as a slip and the M mark is allowed. <br> Bracketing mistake: i.e. $\frac{1}{2} \times 0.2(1+5)+2(1.65+2.35+3.13+4.01)$ instead of $\frac{1}{2} \times 0.2\{(1+5)+2(1.65+2.35+3.13+4.01)\}$, so that only the $(1+5)$ is multiplied by 0.1 scores B1 M1 A0 A0 unless the final answer implies that the calculation has been done correctly (then full marks can be given). <br> Alternative: <br> Separate trapezia may be used, and this can be marked equivalently. |  |


| Question Number | Scheme | Marks |  |
| :---: | :---: | :---: | :---: |
| 2 | (a) Attempting to find $\mathrm{f}(3)$ or $\mathrm{f}(-3)$ $f(3)=3(3)^{3}-5(3)^{2}-(58 \times 3)+40=81-45-174+40=-98$ | $\begin{aligned} & \hline \text { M1 } \\ & \text { A1 } \end{aligned}$ | (2) |
|  | (b) $\left\{3 x^{3}-5 x^{2}-58 x+40=(x-5)\right\}\left(3 x^{2}+10 x-8\right)$ <br> Attempt to factorise 3-term quadratic, or to use the quadratic formula (see general principles at beginning of scheme). This mark may be implied by the correct solutions to the quadratic. $\begin{aligned} & (3 x-2)(x+4)=0 \quad x=\ldots \quad \text { of } \quad x=\frac{-10 \pm \sqrt{100+96}}{6} \\ & \frac{2}{3} \text { (or exact equiv.), }-4, \quad 5 \text { (Allow 'implicit' solns, e.g. } \mathrm{f}(5)=0, \text { etc.) } \\ & \text { Completely correct solutions without working: full marks. } \end{aligned}$ | M1 A1 <br> M1 <br> A1 ft <br> A1 | $(5)$ 7 |

(a) Alternative (long division): 'Grid’ method

Divide by $(x-3)$ to get $\left(3 x^{2}+a x+b\right), a \neq 0, b \neq 0$. [M1]
$\left(3 x^{2}+4 x-46\right)$, and -98 seen.

$3 \left\lvert\,$| 3 | -5 | -58 | 40 |
| ---: | ---: | ---: | ---: |
| 0 | 9 | 12 | -138 |
|  | 3 | 4 | -46 |$-98\right.$

(If continues to say 'remainder $=98$ ', isw)
'Grid' method
(b) 1st M requires use of $(x-5)$ to obtain $\left(3 x^{2}+a x+b\right), a \neq 0, b \neq 0$.

$3 |$| 3 | -5 | -58 | 40 |  |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 15 | 50 | -40 |  |
|  | 3 | 10 | -8 | 0 |

$2^{\text {nd }} \mathrm{M}$ for the attempt to factorise their 3-term quadratic, or to solve it using the quadratic formula. Factorisation: $\left(3 x^{2}+a x+b\right)=(3 x+c)(x+d)$, where $|c d|=|b|$.
A1ft: Correct factors for their 3-term quadratic followed by a solution (at least one value, which might be incorrect), or numerically correct expression from the quadratic formula for their 3 -term quadratic.
Note therefore that if the quadratic is correctly factorised but no solutions are given, the last 2 marks will be lost.
Alternative (first 2 marks):
$(x-5)\left(3 x^{2}+a x+b\right)=3 x^{3}+(a-15) x^{2}+(b-5 a) x-5 b=0$,

$$
\text { then compare coefficients to find values of } a \text { and } b \text {. }
$$

$$
\begin{equation*}
a=10, b=-8 \tag{A1}
\end{equation*}
$$

Alternative 1: (factor theorem)
M1: Finding that $\mathrm{f}(-4)=0$
A1: Stating that $(x+4)$ is a factor.
M1: Finding third factor $(x-5)(x+4)(3 x \pm 2)$.
A1: Fully correct factors (no ft available here) followed by a solution, (which might be incorrect).
A1: All solutions correct.
Alternative 2: (direct factorisation)
M1: Factors $(x-5)(3 x+p)(x+q) \quad$ A1: $p q=-8$
M1: $(x-5)(3 x \pm 2)(x \pm 4)$
Final A marks as in Alternative 1.
Throughout this scheme, allow $\left(x \pm \frac{2}{3}\right)$ as an alternative to ( $3 x \pm 2$ ).

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 3 | (a) $\left(\frac{\mathrm{d} y}{\mathrm{~d} x}=\right) 2 x-\frac{1}{2} k x^{-\frac{1}{2}} \quad$ (Having an extra term, e.g. $+C$, is A0) | M1 A1 |
|  | (b) Substituting $x=4$ into their $\frac{\mathrm{d} y}{\mathrm{~d} x}$ and 'compare with zero' (The mark is allowed for: $<,>,=, \leq, \geq$ ) <br> $8-\frac{k}{4}<0 \quad k>32 \quad($ or $32<k) \quad$ Correct inequality needed | M1 <br> A1 |
|  | (a) M: $x^{2} \rightarrow c x$ or $k \sqrt{x} \rightarrow c x^{-\frac{1}{2}} \quad(c$ constant, $c \neq 0)$ <br> (b) Substitution of $x=4$ into $y$ scores M0. However, $\frac{\mathrm{d} y}{\mathrm{~d} x}$ is sometimes called $y$, and in this case the M mark can be given. <br> $\frac{\mathrm{d} y}{\mathrm{~d} x}=0$ may be 'implied' for M1, when, for example, a value of $k$ or an inequality solution for $k$ is found. <br> Working must be seen to justify marks in (b), i.e. $k>32$ alone is M0 A0. |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 4 | (a) $(1+a x)^{7}=1+7 a x \ldots$ or $1+7(a x) \ldots$ (Not unsimplified versions) $+\frac{7 \times 6}{2}(a x)^{2}+\frac{7 \times 6 \times 5}{6}(a x)^{3}$ Evidence from one of these terms is enough $\begin{array}{ll} +21 a^{2} x^{2} & \text { or }+21(a x)^{2} \text { or }+21\left(a^{2} x^{2}\right) \\ +35 a^{3} x^{3} & \text { or }+35(a x)^{3} \text { or }+35\left(a^{3} x^{3}\right) \end{array}$ | B1 <br> M1 <br> A1 <br> A1 <br> (4) |
|  | (b) $21 a^{2}=525$ $a= \pm 5 \quad \text { (Both values are required) }$ <br> (The answer $a=5$ with no working scores M1 A0) | M1 <br> A1 <br> (2) 6 |
|  | (a) The terms can be 'listed' rather than added. <br> M1: Requires correct structure: a correct binomial coefficient in any form (perhaps from Pascal's triangle) with the correct power of $x$. Allow missing $a$ 's and wrong powers of $a$, e.g. $\frac{7 \times 6}{2} a x^{2}, \quad \frac{7 \times 6 \times 5}{3 \times 2} x^{3}$ <br> However, $21+a^{2} x^{2}+35+a^{3} x^{3}$ or similar is M0. $1+7 a x+21+a^{2} x^{2}+35+a^{3} x^{3}=57+\ldots$. scores the B1 (isw). $\binom{7}{2}$ and $\binom{7}{3}$ or equivalent such as ${ }^{7} C_{2}$ and ${ }^{7} C_{3}$ are acceptable, but not $\left(\frac{7}{2}\right)$ or $\left(\frac{7}{3}\right)$ (unless subsequently corrected). <br> $1^{\text {st }}$ A1: Correct $x^{2}$ term. $2^{\text {nd }}$ A1: Correct $x^{3}$ term (The binomial coefficients must be simplified). <br> Special case: <br> If $(a x)^{2}$ and $(a x)^{3}$ are seen within the working, but then lost... <br> $\ldots$ A1 A0 can be given if $21 a x^{2}$ and $35 a x^{3}$ are both achieved. a's omitted throughout: <br> Note that only the M mark is available in this case. <br> (b) M: Equating their coefficent of $x^{2}$ to 525 . <br> An equation in $a$ or $a^{2}$ alone is required for this M mark, but allow 'recovery' that shows the required coefficient, e.g. $\begin{aligned} 21 a^{2} x^{2}=525 & \Rightarrow 21 a^{2}=525 \text { is acceptable, } \\ \text { but } 21 a^{2} x^{2}=525 & \Rightarrow a^{2}=25 \text { is not acceptable. } \end{aligned}$ <br> After 21ax ${ }^{2}$ in the answer for (a), allow 'recovery' of $a^{2}$ in (b) so that full marks are available for (b) (but not retrospectively for (a)). |  |


| Question Number | Scheme |  |  |
| :---: | :---: | :---: | :---: |
| 5 | (a) $\tan \theta=\frac{2}{5}$ (or 0.4 ) (i.s.w. if a value of $\theta$ is subsequently found) Requires the correct value with no incorrect working seen. | B1 | (1) |
|  | (b) awrt $21.8(\alpha)$ <br> (Also allow awrt 68.2, ft from $\tan \theta=\frac{5}{2}$ in (a), but no other ft ) (This value must be seen in part (b). It may be implied by a correct solution, e.g. 10.9) | B1 |  |
|  | $180+\alpha(=201.8)$, or $90+(\alpha / 2)$ (if division by 2 has already occurred) ( $\alpha$ found from $\tan 2 x=\ldots$ or $\tan x=\ldots$ or $\sin 2 x= \pm \ldots$ or $\cos 2 x= \pm \ldots$ ) | M1 |  |
|  | $360+\alpha(=381.8), \text { or } 180+(\alpha / 2)$ <br> ( $\alpha$ found from $\tan 2 x=\ldots$ or $\sin 2 x=\ldots$ or $\cos 2 x=\ldots$ ) <br> OR $540+\alpha(=561.8)$, or $270+(\alpha / 2)$ <br> ( $\alpha$ found from $\tan 2 x=\ldots$ ) | M1 |  |
|  | Dividing at least one of the angles by 2 <br> ( $\alpha$ found from $\tan 2 x=\ldots$ or $\sin 2 x=\ldots$ or $\cos 2 x=\ldots$ ) | M1 |  |
|  | $x=10.9,100.9,190.9,280.9 \quad \text { (Allow awrt) }$ | A1 | (5) |
|  |  |  | 6 |

(b) Extra solution(s) in range: Loses the final A mark.

Extra solutions outside range: Ignore (whether correct or not).
Common answers:
10.9 and 100.9 would score B1 M1 M0 M1 A0 (Ensure that these M marks are awarded) 10.9 and 190.9 would score B1 M0 M1 M1 A0 (Ensure that these M marks are awarded) Alternatives:
(i) $2 \cos 2 x-5 \sin 2 x=0$

$$
\begin{aligned}
R \cos (2 x+\lambda)=0 \quad \lambda=68.2 \Rightarrow 2 x+68.2=90 & \text { B1 } \\
2 x+\lambda=270 & \text { M1 } \\
2 x+\lambda=450 \text { or } \quad 2 x+\lambda=630 & \text { M1 } \\
\text { Subtracting } \lambda \text { and dividing by } 2 \text { (at least once) } & \text { M1 }
\end{aligned}
$$

(ii) $25 \sin ^{2} 2 x=4 \cos ^{2} 2 x=4\left(1-\sin ^{2} 2 x\right)$

$$
29 \sin ^{2} 2 x=4 \quad 2 x=21.8 \quad \text { B1 }
$$

The M marks are scored as in the main scheme, but extra solutions will be likely, losing the A mark.
Using radians:
B1: Can be given for awrt 0.38 ( $\beta$ )
M1: For $\pi+\beta$ or $180+\beta$
M1: For $2 \pi+\beta$ or $3 \pi+\beta$ (Must now be consistently radians)
M1: For dividing at least one of the angles by 2
A1: For this mark, the answers must be in degrees.
(Correct) answers only (or by graphical methods):
$B$ and $M$ marks can be awarded by implication, e.g.
10.9 scores B1 M0 M0 M1 A0
10.9, 100.9 scores B1 M1 M0 M1 A0
10.9, 100.9, 190.9, 280.9 scores full marks.

Using 11, etc. instead of 10.9 can still score the M marks by implication.


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 7 | (a) $2 \log _{3}(x-5)=\log _{3}(x-5)^{2}$ $\log _{3}(x-5)^{2}-\log _{3}(2 x-13)=\log _{3} \frac{(x-5)^{2}}{2 x-13}$ <br> $\log _{3} 3=1$ seen or used correctly $\begin{align*} \log _{3}\left(\frac{P}{Q}\right)=1 \Rightarrow & P=3 Q \quad\left\{\frac{(x-5)^{2}}{2 x-13}=3 \Rightarrow(x-5)^{2}=3(2 x-13)\right\} \\ & x^{2}-16 x+64=0 \tag{*} \end{align*}$ | B1 <br> M1 <br> B1 <br> M1 <br> A1 cso <br> (5) |
|  | (b) $(x-8)(x-8)=0 \quad \Rightarrow \quad x=8 \quad$ Must be seen in part (b). Or: Substitute $x=8$ into original equation and verify. Having additional solution(s) such as $x=-8$ loses the A mark. $x=8$ with no working scores both marks. | M1 A1 |

(a) Marks may be awarded if equivalent work is seen in part (b).

1st M: $\log _{3}(x-5)^{2}-\log _{3}(2 x-13)=\frac{\log _{3}(x-5)^{2}}{\log _{3}(2 x-13)}$ is M0
$2 \log _{3}(x-5)-\log _{3}(2 x-13)=2 \log \frac{x-5}{2 x-13}$ is M0
$2^{\text {nd }} \mathrm{M}:$ After the first mistake above, this mark is available only if there is 'recovery' to the required $\log _{3}\left(\frac{P}{Q}\right)=1 \Rightarrow P=3 Q$. Even then the final mark (cso) is lost.
'Cancelling logs', e.g. $\frac{\log _{3}(x-5)^{2}}{\log _{3}(2 x-13)}=\frac{(x-5)^{2}}{2 x-13}$ will also lose the $2^{\text {nd }} M$.
A typical wrong solution:
$\log _{3} \frac{(x-5)^{2}}{2 x-13}=1 \quad \Rightarrow \quad \log _{3} \frac{(x-5)^{2}}{2 x-13}=3 \quad \Rightarrow \frac{(x-5)^{2}}{2 x-13}=3 \quad \Rightarrow \quad(x-5)^{2}=3(2 x-13)$
(Wrong step here)
This, with no evidence elsewhere of $\log _{3} 3=1$, scores B1 M1 B0 M0 A0
However, $\log _{3} \frac{(x-5)^{2}}{2 x-13}=1 \Rightarrow \frac{(x-5)^{2}}{2 x-13}=3$ is correct and could lead to full marks.
(Here $\log _{3} 3=1$ is implied).

## No $\log$ methods shown:

It is $\underline{\text { not }}$ acceptable to jump immediately to $\frac{(x-5)^{2}}{2 x-13}=3$. The only mark this scores is the $1^{\text {st }} \mathrm{B} 1$ (by generous implication).
(b) M1: Attempt to solve the given quadratic equation (usual rules), so the factors $(x-8)(x-8)$ with no solution is M0.

\begin{tabular}{|c|c|c|}
\hline Question Number \& Scheme \& Marks \\
\hline \multirow[t]{3}{*}{8} \& \begin{tabular}{l}
(a) \(\frac{\mathrm{d} y}{\mathrm{~d} x}=3 x^{2}-20 x+k\) \\
(Differentiation is required)
\[
\begin{equation*}
\text { At } x=2, \frac{\mathrm{~d} y}{\mathrm{~d} x}=0 \text {, so } 12-40+k=0 \quad k=28 \tag{*}
\end{equation*}
\] \\
N.B. The ' \(=0\) ' must be seen at some stage to score the final mark. \\
Alternatively: (using \(k=28\) )
\[
\begin{equation*}
\frac{\mathrm{d} y}{\mathrm{~d} x}=3 x^{2}-20 x+28 \tag{M1A1}
\end{equation*}
\] \\
'Assuming' \(k=28\) only scores the final cso mark if there is justification that \(\frac{\mathrm{d} y}{\mathrm{~d} x}=0\) at \(x=2\) represents the maximum turning point.
\end{tabular} \& M1 A1
A1 cso

(3) <br>

\hline \& | $\begin{aligned} & \text { (b) } \int\left(x^{3}-10 x^{2}+28 x\right) \mathrm{d} x=\frac{x^{4}}{4}-\frac{10 x^{3}}{3}+\frac{28 x^{2}}{2} \quad \text { Allow } \frac{k x^{2}}{2} \text { for } \frac{28 x^{2}}{2} \\ & {\left[\frac{x^{4}}{4}-\frac{10 x^{3}}{3}+14 x^{2}\right]_{0}^{2}=\ldots} \end{aligned} \quad\left(=4-\frac{80}{3}+56=\frac{100}{3}\right) 8 .$ |
| :--- |
| (With limits 0 to 2 , substitute the limit 2 into a 'changed function') |
| $y$-coordinate of $P=8-40+56=24$ |
| Allow if seen in part (a) |
| (The B1 for 24 may be scored by implication from later working) Area of rectangle $=2 \times($ their $y$-coordinate of $P$ ) |
| Area of $R=($ their 48$)-\left(\right.$ their $\left.\frac{100}{3}\right)=\frac{44}{3}\left(14 \frac{2}{3}\right.$ or $\left.14 . \dot{6}\right)$ |
| If the subtraction is the 'wrong way round', the final A mark is lost. | \& | M1 A1 |
| :--- |
| M1 |
| B1 |
| M1 A1 |
| (6) | <br>


\hline \& | (a) M: $x^{n} \rightarrow c x^{n-1}$ ( $c$ constant, $\left.c \neq 0\right)$ for one term, seen in part (a). |
| :--- |
| (b) $1^{\text {st }} \mathrm{M}: x^{n} \rightarrow c x^{n+1}(c$ constant, $c \neq 0)$ for one term. |
| Integrating the gradient function loses this M mark. |
| 2ndM: Requires use of limits 0 and 2 , with 2 substituted into a 'changed function'. (It may, for example, have been differentiated). |
| Final M: Subtract their values either way round. This mark is dependent on the use of calculus and a correct method attempt for the area of the rectangle. |
| A1: Must be exact, not 14.67 or similar, but isw after seeing, say, $\frac{44}{3}$. |
| Alternative: (effectively finding area of rectangle by integration) $\int\left\{24-\left(x^{3}-10 x^{2}+28 x\right)\right\} \mathrm{d} x=24 x-\left(\frac{x^{4}}{4}-\frac{10 x^{3}}{3}+\frac{28 x^{2}}{2}\right) \text {, etc. }$ |
| This can be marked equivalently, with the $1^{\text {st }} \mathrm{A}$ being for integrating the same 3 terms correctly. The 3rd M (for subtraction) will be scored at the same stage as the $2^{\text {nd }} \mathrm{M}$. If the subtraction is the 'wrong way round', the final A mark is lost. | \& <br>

\hline
\end{tabular}



| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 10 | (a) $(10-2)^{2}+(7-1)^{2}$ or $\sqrt{(10-2)^{2}+(7-1)^{2}}$ <br> $(x \pm 2)^{2}+(y \pm 1)^{2}=k \quad(k$ a positive value) $)$ <br> $(x-2)^{2}+(y-1)^{2}=100 \quad$ (Accept $10^{2}$ for 100) <br> (Answer only scores full marks) | $\begin{align*} & \text { M1 A1 } \\ & \text { M1 } \\ & \text { A1 } \tag{4} \end{align*}$ |
|  | (b) (Gradient of radius $=\frac{7-1}{10-2}=\frac{6}{8}$ (or equiv.) Must be seen in part (b) Gradient of tangent $=\frac{-4}{3} \quad$ (Using perpendicular gradient method) $y-7=m(x-10) \quad$ Eqn., in any form, of a line through $(10,7)$ with any numerical gradient (except 0 or $\infty$ ) <br> $y-7=\frac{-4}{3}(x-10)$ or equiv (ft gradient of radius, dep. on both M marks) $\{3 y=-4 x+61\}$ <br> (N.B. The A1 is only available as $\underline{\mathrm{ft}}$ after B 0 ) <br> The unsimplified version scores the A mark (isw if necessary... subsequent mistakes in simplification are not penalised here. The equation must at some stage be exact, not, e.g. $y=-1.3 x+20.3$ | B1 <br> M1 <br> M1 <br> Alft <br> (4) |
|  | (c) $\sqrt{r^{2}-\left(\frac{r}{2}\right)^{2}}$ Condone sign slip if there is evidence of correct use of Pythag. $=\sqrt{10^{2}-5^{2}}$ or numerically exact equivalent $P Q(=2 \sqrt{75})=10 \sqrt{3} \quad$ Simplest surd form $10 \sqrt{3}$ required for final mark | M1 <br> A1 <br> A1 <br> (3) <br> 11 |
|  | (b) $2^{\mathrm{nd}} \mathrm{M}$ : Using $(10,7)$ to find the equation, in any form, of a straight line through ( 10,7 ), with any numerical gradient (except 0 or $\infty$ ). <br> Alternative: $2^{\text {nd }} \mathrm{M}$ : Using $(10,7)$ and an $m$ value in $y=m x+c$ to find a value of $c$. <br> (b) Alternative for first 2 marks (differentiation): $2(x-2)+2(y-1) \frac{\mathrm{d} y}{\mathrm{~d} x}=0 \quad$ or equiv. <br> Substitute $x=10$ and $y=7$ to find a value for $\frac{\mathrm{d} y}{\mathrm{~d} x} \quad$ M1 <br> (This M mark can be awarded generously, even if the attempted 'differentiation' is not 'implicit'). <br> (c) Alternatives: <br> To score M1, must be a fully correct method to obtain $\frac{1}{2} P Q$ or $P Q$. $1^{\text {st }} \mathrm{A} 1$ : For alternative methods that find $P Q$ directly, this mark is for an exact numerically correct version of $P Q$. |  |

# Mark Scheme (Results) J anuary 2011 

## GCE

## GCE Core Mathematics C2 (6664) Paper 1

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## General Instructions for Marking

1. The total number of marks for the paper is 75 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- Mmarks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod - benefit of doubt
- ft - follow through
- the symbol fwill be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- $\quad$ The second mark is dependent on gaining the first mark


## J anuary 2011 Core Mathematics C2 6664 Mark Scheme

| Question Number | Scheme ${ }^{\text {S }}$ Marks |
| :---: | :---: |
| 1. (a) | $\mathrm{f}(x)=x^{4}+x^{3}+2 x^{2}+a x+b$ <br> Attempting $\mathrm{f}(1)$ or $\mathrm{f}(-1)$. <br> $\mathrm{f}(1)=1+1+2+a+b=7$ or $4+a+b=7 \Rightarrow a+b=3$ (as required) AG |
| (b) | Attempting $\mathrm{f}(-2)$ or $\mathrm{f}(2)$. M1 <br> $\mathrm{f}(-2)=16-8+8-2 a+b=-8$  <br> Solving both equations simultaneously to get as far as $a=\ldots$ or $b=\ldots$ A1 <br> Any one of $a=9$ or $b=-6$ dM1 <br> Both $a=9$ and $b=-6$ A1 <br>  A1 cso <br>  [5) |
|  | Notes |
| (a) | M1 for attempting either $f(1)$ or $f(-1)$. <br> A1 for applying $f(1)$, setting the result equal to 7 , and manipulating this correctly to give the result given on the paper as $a+b=3$. Note that the answer is given in part (a). |
| (b) | M1: attempting either $\mathrm{f}(-2)$ or $\mathrm{f}(2)$. <br> A1: correct underlined equation in $a$ and $b$; eg $\underline{16-8+8-2 a+b=-8}$ or equivalent, eg $-2 a+b=-24$. <br> dM 1 : an attempt to eliminate one variable from 2 linear simultaneous equations in $a$ and $b$. Note that this mark is dependent upon the award of the first method mark. <br> A1: any one of $a=9$ or $b=-6$. <br> A1: both $a=9$ and $b=-6$ and a correct solution only. |
|  | Alternative Method of Long Division: <br> (a) M1 for long division by $(x-1)$ to give a remainder in $a$ and $b$ which is independent of $x$. <br> A1 for $\{$ Remainder $=\} b+a+4=7$ leading to the correct result of $a+b=3$ (answer given.) <br> (b) M1 for long division by $(x+2)$ to give a remainder in $a$ and $b$ which is independent of $x$. <br> A1 for $\{$ Remainder $=\} \underline{b-2(a-8)=-8}\{\Rightarrow-2 a+b=-24\}$. <br> Then dM1A1A1 are applied in the same way as before. |


| Question Number | Scheme ${ }^{\text {a }}$ Marks |
| :---: | :---: |
| 2. <br> (a) | $11^{2}=8^{2}+7^{2}-(2 \times 8 \times 7 \cos C)$ M1 <br> $\cos C=\frac{8^{2}+7^{2}-11^{2}}{2 \times 8 \times 7}($ or equivalent $)$  <br> $\{\hat{C}=1.64228 \ldots\} \Rightarrow \hat{C}=$ awrt 1.64 A1 <br> A1 cso  |
| (b) |  |
|  | Notes |
| (a) | M1 is also scored for $8^{2}=7^{2}+11^{2}-(2 \times 7 \times 11 \cos C)$ or $7^{2}=8^{2}+11^{2}-(2 \times 8 \times 11 \cos C)$ or $\cos C=\frac{7^{2}+11^{2}-8^{2}}{2 \times 7 \times 11} \quad$ or $\quad \cos C=\frac{8^{2}+11^{2}-7^{2}}{2 \times 8 \times 11}$ <br> $1^{\text {st }}$ A1: Rearranged correctly to make $\cos C=\ldots$ and numerically correct (possibly unsimplified). Award A1 for any of $\cos C=\frac{8^{2}+7^{2}-11^{2}}{2 \times 8 \times 7}$ or $\cos C=\frac{-8}{112}$ or $\cos C=-\frac{1}{14}$ or $\cos C=\mathrm{awrt}-0.071$. <br> SC: Also allow $1^{\text {st }} \mathrm{A} 1$ for $112 \cos C=-8$ or equivalent. <br> Also note that the $1^{\text {st }} \mathrm{A} 1$ can be implied for $\hat{C}=$ awrt 1.64 or $\hat{C}=$ awrt $94.1^{\circ}$. <br> Special Case: $\cos C=\frac{1}{14}$ or $\cos C=\frac{11^{2}-8^{2}-7^{2}}{2 \times 8 \times 7}$ scores a SC: M1A0A0. <br> $2^{\text {nd }} \mathrm{A} 1$ : for awrt 1.64 cao <br> Note that $A=0.6876 . . .{ }^{c}$ (or $39.401 . . .{ }^{\circ}$ ), $B=0.8116 . . .{ }^{\text {c }}$ (or 46.503... ${ }^{\circ}$ ) |
| (b) | M1: alternative methods must be fully correct to score the M1. For any (or both) of the M1 or the $1^{\text {st }} \mathrm{A} 1$; their $C$ can either be in degrees or radians. Candidates who use $\cos C=\frac{1}{14}$ to give $C=1.499 \ldots$, can achieve the correct answer of awrt 27.9 in part (b). These candidates will score M1A1A0cso, in part (b). <br> Finding $C=1.499$... in part (a) and achieving awrt 27.9 with no working scores M1A1A0. Otherwise with no working in part (b), awrt 27.9 scores M1A1A1. <br> Special Case: If the candidate gives awrt 27.9 from any of the below then award M1A1A1. $\frac{1}{2}(7 \times 11) \sin \left(0.8116^{c} \text { or } 46.503^{\circ}\right)=\text { awrt } 27.9, \frac{1}{2}(8 \times 11) \sin \left(0.6876 \ldots{ }^{c} \text { or } 39.401 \ldots{ }^{\circ}\right)=\text { awrt } 27.9 .$ <br> Alternative: Hero's Formula: $A=\sqrt{13(13-11)(13-8)(13-7)}=$ awrt 27.9, where M1 is attempt to apply $A=\sqrt{s(s-11)(s-8)(s-7)}$ and the first A1 is for the correct application of the formula. |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| $3 . \quad$ (a) | ar $=750$ and $a r^{4}=-6$ (could be implied from later working in either (a) or (b)). $\begin{aligned} & r^{3}=\frac{-6}{750} \\ & r=-\frac{1}{5} \end{aligned}$ <br> Correct answer from no working, except for special case below gains all three | $\begin{array}{ll}\text { B1 } \\ \text { M1 } \\ \text { A1 } \\ \\ \\ & \text { (3) }\end{array}$ |
| (b) | $\begin{aligned} & a(-0.2)=750 \\ & a\left\{=\frac{750}{-0.2}\right\}=-3750 \end{aligned}$ | M1 <br> A1 ft |
| (c) | Applies $\frac{a}{1-r}$ correctly using both their $a$ and their $\|r\|<1$. Eg. $\frac{-3750}{1--0.2}$ So, $S_{\infty}=-3125$ | $\begin{array}{lr}\text { M1 } & \\ \text { A1 } & \\ & (2) \\ & \text { [7] }\end{array}$ |
|  | Notes |  |
| (a) | B1: for both $a r=750$ and $a r^{4}=-6$ (may be implied from later working in either (a) or (b)). <br> M1: for eliminating $\boldsymbol{a}$ by either dividing $a r^{4}=-6$ by $a r=750$ or dividing ar $=750$ by $a r^{4}=-6$, to achieve an equation in $r^{3}$ or $\frac{1}{r^{3}}$ Note that $r^{4}-r=-\frac{6}{750}$ is M0. <br> Note also that any of $r^{3}=\frac{-6}{750}$ or $r^{3}=\frac{750}{-6}\{=-125\}$ or $\frac{1}{r^{3}}=\frac{-6}{750}$ or $\frac{1}{r^{3}}=\frac{750}{-6}\{=-125\}$ are fine for the award of M1. <br> SC: $a r^{\alpha}=750$ and $a r^{\beta}=-6$ leading to $r^{\delta}=\frac{-6}{750}$ or $r^{\delta}=\frac{750}{-6}\{=-125\}$ <br> or $\frac{1}{r^{\delta}}=\frac{-6}{750}$ or $\frac{1}{r^{\delta}}=\frac{750}{-6}\{=-125\}$ where $\delta=\beta-\alpha$ and $\delta \geq 2$ are fine for the award of M1. SC: $a r^{2}=750$ and $a r^{5}=-6$ leading to $r=-\frac{1}{5}$ scores B0M1A1. |  |
| (b) | M1 for inserting their $r$ into either of their original correct equations of either $a r=750$ or $\{a=\} \frac{750}{r}$ or $a r^{4}=-6$ or $\{a=\} \frac{-6}{r^{4}}$ - in both $\boldsymbol{a}$ and $\boldsymbol{r}$. No slips allowed here for M1. <br> A1 for either $a=-3750$ or $a$ equal to the correct follow through result expressed either as an exact integer, or a fraction in the form $\frac{c}{d}$ where both $c$ and $d$ are integers, or correct to awrt 1 dp . |  |
| (c) | M1 for applying $\frac{a}{1-r}$ correctly (only a slip in substituting $r$ is allowed) using both their $a$ and their $\|r\|<1$. Eg. $\frac{-3750}{1--0.2}$. A1 for -3125 In parts (a) or (b) or (c), the correct answer with no working scores full marks. |  |



| (a) | Notes |
| ---: | :--- |
| B1: for -1 and 5. Note that $(-1,0)$ and $(5,0)$ are acceptable for B1. Also allow |  |
| $(0,-1)$ and $(0,5)$ generously for B1. Note that if a candidate writes down that |  |
| $A:(5,0), B:(-1,0)$, (ie $A$ and $B$ interchanged,) then B0. Also allow values inserted in the |  |
| correct position on the $x$-axis of the graph. |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 5. <br> (a) | $\binom{40}{4}=\frac{40!}{4!b!} ;(1+x)^{n}$ coefficients of $x^{4}$ and $x^{5}$ are $p$ and $q$ respectively. $b=36$ <br> Candidates should usually "identify" two terms as their $p$ and $q$ respectively. | B1 (1) |
| (b) | Term 1: $\left.\begin{array}{c}40 \\ 4\end{array}\right)$ or ${ }^{40} C_{4}$ or $\frac{40!}{4!36!}$ or $\frac{40(39)(38)(37)}{4!}$ or 91390TermAny one of <br> Term 1 or <br> Term 2 <br> correct. <br> (Ignore the <br> label of $p$ <br> and/or $q)$.Hence, $\frac{q}{p}=\frac{658008}{91390}\left\{=\frac{36}{5}=7.2\right\}$ or ${ }^{40} C_{5}$ or $\frac{40!}{5!35!}$ or $\frac{40(39)(38)(37)(36)}{5!}$ or 658008correct.(Ignore thelabel of $p$and/or $q$. | M1 <br> A1 <br> A1 oe cso <br> (3) <br> [4] |

(a) B1: for only $b=36$.
(b) The candidate may expand out their binomial series. At this stage no marks should be awarded until they start to identify either one or both of the terms that they want to focus on. Once they identify their terms then if one out of two of them (ignoring which one is $p$ and which one is $q$ ) is correct then award M1. If both of the terms are identified correctly (ignoring which one is $p$ and which one is $q$ ) then award the first A1.
Term $1=\binom{40}{4} x^{4}$ or ${ }^{40} C_{4}\left(x^{4}\right)$ or $\frac{40!}{4!36!} x^{4}$ or $\frac{40(39)(38)(37)}{4!} x^{4}$ or $91390 x^{4}$,
Term $2=\binom{40}{5} x^{5}$ or ${ }^{40} C_{5}\left(x^{5}\right)$ or $\frac{40!}{5!35!} x^{5}$ or $\frac{40(39)(38)(37)(36)}{5!} x^{5}$ or $658008 x^{5}$
are fine for any (or both) of the first two marks in part (b).
$2^{\text {nd }}$ A1 for stating $\frac{q}{p}$ as $\frac{658008}{91390}$ or equivalent. Note that $\frac{q}{p}$ must be independent of $x$.
Also note that $\frac{36}{5}$ or 7.2 or any equivalent fraction is fine for the $2^{\text {nd }} \mathrm{A} 1$ mark.
SC: If candidate states $\frac{p}{q}=\frac{5}{36}$, then award M1A1A0.
Note that either $\frac{4!36!}{5!35!}$ or $\frac{5!35!}{4!36!}$ would be awarded M1A1.

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| Question <br> Number | Scheme | Marks |
| ---: | :--- | :--- |
| (b) | B1 for using $\frac{1}{2} \times 0.25$ or $\frac{1}{8}$ or equivalent. <br> M1 requires the correct $\{\ldots . .\}$. <br> ordinate plus last $y$-ordinate and the second bracket to be the summation of the remaining $y$ - <br> ordinates in the table. <br> No errors (eg. an omission of a $y$-ordinate or an extra $y$-ordinate or a repeated $y$-ordinate) are <br> allowed in the second bracket and the second bracket must be multiplied by 2 . Only one copying <br> error is allowed here in the $2(0.38+$ their $0.30+$ their 0.24$)$ bracket. <br> A1ft for the correct bracket $\{\ldots . .$.$\} following through candidate’s y$-ordinates found in part (a). <br> A1 for answer of awrt 0.32. <br> Bracketing mistake: Unless the final answer implies that the calculation has been done <br> correctly <br> then award M1A0A0 for either $\frac{1}{2} \times 0.25 \times 0.5+2(0.38+$ their $0.30+$ their 0.24$)+0.2$ <br> (nb: yielding final answer of 2.1025 ) so that the 0.5 is only multiplied by $\frac{1}{2} \times 0.25$ <br> or $\frac{1}{2} \times 0.25 \times(0.5+0.2)+2(0.38+$ their $0.30+$ their 0.24$)$ <br> (nb: yielding final answer of 1.9275$)$ so that the ( $0.5+0.2)$ is multiplied by $\frac{1}{2} \times 0.25$. <br> Need to see trapezium rule - answer only (with no working) gains no marks. <br> Alternative: Separate trapezia may be used, and this can be marked equivalently. (See |  |
| appendix.) |  |  |


| Question Number | Scheme ${ }^{\text {a }}$ ( Marks |
| :---: | :---: |
| 7. | $\begin{aligned} & 3 \sin ^{2} x+7 \sin x=\cos ^{2} x-4 ; 0 \leq x<360^{\circ} \\ & 3 \sin ^{2} x+7 \sin x=\left(1-\sin ^{2} x\right)-4 \\ & 4 \sin ^{2} x+7 \sin x+3=0 \quad \text { AG } \end{aligned}$ |
| (b) | $\left.\begin{array}{lr\|l\|l}(4 \sin x+3)(\sin x+1)\{=0\} & \text { Valid attempt at factorisation } \\ \text { and } \sin x=\ldots\end{array}\right)$ M1 |
|  | Notes |
| (a) | M1 for a correct method to change $\cos ^{2} x$ into $\sin ^{2} x$ (must use $\cos ^{2} x=1-\sin ^{2} x$ ). <br> Note that applying $\cos ^{2} x=\sin ^{2} x-1$, scores M0. <br> A1 for obtaining the printed answer without error (except for implied use of zero.), although the equation at the end of the proof must be $=\mathbf{0}$. Solution just written only as above would score M1A1. |
| (b) | $1^{\text {st }} \mathrm{M} 1$ for a valid attempt at factorisation, can use any variable here, $s, y, x$ or $\sin x$, and an attempt to find at least one of the solutions. <br> Alternatively, using a correct formula for solving the quadratic. Either the formula must be stated correctly or the correct form must be implied by the substitution. <br> $1^{\text {st }} \mathrm{A} 1$ for the two correct values of $\sin x$. If they have used a substitution, a correct value of their $s$ or their $y$ or their $x$. <br> $2^{\text {nd }} \mathrm{M} 1$ for solving $\sin x=-k, 0<k<1$ and realising a solution is either of the form <br> $(180+\|\alpha\|)$ or $(360-\|\alpha\|)$ where $\alpha=\sin ^{-1}(k)$. Note that you cannot access this mark from <br> $\sin x=-1 \Rightarrow x=270$. Note that this mark is dependent upon the $1^{\text {st }}$ M1 mark awarded. <br> $2^{\text {nd }} \mathrm{A} 1$ for both awrt 228.6 and awrt 311.4 <br> B1 for 270 . <br> If there are any EXTRA solutions inside the range $0 \leq x<360^{\circ}$ and the candidate would otherwise score FULL MARKS then withhold the final bA2 mark (the fourth mark in this part of the question). <br> Also ignore EXTRA solutions outside the range $0 \leq x<360^{\circ}$. <br> Working in Radians: Note the answers in radians are $x=3.9896 \ldots, 5.4351 \ldots, 4.7123 \ldots$ <br> If a candidate works in radians then mark part (b) as above awarding the $2^{\text {nd }} \mathrm{A} 1$ for both awrt 4.0 and awrt 5.4 and the B1 for awrt 4.7 or $\frac{3 \pi}{2}$. If the candidate would then score FULL <br> MARKS then withhold the final bA2 mark (the fourth mark in this part of the question.) <br> No working: Award B1 for 270 seen without any working. <br> Award M0A0M1A1 for awrt 228.6 and awrt 311.4 seen without any working. <br> Award M0A0M1A0 for any one of awrt 228.6 or awrt 311.4 seen without any working. |

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| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 8. <br> (a) | Graph of $y=7^{x}, x \in \mathbb{R}$ and solving $7^{2 x}-4\left(7^{x}\right)+3=0$ <br> At least two of the three criteria correct. <br> (See notes below.) <br> All three criteria correct. <br> (See notes below.) | B1  <br> B1  <br>   <br>   <br>   <br>  (2) |
| (b) | Forming a quadratic \{using $\begin{aligned} & y^{2}-4 y+3\{=0\} \\ & \begin{array}{l} \left\{(y-3)(y-1)=0 \text { or }\left(7^{x}-3\right)\left(7^{x}-1\right)=0\right\} \\ \begin{array}{l} y=3, \quad y=1 \quad \text { or } \quad 7^{x}=3,7^{x}=1 \end{array} \\ \left\{7^{x}=3 \Rightarrow\right\} x \log 7=\log 3 \\ \text { or } x=\frac{\log 3}{\log 7} \text { or } x=\log _{7} 3 \end{array} \\ & \begin{array}{l} x=0.5645 \ldots \\ x=0 \end{array} \end{aligned}$ | $\begin{array}{ll}\text { M1 } & \\ \text { A1 } & \\ \text { A1 } & \\ \text { dM1 } & \\ & \\ \text { A1 } & \\ \text { B1 } & \\ & \text { (6) } \\ & {[8]}\end{array}$ |
|  | Notes |  |
| (a) | B1B0: Any two of the following three criteria below correct. <br> B1B1: All three criteria correct. <br> Criteria number 1: Correct shape of curve for $x \geq 0$. <br> Criteria number 2: Correct shape of curve for $x<0$. <br> Criteria number 3: $(0,1)$ stated or 1 marked on the $y$-axis. Allow $(1,0)$ rather than marked in the "correct" place on the $y$-axis. | if |


| Question Number | Scheme $\quad$ Marks |
| :---: | :---: |
| (b) | $1^{\text {st }}$ M1 is an attempt to form a quadratic equation \{using " $y$ " $=7^{x}$. \} <br> $1^{\text {st }} \mathrm{A} 1$ mark is for the correct quadratic equation of $y^{2}-4 y+3\{=0\}$. <br> Can use any variable here, eg: $y, x$ or $7^{x}$. Allow M1A1 for $x^{2}-4 x+3\{=0\}$. <br> Writing $\left(7^{x}\right)^{2}-4\left(7^{x}\right)+3=0$ is also sufficient for M1A1. <br> Award M0A0 for seeing $7^{x^{2}}-4\left(7^{x}\right)+3=0$ by itself without seeing $y^{2}-4 y+3\{=0\}$ or $\left(7^{x}\right)^{2}-4\left(7^{x}\right)+3=0$ <br> $1^{\text {st }} \mathrm{A} 1$ mark for both $y=3$ and $y=1$ or both $7^{x}=3$ and $7^{x}=1$. Do not give this accuracy mark for both $x=3$ and $x=1$, unless these are recovered in later working by candidate applying logarithms on these. <br> Award M1A1A1 for $7^{x}=3$ and $7^{x}=1$ written down with no earlier working. <br> $3^{\text {rd }} \mathrm{dM} 1$ for solving $7^{x}=k, k>0, k \neq 1$ to give either $x \ln 7=\ln k$ or $x=\frac{\ln k}{\ln 7}$ or $x=\log _{7} k$. <br> dM1 is dependent upon the award of M1. <br> $2^{\text {nd }} \mathrm{A} 1$ for 0.565 or awrt 0.56 . B 1 is for the solution of $x=0$, from any working. |

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| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 9. $\begin{array}{rr} \\ & \text { (a) } \\ & \text { (b) }\end{array}$ | $\left.\begin{array}{\|rr} C\left(\frac{-2+8}{2}, \frac{11+1}{2}\right)=C(3,6) \text { AG } & \begin{array}{r} \text { Correct method (no errors) for finding } \\ \text { the mid-point of } A B \text { giving }(3,6) \end{array} \\ (8-3)^{2}+(1-6)^{2} \text { or } \sqrt{(8-3)^{2}+(1-6)^{2}} \text { or } & \begin{array}{r} \text { Applies distance formula in } \\ \text { order to find the radius. } \\ \text { Correct application of } \\ \text { formula. } \end{array} \\ (-2-3)^{2}+(11-6)^{2} \text { or } \sqrt{(-2-3)^{2}+(11-6)^{2}} & (x \pm 3)^{2}+(y \pm 6)^{2}=k, \\ k \text { is a positive value. } \end{array} \quad \begin{array}{rr}  & \left.(x-3)^{2}+(y-6)^{2}=50 \text { (Not } 7.07^{2}\right) \end{array}\right)$ | B1* <br> (1) <br> M1 <br> A1 <br> M1 <br> A1 <br> (4) |
| (c) | $\{$ For $(10,7),\} \quad(10-3)^{2}+(7-6)^{2}=50$, | (1) |
| (d) | $\begin{array}{lr} \text { \{Gradient of radius }\}=\frac{7-6}{10-3} \text { or } \frac{1}{7} & \text { This must be seen in part }(\mathrm{d}) . \\ \text { Gradient of tangent }=\frac{-7}{1} & \text { Using a perpendicular gradient method. } \\ y-7=-7(x-10) & \begin{array}{rl} y-7=(\text { their gradient })(x-10) \\ y=-7 x+77 & y=-7 x+77 \text { or } y=77-7 x \end{array} \end{array}$ | B1 <br> M1 <br> M1 <br> A1 cao <br> (4) <br> [10] |
|  | Notes |  |
| (a) | Alternative method: $C\left(-2+\frac{8--2}{2}, 11+\frac{1-11}{2}\right)$ or $C\left(8+\frac{-2-8}{2}, 1+\frac{11-1}{2}\right)$ |  |
| (b) | You need to be convinced that the candidate is attempting to work out the radius and not the diameter of the circle to award the first M1. Therefore allow $1^{\text {st }} \mathrm{M} 1$ generously for $\frac{(-2-8)^{2}+(11-1)^{2}}{2}$ <br> Award $1^{\text {st }}$ M1A1 for $\frac{(-2-8)^{2}+(11-1)^{2}}{4}$ or $\frac{\sqrt{(-2-8)^{2}+(11-1)^{2}}}{2}$. <br> Correct answer in (b) with no working scores full marks. |  |
| (c) | B1 awarded for correct verification of $(10-3)^{2}+(7-6)^{2}=50$ with no errors. <br> Also to gain this mark candidates need to have the correct equation of the circle either from part (b) or re-attempted in part (c). They cannot verify $(10,7)$ lies on $C$ without a correct $C$. Also a candidate could either substitute $x=10$ in $C$ to find $y=7$ or substitute $y=7$ in $C$ to find $x=10$. |  |

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| Question Number | Scheme $\quad$ Marks |
| :---: | :---: |
| (d) | $2^{\text {nd }} \mathrm{M} 1$ mark also for the complete method of applying $7=($ their gradient)(10) $+c$, finding $c$. Note: Award $2^{\text {nd }} \mathrm{M} 0$ in (d) if their numerical gradient is either 0 or $\infty$. <br> Alternative: For first two marks (differentiation): $2(x-3)+2(y-6) \frac{\mathrm{d} y}{\mathrm{~d} x}=0$ (or equivalent) scores B1. <br> $1^{\text {st }}$ M1 for substituting both $x=10$ and $y=7$ to find a value for $\frac{\mathrm{d} y}{\mathrm{~d} x}$, which must contain both $x$ and $y$. (This M mark can be awarded generously, even if the attempted "differentiation" is not "implicit".) <br> Alternative: $(10-3)(x-3)+(7-6)(y-6)=50$ scores B1M1M1 which leads to $y=-7 x+77$. |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 10. <br> (a) | $V=4 x(5-x)^{2}=4 x\left(25-10 x+x^{2}\right)$ <br> So, $V=100 x-40 x^{2}+4 x^{3}$ <br> $\pm \alpha x \pm \beta x^{2} \pm \gamma x^{3}$, where $\alpha, \beta, \gamma \neq 0$ $V=100 x-40 x^{2}+4 x^{3}$ $\frac{\mathrm{d} V}{\mathrm{~d} x}=100-80 x+12 x^{2}$ <br> At least two of their expanded terms differentiated correctly. $100-80 x+12 x^{2}$ | M1 <br> A1 <br> M1 <br> A1 cao <br> (4) |
| (b) | $\begin{array}{lr} 100-80 x+12 x^{2}=0 & \text { Sets their } \frac{\mathrm{d} V}{\mathrm{~d} x} \text { from part (a) }=0 \\ \left\{\Rightarrow 4\left(3 x^{2}-20 x+25\right)=0 \Rightarrow 4(3 x-5)(x-5)=0\right\} & x=\frac{5}{3} \text { or } x=\text { awrt } 1.67 \\ \{\text { As } 0<x<5\} x=\frac{5}{3} & \text { Substitute candidate's value of } x \\ x=\frac{5}{3}, V=4\left(\frac{5}{3}\right)\left(5-\frac{5}{3}\right)^{2} & \text { where } 0<x<5 \text { into a formula for } V . \\ \text { So, } V=\frac{2000}{27}=74 \frac{2}{27}=74.074 \ldots & \text { Either } \frac{2000}{27} \text { or } 74 \frac{2}{27} \text { or awrt } 74.1 \end{array}$ | M1 <br> A1 <br> dM1 <br> A1 <br> (4) |
| (c) | $\begin{array}{ll} \frac{\mathrm{d}^{2} V}{\mathrm{~d} x^{2}}=-80+24 x & \text { Differentiates their } \frac{\mathrm{d} V}{\mathrm{~d} x} \text { correctly to give } \frac{\mathrm{d}^{2} V}{\mathrm{~d} x^{2}} . \\ \text { When } x=\frac{5}{3}, \frac{\mathrm{~d}^{2} V}{\mathrm{~d} x^{2}}=-80+24\left(\frac{5}{3}\right) & \\ \frac{\mathrm{d}^{2} V}{\mathrm{~d} x^{2}}=-40<0 \Rightarrow V \text { is a maximum } & \frac{\mathrm{d}^{2} V}{\mathrm{~d} x^{2}}=-40 \text { and }<0 \text { or negative and maximum. } \end{array}$ | M1 <br> A1 cso <br> (2) <br> [10] |
|  | Notes |  |
| (a) | $1^{\text {st }} \mathrm{M} 1$ for a three term cubic in the form $\pm \alpha x \pm \beta x^{2} \pm \gamma x^{3}$. <br> Note that an un-combined $\pm \alpha x \pm \lambda x^{2} \pm \mu x^{2} \pm \gamma x^{3}, \alpha, \lambda, \mu, \gamma \neq 0$ is fine for the $1^{\text {st }} \mathrm{M} 1$. $1^{\text {st }} \mathrm{A} 1$ for either $100 x-40 x^{2}+4 x^{3}$ or $100 x-20 x^{2}-20 x^{2}+4 x^{3}$. <br> $2^{\text {nd }}$ M1 for any two of their expanded terms differentiated correctly. NB: If expanded expression is divided by a constant, then the $2^{\text {nd }} \mathrm{M} 1$ can be awarded for at least two terms are correct. <br> Note for un-combined $\pm \lambda x^{2} \pm \mu x^{2}, \pm 2 \lambda x \pm 2 \mu x$ counts as one term differentiated correctly. $2^{\text {nd }}$ A1 for $100-80 x+12 x^{2}$, cao. <br> Note: See appendix for those candidates who apply the product rule of differentiation. |  |


| Question <br> Number | Scheme | Marks |
| ---: | :--- | :---: |
| (b) | Note you can mark parts (b) and (c) together. <br> Ignore the extra solution of $x=5$ (and $V=0$ ). Any extra solutions for $V$ inside found for <br> values inside the range of $x$, then award the final A0. |  |
| (c) | M1 is for their $\frac{\mathrm{d} V}{\mathrm{~d} x}$ differentiated correctly (follow through) to give $\frac{\mathrm{d}^{2} V}{\mathrm{~d} x^{2}}$. <br> A1 for all three of $\frac{\mathrm{d}^{2} V}{\mathrm{~d} x^{2}}=-40$ and $<0$ or negative and maximum. <br> Ignore any second derivative testing on $x=5$ for the final accuracy mark. <br> $\underline{\text { Alternative Method: Gradient Test: M1 for finding the gradient either side of their } x \text {-value }}$ <br> from part (b) where $0<x<5$. A1 for both gradients calculated correctly to the near integer, <br> using $>0$ and $<0$ respectively or a correct sketch and maximum. (See appendix for gradient <br> values.) |  |

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| Question Number | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| Aliter <br> 6 <br> (b) <br> Way 2 | $0.25 \times\left\{\frac{0.5+0.38}{2}+\frac{0.38+0.30}{2}+\frac{0.30+0.24}{2}+\frac{0.24+0.2}{2}\right\}$ <br> which is equivalent to: $\begin{aligned} & \frac{1}{2} \times 0.25 ; \times\{(0.5+0.2)+2(0.38+\text { their } 0.30+\text { their } 0.24)\} \\ & \left\{=\frac{1}{8}(2.54)\right\}=\text { awrt } 0.32 \end{aligned}$ | 0.25 and a divisor of 2 on all terms inside brackets. One of first and last ordinates, two of the middle ordinates inside brackets ignoring the denominator of 2 . Correct expression inside brackets if $\frac{1}{2}$ was to be factorised out. awrt 0.32 | B1 <br> M1 <br> A1 $\sqrt{ }$ <br> A1 <br> (4) |

## edexcel

| Question Number | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Aliter } \\ 10 \quad \text { (a) } \\ \text { Way2 } \end{gathered}$ | Product Rule Method: $\left\{\begin{array}{ll} u=4 x & v=(5-x)^{2} \\ \frac{\mathrm{~d} u}{\mathrm{~d} x}=4 & \frac{\mathrm{~d} v}{\mathrm{~d} x}=2(5-x)^{1}(-1) \end{array}\right\}$ |  |  |
|  | $\frac{\mathrm{d} y}{\mathrm{~d} x}=4(5-x)^{2}+4 x(2)(5-x)^{1}(-1)$ $\frac{\mathrm{d} y}{\mathrm{~d} x}=4(5-x)^{2}-8 x(5-x)$ | $\pm\left(\right.$ their $\left.u^{\prime}\right)(5-x)^{2} \pm(4 x)$ (their $\left.v^{\prime}\right)$ <br> A correct attempt at differentiating any one of either $u$ or $v$ correctly. <br> Both $\frac{\mathrm{d} u}{\mathrm{~d} x}$ and $\frac{\mathrm{d} v}{\mathrm{~d} x}$ correct $4(5-x)^{2}-8 x(5-x)$ | M1 dM1 A1 A1 |
| $\begin{gathered} \text { Aliter } \\ 10 \quad(\mathrm{a}) \\ \text { Way3 } \end{gathered}$ | $\left\{\begin{array}{ll} u=4 x & v=25-10 x+x^{2} \\ \frac{\mathrm{~d} u}{\mathrm{~d} x}=4 & \frac{\mathrm{~d} v}{\mathrm{~d} x}=-10+2 x \end{array}\right\}$ |  | (4) |
|  | $\frac{\mathrm{d} y}{\mathrm{~d} x}=4\left(25-10 x+x^{2}\right)+4 x(-10+2 x)$ | $\pm\left(\right.$ their $\left.u^{\prime}\right)\left(\right.$ their $\left.(5-x)^{2}\right) \pm(4 x)$ (their $\left.v^{\prime}\right)$ <br> A correct attempt at differentiating any one of either $u$ or their $v$ correctly. <br> Both $\frac{\mathrm{d} u}{\mathrm{~d} x}$ and $\frac{\mathrm{d} v}{\mathrm{~d} x}$ correct | M1 <br> dM1 <br> A1 |
|  | $\frac{\mathrm{d} V}{\mathrm{~d} x}=100-80 x+12 x^{2}$ | $100-80 x+12 x^{2}$ |  |
|  | Note: The candidate needs to use a c award the the first M1 mark here. Th method mark awarded. | duct rule method in order for you to thod mark is dependent on the first |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| $$ | Gradient Test Method: $\frac{\mathrm{d} V}{\mathrm{~d} x}=100-80 x+12 x^{2}$ <br> Helpful table! |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 8 (b) | Method of trial and improvement Helpful table: |  |
|  | $x$ $y=7^{2 x}-4\left(7^{x}\right)+3$ <br> 0  |  |
|  | 0 |  |
|  | 0.1 -0.38348 |  |
|  | 0.2 -0.72519 |  |
|  | 0.3 -0.95706 |  |
|  | 0.4 -0.96835 |  |
|  | 0.5 -0.58301 |  |
|  | 0.51 -0.51316 |  |
|  | 0.52 -0.43638 |  |
|  | $0.53-0.3523$ |  |
|  | 0.54 -0.26055 <br> 0.55  |  |
|  | 0.55 |  |
|  | 0.56 -0.05247 |  |
|  | 0.561 -0.04116 |  |
|  | 0.562 -0.02976 |  |
|  | 0.563 -0.01828 |  |
|  | 0.564 |  |
|  | 0.565 0.00497 |  |
|  | 0.57 0.064688 |  |
|  | 0.58 0.19118 |  |
|  | 0.59 0.327466 |  |
|  | 0.6 0.474029 |  |
|  | 0.7 2.62723 |  |
|  | 0.8 6.525565 |  |
|  | 0.9 13.15414 |  |
|  | 1 24 |  |
|  | For a full method of trial and improvement by trialing $\mathrm{f}($ value between 0.1 and 0.5645$)=$ value and f (value between 0.5645 and 1$)=$ value <br> Any one of these values correct to 1 sf or truncated 1 sf. <br> Both of these values correct to 1sf or truncated 1sf. <br> A method to confirm root to 2 dp by finding by trialing <br> $\mathrm{f}($ value between 0.56 and 0.5645$)=$ value and <br> f (value between 0.5645 and 0.565 ) $=$ value <br> Both values correct to 1sf or truncated 1sf and the confirmation that the root is $\begin{aligned} & x=0.56 \text { (only) } \\ & x=0 \end{aligned}$ | M1 |
|  |  | A1 |
|  |  | A1 |
|  |  | M1 |
|  |  | A1 |
|  |  | B1 (6) |
|  Note: If a candidate goes from $7^{x}=3$ with no working to $x=0.5645 . .$. then give <br> M1A1 implied. |  |  |

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## Mark Scheme (Results)

## June 2011

## GCE Core Mathematics C2 (6664) Paper 1

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## EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

1. The total number of marks for the paper is 75 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of $M$ marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod - benefit of doubt
- ft - follow through
- the symbol wifl be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- $\quad$ The second mark is dependent on gaining the first mark


# J une 2011 <br> Core Mathematics C2 6664 <br> Mark Scheme 

\begin{tabular}{|c|c|}
\hline Question Number \& Scheme \({ }_{\text {S }}\) Marks \\
\hline \begin{tabular}{l}
1. \\
(a)
\end{tabular} \& \begin{tabular}{l}
\[
\begin{aligned}
\& \mathrm{f}(\mathrm{x})=2 x^{3}-7 x^{2}-5 x+4 \\
\& \text { Remainder }=f(1)=2-7-5+4=-6 \\
\& \quad=-6
\end{aligned}
\] \\
Attempts \(f(1)\) or \(f(-1)\).
\end{tabular} \\
\hline (b) \& \begin{tabular}{lr|r}
\(\mathrm{f}(-1)=2(-1)^{3}-7(-1)^{2}-5(-1)+4\) \\
and so \((x+1)\) is a factor. \& \(\mathrm{f}(-1)=0\) with no sign or substitution \& M1 \\
A1 \& errors and for conclusion. \& \\
\hline
\end{tabular} \\
\hline (c) \& \begin{tabular}{rl|r|}
\(\mathrm{f}(x)\) \& \(=\{(x+1)\}\left(2 x^{2}-9 x+4\right)\) \\
\& \(=(x+1)(2 x-1)(x-4)\) \& M1 A1 \\
(Note: Ignore the ePEN notation of \((b)\) (should be \((c))\) for the final three marks in this part). \& dM1 A1 \\
\& {\([4]\)} \\
\hline
\end{tabular} \\
\hline (a)
(b)

(c) \& | M1 for attempting either $\mathrm{f}(1)$ or $\mathrm{f}(-1)$. Can be implied. Only one slip permitted. |
| :--- |
| M1 can also be given for an attempt (at least two "subtracting" processes) at long division to give a remainder which is independent of $x$. A1 can be given also for -6 seen at the bottom of long division working. Award A0 for a candidate who finds -6 but then states that the remainder is 6 . |
| Award M1A1 for -6 without any working. |
| M1: attempting only $f(-1)$. A1: must correctly show $f(-1)=0$ and give a conclusion in part (b) only. |
| Note: Stating "hence factor" or "it is a factor" or a "tick" or "QED" is fine for the conclusion. |
| Note also that a conclusion can be implied from a preamble, eg: "If $\mathrm{f}(-1)=0,(x+1)$ is a factor...." |
| Note: Long division scores no marks in part (b). The factor theorem is required. |
| $1^{\text {st }}$ M1: Attempts long division or other method, to obtain ( $2 x^{2} \pm a x \pm b$ ), $a \neq 0$, even with a remainder. |
| Working need not be seen as this could be done "by inspection." ( $2 x^{2} \pm a x \pm b$ ) must be seen in part (c) only. Award $1^{\text {st }}$ M0 if the quadratic factor is clearly found from dividing $\mathrm{f}(x)$ by $(x-1)$. Eg. Some candidates use their $\left(2 x^{2}-5 x-10\right)$ in part (c) found from applying a long division method in part (a). |
| $1^{\text {st }}$ A1: For seeing $\left(2 x^{2}-9 x+4\right)$. |
| $2^{\text {nd }}$ dM1: Factorises a 3 term quadratic. (see rule for factorising a quadratic). This is dependent on the previous method mark being awarded. This mark can also be awarded if the candidate applies the quadratic formula correctly. |
| $2^{\text {nd }}$ A1: is cao and needs all three factors on one line. Ignore following work (such as a solution to a quadratic equation.) |
| Note: Some candidates will go from $\{(x+1)\}\left(2 x^{2}-9 x+4\right)$ to $\{x=-1\}, x=\frac{1}{2}, 4$, and not list all three factors. Award these responses M1A1M1A0. |
| Alternative: $1^{\text {st }}$ M1: For finding either $\mathrm{f}(4)=0$ or $\mathrm{f}\left(\frac{1}{2}\right)=0$. |
| $1^{\text {st }} \mathrm{A} 1$ : A second correct factor of usually $(x-4)$ or $(2 x-1)$ found. Note that any one of the other correct factors found would imply the $1^{\text {st }}$ M1 mark. |
| $2^{\text {nd }} \mathrm{dM} 1$ : For using two known factors to find the third factor, usually $(2 x \pm 1)$. |
| $2^{\text {nd }} \mathrm{A} 1$ for correct answer of $(x+1)(2 x-1)(x-4)$. |
| Alternative: (for the first two marks) |
| $1^{\text {st }}$ M1: Expands $(x+1)\left(2 x^{2}+a x+b\right)$ \{giving $\left.2 x^{3}+(a+2) x^{2}+(b+a) x+b\right\}$ then compare coefficients to find values for $a$ and $b . \quad 1^{\text {st }} \mathrm{A} 1: a=-9, b=4$ |
| Not dealing with a factor of 2: $(x+1)\left(x-\frac{1}{2}\right)(x-4)$ or $(x+1)\left(x-\frac{1}{2}\right)(2 x-8)$ scores M1A1M1A0. |
| Answer only, with one sign error: eg. $(x+1)(2 x+1)(x-4)$ or $(x+1)(2 x-1)(x+4)$ scores |
| M1A1M1A0. (c) Award M1A1M1A1 for Listing all three correct factors with no working. | <br>

\hline
\end{tabular}

| Question Number | Scheme Marks |
| :---: | :---: |
| 2. (a) | $\begin{array}{rlrl} \left\{(3+b x)^{5}\right\} & =(3)^{5}+{ }^{5} \mathrm{C}_{1}(3)^{4}(b \underline{x})+{ }^{5} \mathrm{C}_{2}(3)^{3}(b x)^{2}+\ldots & 243 \text { as a constant term seen. } & \text { B1 } \\ & =243+405 b x+270 b^{2} x^{2}+\ldots & & \begin{array}{l} \text { B } \\ \end{array} \\ & & \left.{ }^{5} \mathrm{C}_{1} \times \ldots \times x\right) \text { or }\left({ }^{5} \mathrm{C}_{2} \times \ldots \times x^{2}\right) & \text { B1 } \\ \text { M1 } \end{array}$ |
| (b) | $\left\{2(\right.$ coeff $x)=$ coeff $\left.x^{2}\right\} \Rightarrow 2(405 b)=270 b^{2}$ Establishes an equation from <br> their coefficients. Condone 2 on <br> the wrong side of the equation. <br> So, $\left\{b=\frac{810}{270} \Rightarrow\right\} b=3$ $b=3$ (Ignore $b=0$, if seen.)A1A1 <br> [2] |
| (a) | The terms can be "listed" rather than added. Ignore any extra terms. <br> $1^{\text {st }} \mathrm{B} 1$ : A constant term of 243 seen. Just writing (3) ${ }^{5}$ is B0. <br> $2^{\text {nd }} \mathrm{B} 1$ : Term must be simplified to $405 b x$ for B 1 . The $x$ is required for this mark. Note $405+b x$ is B 0. <br> M1: For either the $x$ term or the $x^{2}$ term. Requires correct binomial coefficient in any form with the correct power of $x$, but the other part of the coefficient (perhaps including powers of 3 and/or $b$ ) may be wrong or missing. <br> Allow binomial coefficients such as $\binom{5}{2},\left(\frac{5}{2}\right),\binom{5}{1},\left(\frac{5}{1}\right),{ }^{5} \mathrm{C}_{2},{ }^{5} \mathrm{C}_{1}$. <br> A1: For either $270 b^{2} x^{2}$ or $270(b x)^{2}$. (If $270 b x^{2}$ follows $270(b x)^{2}$, isw and allow A1.) <br> Alternative: <br> Note that a factor of $3^{5}$ can be taken out first: $3^{5}\left(1+\frac{b x}{3}\right)^{5}$, but the mark scheme still applies. <br> Ignore subsequent working (isw): Isw if necessary after correct working: e.g. $243+405 b x+270 b^{2} x^{2}+\ldots$ leading to $9+15 b x+10 b^{2} x^{2}+\ldots$ scores B1B1M1A1 isw. <br> Also note that full marks could also be available in part (b), here. <br> Special Case: Candidate writing down the first three terms in descending powers of $x$ usually get $(b x)^{5}+{ }^{5} \mathrm{C}_{4}(3)^{1}(b x)^{4}+{ }^{5} \mathrm{C}_{3}(3)^{2}(b x)^{3}+\ldots=b^{5} x^{5}+15 b^{4} x^{4}+90 b^{3} x^{3}+\ldots$ <br> So award SC: B0B0M1A0 for either $\left({ }^{5} \mathrm{C}_{4} \times \ldots \times x^{4}\right)$ or $\left({ }^{5} \mathrm{C}_{3} \times \ldots \times x^{3}\right)$ <br> M1 for equating 2 times their coefficient of $x$ to the coefficient of $x^{2}$ to get an equation in $b$, or equating their coefficient of $x$ to 2 times that of $x^{2}$, to get an equation in $b$. <br> Allow this M mark even if the equation is trivial, providing their coefficients from part (a) have been used, eg: $2(405 b)=270 b$, but beware $b=3$ from this, which is A0. <br> An equation in $b$ alone is required: <br> e.g. $2(405 b) x=270 b^{2} x^{2} \Rightarrow b=3$ or similar will be Special Case SC: M1A0 (as equation in coefficients only is not seen here). <br> e.g. $2(405 b) x=270 b^{2} x^{2} \Rightarrow 2(405 b)=270 b^{2} \Rightarrow b=3$ will get M1A1 (as coefficients rather than terms have now been considered). <br> Note: Answer of 3 from no working scores M1A0. <br> Note: The mistake $k\left(1+\frac{b x}{3}\right)^{5}, k \neq 243$ would give a maximum of 3 marks: B0B0M1A0, M1A1 <br> Note: For $270 b x^{2}$ in part (a), followed by $2(405 b)=270 b^{2} \Rightarrow b=3$, in part (b), allow recovery M1A1. |

\begin{tabular}{|c|c|}
\hline Question Number \& Scheme $\quad$ Marks <br>
\hline 3. $\begin{array}{r} \\ \\ \text { (a) }\end{array}$ \& $$
\begin{aligned}
& \text { (a) } 5^{x}=10 \text { and (b) } \log _{3}(x-2)=-1 \\
& x=\frac{\log 10}{\log 5} \text { or } x=\log _{5} 10 \\
& x\{=1.430676558 \ldots\}=1.43(3 \mathrm{sf})
\end{aligned}
$$ <br>
\hline (b) \&  <br>
\hline (a)

(b) \& | M1: for $x=\frac{\log 10}{\log 5}$ or $x=\log _{5} 10$. Also allow M1 for $x=\frac{1}{\log 5}$ |
| :--- |
| 1.43 with no working (or any working) scores M1A1 (even if left as $5^{1.43}$ ). |
| Other answers which round to 1.4 with no working score M1A0. |
| Trial \& Improvement Method: M1: For a method of trial and improvement by trialing |
| f (value between 1.4 and 1.43) $=$ Value below 10 and |
| $\mathrm{f}($ value between 1.431 and 1.5) $=$ Value over 10. |
| A1 for 1.43 cao. |
| Note: $x=\log _{10} 5$ by itself is M0; but $x=\log _{10} 5$ followed by $x=1.430676558 \ldots$ is M1. |
| M1: Is for correctly eliminating log out of the equation. |
| Eg 1: $\log _{3}(x-2)=\log _{3}\left(\frac{1}{3}\right) \Rightarrow x-2=\frac{1}{3}$ only gets M1 when the logs are correctly removed. |
| Eg 2: $\log _{3}(x-2)=-\log _{3}(3) \Rightarrow \log _{3}(x-2)+\log _{3}(3)=0 \Rightarrow \log _{3}(3(x-2))=0$ |
| $\Rightarrow 3(x-2)=3^{0}$ only gets M1 when the logs are correctly removed, |
| but $3(x-2)=0$ would score M0. |
| Note: $\log _{3}(x-2)=-1 \Rightarrow \log _{3}\left(\frac{x}{2}\right)=-1 \Rightarrow \frac{x}{2}=3^{-1}$ would score M0 for incorrect use of logs. |
| Alternative: changing base |
| $\frac{\log _{10}(x-2)}{\log _{10} 3}=-1 \Rightarrow \log _{10}(x-2)=-\log _{10} 3 \Rightarrow \log _{10}(x-2)+\log _{10} 3=0$ |
| $\Rightarrow \log _{10} 3(x-2)=0 \Rightarrow 3(x-2)=10^{\circ}$. At this point M1 is scored. |
| A correct answer in (b) without any working scores M1A1. | <br>

\hline
\end{tabular}



Note: Please mark parts (a) and (b) together. Answers only in (a) and/or (b) get full marks. Note in part (a) the marks are now M1A1 and not B1B1 as on ePEN.
M1: for $( \pm 2, \pm 1)$. Otherwise, M1 for an attempt to complete the square eg. $(x \pm 2)^{2} \pm \alpha, \alpha \neq 0$ or $\underline{\underline{(y \pm 1)^{2} \pm \beta}}, \beta \neq 0$. M1A1: Correct answer of $(-2,1)$ stated from any working gets M1A1.
(b) M1: to find the radius using 11 , " 1 " and " 4 ", ie. $r=\sqrt{11 \pm " 1 " \pm " 4 "}$. By applying this method candidates will usually achieve $\sqrt{16}, \sqrt{6}, \sqrt{8}$ or $\sqrt{14}$ and not $16,6,8$ or 14 .
Note: $(x+2)^{2}+(y-1)^{2}=-11-5=-16 \Rightarrow r=\sqrt{16}=4$ should be awarded M0A0.
Alternative: M1 in part (a): For comparing with $x^{2}+y^{2}+2 g x+2 f y+c=0$ to write down centre $(-g,-f)$ directly. Condone sign errors for this M mark. M1 in part (b): For using $r=\sqrt{g^{2}+f^{2}-c}$. Condone sign errors for this method mark.
$(x+2)^{2}+(y-1)^{2}=16 \Rightarrow r=8$ scores M0A0, but $r=\sqrt{16}=8$ scores M1A1 isw.
(c) $\quad 1^{\text {st }} \mathrm{M} 1$ : Putting $x=0$ in either $x^{2}+y^{2}+4 x-2 y-11=0$ or their circle equation usually given in part (a) or part (b). $\quad 1^{\text {st }} \mathrm{A} 1$ for a correct equation in $y$ in any form which can be implied by later working. $2^{\text {nd }}$ M1: See rules for using the formula. Or completing the square on a 3TQ to give $y=a \pm \sqrt{b}$, where $\sqrt{b}$ is a surd, $b \neq$ their 11 and $b>0$. This mark should not be given for an attempt to factorise. $2^{\text {nd }} \mathrm{A} 1$ : Need exact pair in simplified surd form of $\{y=\} 1 \pm 2 \sqrt{3}$. This mark is also cso.
Do not need to see $(0,1+2 \sqrt{3})$ and $(0,1-2 \sqrt{3})$. Allow $2^{\text {nd }}$ A1 for bod $(1+2 \sqrt{3}, 0)$ and $(1-2 \sqrt{3}, 0)$. Any incorrect working in (c) gets penalised the final accuracy mark. So, beware: incorrect $(x-2)^{2}+(y-1)^{2}=16$ leading to $y^{2}-2 y-11=0$ and then $y=1 \pm 2 \sqrt{3}$ scores M1A1M1A0. Special Case for setting $y=0$ : Award SC: M0A0M1A0 for an attempt at applying the formula

$$
x=\frac{-4 \pm \sqrt{(-4)^{2}-4(1)(-11)}}{2(1)}\left\{=\frac{-4 \pm \sqrt{60}}{2}=-2 \pm \sqrt{15}\right\}
$$

Award SC: M0A0M1A0 for completing the square to their equation in $x$ which will usually be $x^{2}+4 x-11=0$ to give $a \pm \sqrt{b}$, where $\sqrt{b}$ is a surd, $b \neq$ their 11 and $b>0$.
Special Case: For a candidate not using $\pm$ but achieving one of the correct answers then award SC: M1A1 M1A0 for one of either $y=1+2 \sqrt{3}$ or $y=1-2 \sqrt{3}$ or $y=1+\sqrt{12}$ or $y=1-\sqrt{12}$.

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 5. (a) | $\frac{1}{2} r^{2} \theta=\frac{1}{2}(6)^{2}\left(\frac{\pi}{3}\right)=6 \pi$ or 18.85 or awrt $18.8(\mathrm{~cm})^{2} \quad$ Using $\frac{1}{2} r^{2} \theta$ (See notes) | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ |
|  |  | [2] |
| (b) | $\sin \left(\frac{\pi}{6}\right)=\frac{r}{6-r} \quad \sin \left(\frac{\pi}{6}\right) \text { or } \sin 30^{\circ}=\frac{r}{6-r}$ | M1 |
|  | $\frac{1}{2}=\frac{r}{6-r} \quad$ Replaces sin by numeric value | dM1 |
|  | $6-r=2 r \Rightarrow r=2 \quad r=2$ | A1 cso <br> [3] |
| (c) | Area $=6 \pi-\pi(2)^{2}=2 \pi$ or awrt $6.3(\mathrm{~cm})^{2} \quad$ their area of sector $-\pi r^{2}$ | M1 |
|  |  | $\begin{array}{r} {[2]} \\ 7 \end{array}$ |
| (a) | M1: Needs $\theta$ in radians for this formula. Candidate could convert to degrees and use the degrees formula. |  |
|  |  |  |
|  | A1: Does not need units. Answer should be either $6 \pi$ or 18.85 or awrt 18.8 |  |
|  | Correct answer with no working is M1A1. <br> This M1A1 can only be awarded in part (a). |  |
| (b) | M1: Also allow $\cos \left(\frac{\pi}{3}\right)$ or $\cos 60^{\circ}=\frac{r}{6-r}$. |  |
|  | $1^{\text {st }}$ M1: Needs correct trigonometry method. Candidates could state $\sin \left(\frac{\pi}{6}\right)=\frac{r}{x}$ and $x+r=6$ or |  |
|  | equivalent in their working to gain this method mark. <br> dM1: Replaces sin by numerical value. $0.009 \ldots=\frac{r}{6-r}$ from working "incorrectly" in degre here for dM1. | es is fine |
|  | A1: For $r=2$ from correct solution only. |  |
|  | Alternative: $1^{\text {st }} \mathrm{M} 1$ for $\frac{r}{O C}=\sin 30$ or $\frac{r}{O C}=\cos 60.2^{\text {nd }} \mathrm{M} 1$ for $O C=2 r$ and then A 1 for $r=2$. | $=2 .$ |
|  | Special Case: If a candidate states an answer of $r=2$ (must be in part (b)) as a guess or from an incorrect method then award SC: M0M0B1. Such a candidate could then go on to score M1A1 in part |  |
| (c) | M1: For "their area of sector - their area of circle", where $r>0$ is ft from their answer to part (b). Allow the method mark if "their area of sector" < "their area of circle". The candidate must show somewhere in their working that they are subtracting the correct way round, even if their answer is negative. <br> Some candidates in part (c) will either use their value of $r$ from part (b) or even introduce a value of $r$ in part (c). You can apply the scheme to award either M0A0 or M1A0 or M1A1 to these candidates. |  |
|  |  |  |
|  |  |  |
|  | Note: Candidates can get M1 by writing "their part (a) answer $-\pi r^{2}$ ", where the radius of the circle is |  |
|  | not substituted. <br> A1: cao - accept exact answer or awrt 6.3 |  |
|  | Correct answer only with no working in (c) gets M1A1 |  |
|  | Beware: The answer in (c) is the same as the arc length of the pendant |  |

\begin{tabular}{|c|c|}
\hline Question Number \& Scheme \(\quad\) Marks \\
\hline \begin{tabular}{l}
6. \\
(a)
\end{tabular} \& \[
\left\{a r=192 \text { and } a r^{2}=144\right\}
\]
\begin{tabular}{lr|r}
\(r=\frac{144}{192}\) \& Attempt to eliminate \(a\). (See notes.) \& M1 \\
\(r=\frac{3}{4}\) or 0.75 \& \(\frac{3}{4}\) or 0.75 \& A1
\end{tabular} \\
\hline (b) \& \begin{tabular}{l|l|l|}
\(a(0.75)=192\) \& M1 \\
\(a\left\{=\frac{192}{0.75}\right\}=256\)
\end{tabular}\(\quad 256\) A1 \(^{\text {[2] }}\)\begin{tabular}{l} 
[2]
\end{tabular} \\
\hline (c) \& \begin{tabular}{cr|l}
\(\mathrm{S}_{\infty}=\frac{256}{1-0.75}\) \& Applies \(\frac{a}{1-r}\) correctly using both their \(a\) and their \(|r|<1\). \& M1 \\
So, \(\left\{\mathrm{S}_{\infty}=\right\} 1024\) \& \& 1024
\end{tabular} A1 cao \(\quad\) [2] \\
\hline (d) \&  \\
\hline (a)

(b) \& | M1: for eliminating $\boldsymbol{a}$ by eg. $192 r=144$ or by either dividing $a r^{2}=144$ by ar $=192$ or dividing $a r=192$ by $a r^{2}=144$, to achieve an equation in $r$ or $\frac{1}{r}$ Note that $r^{2}-r=\frac{144}{192}$ is M0. |
| :--- |
| Note also that any of $r=\frac{144}{192}$ or $r=\frac{192}{144}\left\{=\frac{4}{3}\right\}$ or $\frac{1}{r}=\frac{192}{144}$ or $\frac{1}{r}=\frac{144}{192}$ are fine for the award of M1. Note: A candidate just writing $r=\frac{144}{192}$ with no reference to $a$ can also get the method mark. Note: $a r^{2}=192$ and $a r^{3}=144$ leading to $r=\frac{3}{4}$ scores M1A1. This is because $r$ is the ratio between any two consecutive terms. These candidates, however, will usually be penalised in part (b). M1 for inserting their $r$ into either of the correct equations of either $a r=192$ or $\{a=\} \frac{192}{r}$ or $a r^{2}=144$ or $\{a=\} \frac{144}{r^{2}}$. No slips allowed here for M1. |
| M1: can also be awarded for writing down $144=a\left(\frac{192}{a}\right)^{2}$ |
| A1 for $a=256$ only. Note 256 from any working scores M1A1. |
| Note: Some candidates incorrectly confuse notation to give $r=\frac{4}{3}$ or 1.33 in part (a) (getting M1A0). In part (b), they recover to write $a=192 \times \frac{4}{3}$ for M1 and then 256 for A1. | <br>

\hline
\end{tabular}



\begin{tabular}{|c|c|c|}
\hline Question Number \& Scheme \& Marks \\
\hline \& \begin{tabular}{l}
Note: A similar scheme would apply for T\&I for candidates using their \(a\) and their \(r\). So,.. \(1^{\text {st }} \mathrm{M} 1\) : For attempting to find one of the correct \(\mathrm{S}_{n}\) 's either side (but next to) 1000. \\
\(2^{\text {nd }} \mathrm{M} 1\) : For one of these \(\mathrm{S}_{n}\) 's correct for their \(a\) and their \(r\). (You may need to get your ca out!) \\
\(3^{\text {rd }}\) M1: For attempting to find both of the correct \(S_{n}\) 's either side (but next to) 1000. \\
A1: Cannot be gained for wrong \(a\) and/or \(r\). \\
Trial \& Improvement Cumulative Approach: \\
A similar scheme to T\&I will be applied here: \\
\(1^{\text {st }} \mathrm{M} 1\) : For getting as far as the cumulative sum of 13 terms. \(2^{\text {nd }} \mathrm{M} 1\) : (1) \(\mathrm{S}_{13}=\) awrt 999.7 truncated 999. \(3^{\text {rd }} \mathrm{M} 1\) : For getting as far as the cumulative sum to 14 terms. Also at this s \(\mathrm{S}_{13}<1000\) and \(\mathrm{S}_{14}>1000\). A1: BOTH (1) \(\mathrm{S}_{13}=\) awrt 999.7 or truncated 999 AND (2) \(\mathrm{S}_{14}=\) awrt 1005.8 or truncated 1005 AND \(n=14\). \\
Trial \& Improvement Method: for \((0.75)^{n}<\frac{6}{256}=0.0234375\) \\
\(3^{\text {rd }} \mathrm{M} 1\) : For evidence of examining both \(n=13\) and \(n=14\). \\
Eg: \((0.75)^{13}\{=0.023757 \ldots\}\) and \((0.75)^{14}\{=0.0178179 \ldots\}\) \\
A1: \(n=14\) \\
Any misreads, \(\mathrm{S}_{n}>10000\) etc, please escalate up to your Team Leader.
\end{tabular} \& ulators \\
\hline 7.

(a) \& \begin{tabular}{l}
(a) $3 \sin \left(x+45^{\circ}\right)=2 ; 0 \leq x<360^{\circ}$ <br>
(b) $2 \sin ^{2} x+2=7 \cos x ; 0 \leq x<2 \pi$ $\sin \left(x+45^{\circ}\right)=\frac{2}{3}$, so $\left(x+45^{\circ}\right)=41.8103 \ldots \quad(\alpha=41.8103 \ldots) \quad \sin ^{-1}\left(\frac{2}{3}\right)$ or awrt 41.8 or awrt $0.73^{\text {c }}$ <br>
So, $x+45^{\circ}=\{138.1897 \ldots, 401.8103 \ldots\}$ $x+45^{\circ}=$ either " $180-$ their $\alpha$ " or $" 360^{\circ}+$ their $\alpha$ " ( $\alpha$ could be in radians). <br>
and $x=\{93.1897 \ldots, 356.8103 \ldots\}$ <br>
Either awrt $93.2^{\circ}$ or awrt $356.8^{\circ}$ <br>
Both awrt $93.2^{\circ}$ and awrt $356.8^{\circ}$

 \& 

M1 \& <br>
M1 \& <br>
A1 \& <br>
A1 \& <br>
\& {$[4]$} <br>
\hline
\end{tabular} <br>

\hline (b) \& | $2\left(1-\cos ^{2} x\right)+2=7 \cos x$ | Applies $\sin ^{2} x=1-\cos ^{2} x$ |
| :--- | ---: |
| $2 \cos ^{2} x+7 \cos x-4=0$ | Correct 3 term, $2 \cos ^{2} x+7 \cos x-4\{=0\}$ |
| $(2 \cos x-1)(\cos x+4)\{=0\}, \cos x=\ldots$ | Valid attempt at solving and $\cos x=\ldots$ |
| $\cos x=\frac{1}{2}, \quad\{\cos x=-4\}$ | $\cos x=\frac{1}{2}$ (See notes.) |
| $\left(\beta=\frac{\pi}{3}\right)$ |  |
| $x=\frac{\pi}{3}$ or $1.04719 \ldots$ | Either $\frac{\pi}{3}$ or awrt $1.05^{\text {c }}$ |
| $x=\frac{5 \pi}{3}$ or $5.23598 \ldots{ }^{\text {c }}$ | Either $\frac{5 \pi}{3}$ or awrt $5.24^{\text {c }}$ or $2 \pi-$ their $\beta$ (See notes.) | \& | M1 |
| :--- |
| A1 oe |
| M1 |
| A1 cso |
| B1 |
| B1 ft | <br>

\hline
\end{tabular}

| Question Number | Scheme $\quad$ Marks |
| :---: | :---: |
| (a) | $1^{\text {st }}$ M1: can also be implied for $x=$ awrt -3.2 <br> $2^{\text {nd }}$ M1: for $x+45^{\circ}=$ either " $180-$ their $\alpha$ " or " $360^{\circ}+$ their $\alpha$ ". This can be implied by later working. The candidate's $\alpha$ could also be in radians. <br> Note that this mark is not for $x=$ either " 180 - their $\alpha$ " or " $360^{\circ}+$ their $\alpha$ ". <br> Note: Imply the first two method marks or award M1M1A1 for either awrt $93.2^{\circ}$ or awrt $356.8^{\circ}$. <br> Note: Candidates who apply the following incorrect working of $3 \sin \left(x+45^{\circ}\right)=2$ <br> $\Rightarrow 3(\sin x+\sin 45)=2$, etc will usually score M0M0A0A0. <br> If there are any EXTRA solutions inside the range $0 \leq x<360$ and the candidate would otherwise score FULL MARKS then withhold the final aA2 mark (the final mark in this part of the question). Also ignore EXTRA solutions outside the range $0 \leq x<360$. <br> Working in Radians: Note the answers in radians are $x=$ awrt 1.6, awrt 6.2 <br> If a candidate works in radians then mark part (a) as above awarding the A marks in the same way. If the candidate would then score FULL MARKS then withhold the final aA2 mark (the final mark in this part of the question.) <br> No working: Award M1M1A1A0 for one of awrt $93.2^{\circ}$ or awrt $356.8^{\circ}$ seen without any working. Award M1M1A1A1 for both awrt $93.2^{\circ}$ and awrt $356.8^{\circ}$ seen without any working. Allow benefit of the doubt (FULL MARKS) for final answer of $\sin x\{$ and not $x\}=\{$ awrt 93.2, awrt 356.8\} |


| Question Number | Scheme Marks |
| :---: | :---: |
| (b) | $1^{\text {st }}$ M1: for a correct method to use $\sin ^{2} x=1-\cos ^{2} x$ on the given equation. <br> Give bod if the candidate omits the bracket when substituting for $\sin ^{2} x$, but <br> $2-\cos ^{2} x+2=7 \cos x$, without supporting working, (eg. seeing " $\sin ^{2} x=1-\cos ^{2} x$ ") would score $1^{\text {st }}$ M0. <br> Note that applying $\sin ^{2} x=\cos ^{2} x-1$, scores M0. <br> $1^{\text {st }} \mathrm{A} 1$ : for obtaining either $2 \cos ^{2} x+7 \cos x-4$ or $-2 \cos ^{2} x-7 \cos x+4$. <br> $1^{\text {st }}$ A1: can also awarded for a correct three term equation eg. $2 \cos ^{2} x+7 \cos x=4$ or $2 \cos ^{2} x=4-7 \cos x$ etc. <br> $2^{\text {nd }} \mathrm{M} 1$ : for a valid attempt at factorisation of a quadratic (either 2TQ or 3TQ) in cos, can use any variable here, $c, y, x$ or $\cos x$, and an attempt to find at least one of the solutions. See introduction to the Mark Scheme. Alternatively, using a correct formula for solving the quadratic. Either the formula must be stated correctly or the correct form must be implied by the substitution. <br> $2^{\text {nd }}$ A1: for $\cos x=\frac{1}{2}$, BY A CORRECT SOLUTION ONLY UP TO THIS POINT. Ignore extra answer of $\cos x=-4$, but penalise if candidate states an incorrect result e.g. $\cos x=4$. If they have used a substitution, a correct value of their $c$ or their $y$ or their $x$. <br> Note: $2^{\text {nd }}$ A1 for $\cos x=\frac{1}{2}$ can be implied by later working. <br> $1^{\text {st }} \mathrm{B} 1$ : for either $\frac{\pi}{3}$ or awrt $1.05^{\text {c }}$ <br> $2^{\text {nd }} \mathrm{B} 1$ : for either $\frac{5 \pi}{3}$ or awrt $5.24^{\text {c }}$ or can be ft from $2 \pi$ - their $\beta$ or $360^{\circ}$ - their $\beta$ where <br> $\beta=\cos ^{-1}(k)$, such that $0<k<1$ or $-1<k<0$, but $k \neq 0, k \neq 1$ or $k \neq-1$. <br> If there are any EXTRA solutions inside the range $0 \leq x<2 \pi$ and the candidate would otherwise score FULL MARKS then withhold the final bB2 mark (the final mark in this part of the question). Also ignore EXTRA solutions outside the range $0 \leq x<2 \pi$. <br> Working in Degrees: Note the answers in degrees are $x=60,300$ <br> If a candidate works in degrees then mark part (b) as above awarding the B marks in the same way. If the candidate would then score FULL MARKS then withhold the final bB2 mark (the final mark in this part of the question.) |

Answers from no working:
$x=\frac{\pi}{3}$ and $x=\frac{5 \pi}{3}$ scores M0A0M0A0B1B1,
$x=60$ and $x=300$ scores M0A0M0A0B1B0,
$x=\frac{\pi}{3}$ ONLY or $x=60$ ONLY scores M0A0M0A0B1B0,
$x=\frac{5 \pi}{3}$ ONLY or $x=120$ ONLY scores M0A0M0A0B0B1.
No working: You cannot apply the ft in the B1ft if the answers are given with NO working.
Eg: $x=\frac{\pi}{5}$ and $x=\frac{9 \pi}{3}$ FROM NO WORKING scores M0A0M0A0B0B0.
For candidates using trial \& improvement, please forward these to your Team Leader.

\begin{tabular}{|c|c|}
\hline Question Number \& Scheme ${ }^{\text {S }}$ <br>
\hline 8. \& $$
\begin{array}{rr|l}
\{V=\} 2 x^{2} y=81 & 2 x^{2} y=81 \\
\{L=2(2 x+x+2 x+x)+4 y \Rightarrow L=12 x+4 y\} & \text { B1 oe } \\
y=\frac{81}{2 x^{2}} \Rightarrow L=12 x+4\left(\frac{81}{2 x^{2}}\right) & \begin{array}{r}
\text { Making } y \text { the subject of their } \\
\text { expression and substitute this } \\
\text { into the correct } L \text { formula. }
\end{array} \\
\text { So, } L=12 x+\frac{162}{x^{2}} \text { AG } & \text { Correct solution only. AG. }
\end{array} \text { A1 cso }
$$ <br>
\hline (b) \&  <br>
\hline (c) \& $\{$ For $x=3\}, \frac{\mathrm{d}^{2} L}{\mathrm{~d} x^{2}}=\frac{972}{x^{4}}>0 \Rightarrow$ Minimum $\quad \begin{aligned} & \text { Correct } \mathrm{ft} L^{\prime \prime} \text { and considering sign. } \\ & \begin{array}{l}\text { M1 } \\ \\ \frac{972}{x^{4}} \text { and }>0 \text { and conclusion. }\end{array} \\ & \text { A1 } \\ & \text { [2] } \\ & \text { 11 }\end{aligned}$ <br>
\hline (a)
(b)

(c) \& | B1: For any correct form of $2 x^{2} y=81$. (may be unsimplified). Note that $2 x^{3}=81$ is B0. Otherwise, candidates can use any symbol or letter in place of $y$. |
| :--- |
| M1: Making $y$ the subject of their formula and substituting this into a correct expression for $L$. |
| A1: Correct solution only. Note that the answer is given. |
| Note you can mark parts (b) and (c) together. |
| $2^{\text {nd }}$ M1: Setting their $\frac{\mathrm{d} L}{\mathrm{~d} x}=0$ and "candidate's ft correct power of $x=$ a value". The power of $x$ must be consistent with their differentiation. If inequalities are used this mark cannot be gained until candidate states value of $x$ or $L$ from their $x$ without inequalities. |
| $L^{\prime}=0$ can be implied by $12=\frac{324}{x^{3}}$. |
| $2^{\text {nd }} \mathrm{A} 1: x^{3}=27 \Rightarrow x= \pm 3$ scores A0. |
| $2^{\text {nd }} \mathrm{A} 1$ : can be given for no value of $x$ given but followed through by correct working leading to $L=54$. |
| $3^{\text {rd }}$ M1: Note that this method mark is dependent upon the two previous method marks being awarded. |
| M1: for attempting correct ft second derivative and considering its sign. |
| A1: Correct second derivative of $\frac{972}{x^{4}}$ (need not be simplified) and a valid reason (e.g. $>0$ ), and conclusion. Need to conclude minimum (allow $x$ and not $L$ is a minimum) or indicate by a tick that it is a minimum. The actual value of the second derivative, if found, can be ignored, although substituting their $L$ and not $x$ into $L^{\prime \prime}$ is A0. Note: 2 marks can be scored from a wrong value of $x$, no value of $x$ found or from not substituting in the value of their $x$ into $L^{\prime \prime}$. |
| Gradient test or testing values either side of their $x$ scores M0A0 in part (c). |
| Throughout this question allow confused notation such as $\frac{\mathrm{d} y}{\mathrm{~d} x}$ for $\frac{\mathrm{d} L}{\mathrm{~d} x}$. | <br>

\hline
\end{tabular}

## edexcel

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 9. <br> (a) | $\begin{aligned} & \text { Curve: } y=-x^{2}+2 x+24 \text {, Line: } y=x+4 \\ & \{\text { Curve }=\text { Line }\} \Rightarrow-x^{2}+2 x+24=x+4 \\ & x^{2}-x-20\{=0\} \Rightarrow(x-5)(x+4)\{=0\} \Rightarrow x=\ldots . . \end{aligned}$ <br> So, $x=5,-4$ <br> So corresponding $y$-values are $y=9$ and $y=0$. <br> Eliminating $y$ correctly. <br> Attempt to solve a resulting quadratic to give $x=$ their values. <br> Both $x=5$ and $x=-4$. <br> See notes below. | $\begin{array}{lr} \hline \text { B1 } & \\ \text { M1 } & \\ \text { A1 } & \\ \text { B1ft } & {[4]} \\ \hline \end{array}$ |
| (b) | $\begin{aligned} & \left\{\int\left(-x^{2}+2 x+24\right) \mathrm{d} x\right\}=-\frac{x^{3}}{3}+\frac{2 x^{2}}{2}+24 x\left\{+c \quad \begin{array}{r} \text { M1: } x^{n} \rightarrow x^{n+1} \text { for any one term. } \\ 1^{\text {st }} \text { A1 at least two out of three terms. } \\ 2^{\text {nd }} \mathrm{A} 1 \text { for correct answer. } \end{array}\right. \\ & {\left[-\frac{x^{3}}{3}+\frac{2 x^{2}}{2}+24 x\right]_{-4}^{5}=(\ldots \ldots . .)-(\ldots \ldots) \quad \begin{array}{r} \text { Substitutes } 5 \text { and }-4 \text { (or their limits from } \\ \text { part(a)) into an "integrated function" and } \\ \text { subtracts, either way round. } \end{array}} \\ & \left\{\left(-\frac{125}{3}+25+120\right)-\left(\frac{64}{3}+16-96\right)=\left(103 \frac{1}{3}\right)-\left(-58 \frac{2}{3}\right)=162\right\} \end{aligned} \begin{aligned} & \text { Are of } \Delta=\frac{1}{2}(9)(9)=40.5 \quad \text { Uses correct method for finding area of triangle. } \\ & \text { So area of } R \text { is } 162-40.5=121.5 \end{aligned}$ | M1A1A1 <br> dM1 <br> M1 <br> M1 <br> A1 oe cao |


| Question Number | Scheme ${ }^{\text {a }}$ Marks |
| :---: | :---: |
| (a) (b) | $1^{\text {st }} \mathrm{B} 1$ : For correctly eliminating either $x$ or $y$. Candidates will usually write $-x^{2}+2 x+24=x+4$. This mark can be implied by the resulting quadratic. <br> M1: For solving their quadratic (which must be different to $-x^{2}+2 x+24$ ) to give $x=\ldots$ See introduction for Method mark for solving a 3TQ. It must result from some attempt to eliminate one of the variables. <br> A1: For both $x=5$ and $x=-4$. <br> $2^{\text {nd }}$ B1ft: For correctly substituting their values of $x$ in equation of line or parabola to give both correct ft $y$-values. (You may have to get your calculators out if they substitute their $x$ into $y=-x^{2}+2 x+24$ ). <br> Note: For $x=5,-4 \Rightarrow y=9$ and $y=0 \Rightarrow$ eg. $(-4,9)$ and $(5,0)$, award B1 isw. <br> If the candidate gives additional answers to $(-4,0)$ and $(5,9)$, then withhold the final B1 mark. <br> Special Case: Award SC: B0M0A0B1 for $\{A\}(-4,0)$. You may see this point marked on the diagram. Note: SC: B0M0A0B1 for solving $0=-x^{2}+2 x+24$ to give $\{A\}(-4,0)$ and/or $(6,10)$. <br> Note: Do not give marks for working in part (b) which would be creditable in part (a). $1^{\text {st }} \mathrm{M} 1$ for an attempt to integrate meaning that $x^{n} \rightarrow x^{n+1}$ for at least one of the terms. Note that $24 \rightarrow 24 x$ is sufficient for M1. <br> $1^{\text {st }} \mathrm{A} 1$ at least two out of three terms correctly integrated. <br> $2^{\text {nd }} \mathrm{A} 1$ for correct integration only and no follow through. Ignore the use of a ' $+c^{\prime}$ '. <br> $2^{\text {nd }}$ M1: Note that this method mark is dependent upon the award of the first M1 mark in part (b). Substitutes 5 and -4 (and not 4 if the candidate has stated $x=-4$ in part (a).) (or the limits the candidate has found from part(a)) into an "integrated function" and subtracts, either way round. Allow one slip! <br> $3^{\text {rd }}$ M1: Area of triangle $=\frac{1}{2}$ (their $x_{2}$ - their $x_{1}$ )(their $y_{2}$ ) or Area of triangle $=\int_{x_{1}}^{x_{2}} x+4\{\mathrm{~d} x\}$. <br> Where $x_{1}=$ their $-4, x_{2}=$ their 5 and $y_{2}=$ their $y$ usually found in part (a). <br> $4^{\text {th }}$ M1: Area under curve - Area under triangle, where both Area under curve $>0$ and Area under triangle > 0 and Area under curve > Area under triangle. <br> $3^{\text {rd }}$ A1: 121.5 or $\frac{243}{2}$ oe cao. |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Aliter 9.(b) Way 2 | Curve: $y=-x^{2}+2 x+24$, Line: $y=x+4$ <br> $3^{\text {rd }}$ M1: Uses integral of $(x+4)$ with $\begin{aligned} & \text { Area of } R=\int_{-4}^{5}\left(-x^{2}+2 x+24\right)-(x+4) \mathrm{d} x \\ & =-\frac{x^{3}}{3}+\frac{x^{2}}{2}+20 x\{+c\} \quad \begin{array}{c} \text { M: } x^{n} \end{array} \\ & {\left[-\frac{x^{3}}{3}+\frac{x^{2}}{2}+20 x\right]_{-4}^{5}=(\ldots \ldots)-(\ldots \ldots)} \\ & \left\{\left(-\frac{125}{3}+\frac{25}{2}+100\right)-\left(\frac{64}{3}+8-80\right)=\left(70 \frac{5}{6}\right)-\left(-50 \frac{2}{3}\right)\right\} \end{aligned}$ $\text { Substitutes } 5 \text { and }-4 \text { (or their limits from }$ part(a)) into an "integrated function" and subtracts, either way round. <br> See above working to decide to award $3^{\text {rd }}$ M1 mark here: See above working to decide to award $4^{\text {th }}$ M1 mark here: <br> So area of $R$ is $=121.5$ | M1 <br> A1ft <br> A1 <br> dM1 <br> M1 <br> M1 <br> A1 oe cao <br> [7] <br> 11 |

(b) $\quad 1^{\text {st }} \mathrm{M} 1$ for an attempt to integrate meaning that $x^{n} \rightarrow x^{n+1}$ for at least one of the terms. Note that $20 \rightarrow 20 x$ is sufficient for M1.
$1^{\text {st }} \mathrm{A} 1$ at least two out of three terms correctly ft . Note this accuracy mark is ft in Way 2.
$2^{\text {nd }} \mathrm{A} 1$ for correct integration only and no follow through. Ignore the use of a $+c c^{\prime}$.
Allow $2^{\text {nd }} \mathrm{A} 1$ also for $-\frac{x^{3}}{3}+\frac{2 x^{2}}{2}+24 x-\left(\frac{x^{2}}{2}+4 x\right)$. Note that $\frac{2 x^{2}}{2}-\frac{x^{2}}{2}$ or $24 x-4 x$ only counts as one integrated term for the $1^{\text {st }} \mathrm{A} 1$ mark. Do not allow any extra terms for the $2^{\text {nd }} \mathrm{A} 1$ mark. $2^{\text {nd }}$ M1: Note that this method mark is dependent upon the award of the first M1 mark in part (b).
Substitutes 5 and -4 (and not 4 if the candidate has stated $x=-4$ in part (a).) (or the limits the candidate has found from part(a)) into an "integrated function" and subtracts, either way round. Allow one slip!
$3^{\text {rd }} \mathrm{M} 1$ : Uses the integral of $(x+4)$ with correct ft limits of their $x_{1}$ and their $x_{2}$ (usually found in part (a)) $\left\{\right.$ where $\left(x_{1}, y_{1}\right)=(-4,0)$ and $\left(x_{2}, y_{2}\right)=(5,9)$. $\}$ This mark is usually found in the first line of the candidate's working in part (b).
$4^{\text {th }}$ M1: Uses "curve" - "line" function with correct ft (usually found in part (a)) limits. Subtraction must be correct way round. This mark is usually found in the first line of the candidate's working in part (b).
Allow $\int_{-4}^{5}\left(-x^{2}+2 x+24\right)-x+4\{\mathrm{~d} x\}$ for this method mark.
$3^{\text {rd }} \mathrm{A} 1$ : 121.5 oe cao.

## Note: SPECIAL CASE for this alternative method

Area of $R=\int_{-4}^{5}\left(x^{2}-x-20\right) \mathrm{d} x=\left[\frac{x^{3}}{3}-\frac{x^{2}}{2}-20 x\right]_{-4}^{5}=\left(\frac{125}{3}-\frac{25}{2}-100\right)-\left(-\frac{64}{3}-8+80\right)$
The working so far would score SPEICAL CASE M1A1A1M1M1M0A0.
The candidate may then go on to state that $=\left(-70 \frac{5}{6}\right)-\left(50 \frac{2}{3}\right)=-\frac{243}{2}$
If the candidate then multiplies their answer by -1 then they would gain the $4^{\text {th }} \mathrm{M} 1$ and 121.5 would gain the final A1 mark.

## edexcel

| Question <br> Number | Scheme Marks |
| :---: | :---: |
| Aliter <br> 9. (a) <br> Way 2 |  |
|  | $2^{\text {nd }}$ B1ft: For correctly substituting their values of $y$ in equation of line or parabola to give both correct ft $x$-values. |
| 9. (b) | Alternative Methods for obtaining the M1 mark for use of limits: <br> There are two alternative methods can candidates can apply for finding "162". <br> Alternative 1: $\begin{aligned} & \int_{-4}^{0}\left(-x^{2}+2 x+24\right) \mathrm{d} x+\int_{0}^{5}\left(-x^{2}+2 x+24\right) \mathrm{d} x \\ = & {\left[-\frac{x^{3}}{3}+\frac{2 x^{2}}{2}+24 x\right]_{-4}^{0}+\left[-\frac{x^{3}}{3}+\frac{2 x^{2}}{2}+24 x\right]_{0}^{5} } \\ = & (0)-\left(\frac{64}{3}+16-96\right)+\left(-\frac{125}{3}+25+120\right)-(0) \\ = & \left(103 \frac{1}{3}\right)-\left(-58 \frac{2}{3}\right)=162 \end{aligned}$ <br> Alternative 2: $\begin{aligned} & \int_{-4}^{6}\left(-x^{2}+2 x+24\right) \mathrm{d} x-\int_{5}^{6}\left(-x^{2}+2 x+24\right) \mathrm{d} x \\ = & {\left[-\frac{x^{3}}{3}+\frac{2 x^{2}}{2}+24 x\right]_{-4}^{6}-\left[-\frac{x^{3}}{3}+\frac{2 x^{2}}{2}+24 x\right]_{5}^{6} } \\ = & \left\{\left(-\frac{216}{3}+36+144\right)-\left(\frac{64}{3}+16-96\right)\right\}-\left\{\left(-\frac{216}{3}+36+144\right)-\left(-\frac{125}{3}+25+120\right)\right\} \\ = & \left\{(108)-\left(-58 \frac{2}{3}\right)\right\}-\left\{(108)-\left(103 \frac{1}{3}\right)\right\} \\ = & \left(166 \frac{2}{3}\right)-\left(4 \frac{2}{3}\right)=162 \end{aligned}$ |

## Appendix

## List of Abbreviations

- dM1 denotes a method mark which is dependent upon the award of the previous method mark.
- ft or $\sqrt{ }$ denotes "follow through"
- cao denotes "correct answer only"
- aef denotes "any equivalent form"
- cso denotes "correct solution only"
- AG or * denotes "answer given" (in the question paper.)
- awrt denotes "anything that rounds to"
- aliter denotes "alternative methods"


## Extra Solutions

If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

| Question <br> Number | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| Aliter <br> 4. (c) <br> Way 2 | $(x+2)^{2}+(y-1)^{2}=16$, centre $\left(x_{1}, y_{1}\right)=(-2,1)$ and radius $r=4$. |  | M1 <br> A1 aef |
|  | $d_{1}=\sqrt{4^{2}-2^{2}}=\sqrt{12}$ | $\begin{array}{r} \text { Applying } \sqrt{\text { their } r^{2}-\mid \text { their }\left.x_{1}\right\|^{2}} \\ \sqrt{12} \end{array}$ |  |
|  | Hence, $y=1 \pm \sqrt{12}$ | Applies $y=$ their $y_{1} \pm$ their $d$ |  |
|  | So, $y=1 \pm 2 \sqrt{3}$ | $1 \pm 2 \sqrt{3}$ | A1 cao cso |

Special Case: Award Final SC: M1A1 M1A0 if candidate achieves any one of either $y=1+2 \sqrt{3}$ or $y=1-2 \sqrt{3}$ or $y=1+\sqrt{12}$ or $y=1-\sqrt{12}$.

| Aliter <br> 8. (a) | $2 x^{2}\left(\frac{L-12 x}{4}\right)=81$ | $2 x^{2}\left(\frac{L-12 x}{4}\right)=81$ | B1 oe |
| :---: | :--- | ---: | :--- |
| Way 2 | $\Rightarrow x^{2}(L-12 x)=162 \Rightarrow L=12 x+\frac{162}{x^{2}}$ | Rearranges their equation to make $y$ the subject. | M1 |
|  |  | Correct solution only. AG. | A1 cso |

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Core Mathematics 2 (6664)

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## SOME GENERAL PRINCIPLES FOR C2 MARKING

(But the particular mark scheme always takes precedence)

## Method mark for solving 3 term quadratic:

1. Factorisation

$$
\begin{aligned}
& \left(x^{2}+b x+c\right)=(x+p)(x+q), \text { where }|p q|=|c|, \quad \text { leading to } \mathrm{x}=\ldots \\
& \left(a x^{2}+b x+c\right)=(m x+p)(n x+q), \text { where }|p q|=|c| \text { and }|m n|=|a|, \quad \text { leading to } \mathrm{x}=\ldots
\end{aligned}
$$

2. Formula

Attempt to use correct formula (with values for $a, b$ and $c$ ).
3. Completing the square

Solving $x^{2}+b x+c=0: \quad\left(x \pm \frac{b}{2}\right)^{2} \pm q \pm c=0, \quad q \neq 0, \quad$ leading to $x=\ldots$

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.
Normal marking procedure is as follows:
Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values (but refer to the mark scheme first... the application of this principle may vary). Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but will be lost if there is any mistake in the working.

## Equation of a straight line

Apply the following conditions to the M mark for the equation of a line through $(a, b)$ : If the a and b are the wrong way round the M mark can still be given if a correct formula is seen, (e.g. $\left.y-y_{1}=m\left(x-x_{1}\right)\right)$ otherwise M0.

If $(\mathrm{a}, \mathrm{b})$ is substituted into $y=m x+c$ to find c , the M mark is for attempting this.

## Answers without working

The rubric says that these may gain no credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required. Most candidates do show working, but there are occasional awkward cases and if the mark scheme does not cover this, please contact your team leader for advice.

## Misreads

A misread must be consistent for the whole question to be interpreted as such.
These are not common. In clear cases, please deduct the first 2 A (or B) marks which would have been lost by following the scheme. (Note that 2 marks is the maximum misread penalty, but that misreads which alter the nature or difficulty of the question cannot be treated so generously and it will usually be necessary here to follow the scheme as written).
Sometimes following the scheme as written is more generous to the candidate than applying the misread rule, so in this case use the scheme as written. If in doubt, send the response to Review.

## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

1. The total number of marks for the paper is 75 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of $M$ marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- $\square$ The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected. If you are using the annotation facility on ePEN, indicate this action by 'MR' in the body of the script.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.
8. Marks for each question are scored by clicking in the marking grids that appear below each student response on ePEN. The maximum mark allocation for each question/part question(item) is set out in the marking grid and you should allocate a score of ' 0 ' or ' 1 ' for each mark, or "trait", as shown:

|  | 0 | 1 |
| :---: | ---: | ---: |
| aM |  | $\bullet$ |
| aA | $\bullet$ |  |
| bM 1 |  | $\bullet$ |
| $\mathrm{bA1}$ | $\bullet$ |  |
| bB | $\bullet$ |  |
| bM 2 |  | $\bullet$ |
| bA 2 |  | $\bullet$ |

9. Be careful when scoring a response that is either all correct or all incorrect. It is very easy to click down the ' 0 ' column when it was meant to be ' 1 ' and all correct.


| Question <br> number | Scheme | Marks |
| :---: | :--- | :--- |
| $\mathbf{2}$ | The equation of the circle is $(x+1)^{2}+(y-7)^{2}=\left(r^{2}\right)$ <br> The radius of the circle is $\sqrt{(-1)^{2}+7^{2}}=\sqrt{50}$ or $5 \sqrt{2}$ or $r^{2}=50$ <br> So $(x+1)^{2}+(y-7)^{2}=50$ or equivalent | M1 A1 |
|  | M1 <br> Notes <br> M1 is for Pythagoras or substitution into equation of circle to give $r$ or $r^{2}$ <br> Giving this value as diameter is M0 <br> A1, cao for cartesian equation with numerical values but allow $(\sqrt{ } 50)^{2}$ or $(5 \sqrt{2})^{2}$ or any exact <br> equivalent <br> A correct answer implies a correct method - so answer given with no working earns all four <br> marks for this question. |  |
| Alternative <br> method | Equation of circle is $x^{2}+y^{2} \pm 2 x \pm 14 y+c=0$ <br> Equation of circle is $x^{2}+y^{2}+2 x-14 y+c=0$ <br> Uses $(0,0)$ to give $c=0$, or finds $r=\sqrt{(-1)^{2}+7^{2}}=\sqrt{50}$ or $5 \sqrt{2}$ or $r^{2}=50$ <br> So $x^{2}+y^{2}+2 x-14 y=0$ or equivalent | M1 |

\begin{tabular}{|c|c|}
\hline Question number \& Scheme ${ }^{\text {S }}$ <br>
\hline 3 (a).

(b) \&  <br>

\hline $$
\begin{aligned}
& \text { Alternative } \\
& \text { for (b) } \\
& \text { Special case }
\end{aligned}
$$ \& Starts again and expands $(1+0.025)^{8}$ to

$$
\begin{aligned}
& 1+8 \times 0.025+\frac{8 \times 7}{2}(0.025)^{2}+\frac{8 \times 7 \times 6}{2 \times 3}(0.025)^{3},=1.2184 \\
& (\text { Or } 1+1 / 5+7 / 400+7 / 8000=1.2184)
\end{aligned}
$$ <br>

\hline Notes \& | (a) B1 must be simplified |
| :--- |
| The method mark (M1) is awarded for an attempt at Binomial to get the third and/or fourth term - need correct binomial coefficient combined with correct power of $x$. Ignore bracket errors or errors in powers of 4 . Accept any notation for ${ }^{8} C_{2}$ and ${ }^{8} C_{3}$, e.g. $\binom{8}{2}$ and $\binom{8}{3}$ (unsimplified) or 28 and 56 from Pascal's triangle. (The terms may be listed without + signs) |
| First A1 is for two completely correct unsimplified terms |
| A1 needs the fully simplified $\frac{7}{4} x^{2}$ and $\frac{7}{8} x^{3}$. |
| (b) B1 - states or uses $x=0.1$ or $\frac{x}{4}=\frac{1}{40}$ |
| M1 for substituting their value of $x(0<x<1)$ into expansion |
| (e.g. 0.1 (correct) or $0.01,0.00625$ or even 0.025 but not 1 nor 1.025 which would earn M0) |
| A1 Should be answer printed cao (not answers which round to) and should follow correct work. |
| Answer with no working at all is B0, M0, A0 |
| States 0.1 then just writes down answer is B1 M0A0 | <br>

\hline
\end{tabular}

| Question number | Scheme ${ }^{\text {a }}$ Marks |
| :---: | :---: |
| 4. (a) <br> (b) | $\log _{3} 3 x^{2}=\log _{3} 3+\log _{3} x^{2}$ or $\log y-\log x^{2}=\log 3$ or B1 <br> $\log y-\log 3=\log x^{2}$ B1  <br> $\log _{3} x^{2}=2 \log _{3} x$ B1  <br> Using $\log _{3} 3=1$ (3)  <br> $3 x^{2}=28 x-9$ M1  <br> Solves $3 x^{2}-28 x+9=0$ to give $x=\frac{1}{3}$ or $x=9$ M1 A1 <br>   (3) |
| Notes (a) <br> (b) | B1 for correct use of addition rule (or correct use of subtraction rule) <br> B1: replacing $\log x^{2}$ by $2 \log x \quad-$ not $\log 3 x^{2}$ by $2 \log 3 x$ this is B0 <br> These first two B marks are often earned in the first line of working <br> B1. for replacing $\log 3$ by 1 (or use of $3^{1}=3$ ) <br> If candidate has been awarded 3 marks and their proof includes an error or omission of reference to $\log y$ withhold the last mark. <br> So just B1 B1 B0 <br> These marks must be awarded for work in part (a) only <br> M1 for removing logs to get an equation in $x$ - statement in scheme is sufficient. This needs to be accurate without any errors seen in part (b). <br> M1 for attempting to solve three term quadratic to give $x=$ (see notes on marking quadratics) <br> A1 for the two correct answers - this depends on second M mark only. <br> Candidates often begin again in part (b) and do not use part (a). <br> If such candidates make errors in log work in part (b) they score first M0. The second $\mathbf{M}$ and the <br> A are earned as before. It is possible to get M0M1A1 or M0M1A0. |
| Alternative to (b) using $y$ | Eliminates $x$ to give $3 y^{2}-730 y+243=0$ with no errors is M1 Solves quadratic to find $y$, then uses values to find $x$ M1 A1 as before <br> See extra sheet with examples illustrating the scheme. |




| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 7 (a) | $r \theta=6 \times 0.95,=5.7 \quad(\mathrm{~cm})$ | M1, A1 |
| (b) | $\frac{1}{2} r^{2} \theta=\frac{1}{2} \times 6^{2} \times 0.95,=17.1\left(\mathrm{~cm}^{2}\right)$ | M1, A1 <br> (2) |
| (c) | Let $A D=x$ then $\frac{x}{\sin 0.95}=\frac{6}{\sin 1.24}$ so $x=5.16$ | M1 A1 |
|  | OR $\quad x=3 / \cos 0.95$ OR so $x=3 / \sin 0.62$ so $x=5.16 \quad *$ | (2) |
| (d) | $\begin{aligned} & \text { OR } x^{2}=6^{2}+x^{2}-12 x \cos 0.95 \text { leading to } x= \\ & \text { Perimeter }=‘^{\prime} 5.7 \text { ' so } x=5.16+6-5.16=\text { " } 11.7 \text { " } \quad \text { or } 6+\text { their } 5.7 \end{aligned}$ | M1A1 ft <br> (2) |
| (e) | $\begin{aligned} & \text { Area of triangle } A B D=\frac{1}{2} \times 6 \times 5.16 \times \sin 0.95=12.6 \text { or } \\ & \frac{1}{2} \times 6 \times 3 \times \tan 0.95=12.6\left(1 / 2 \text { base } \mathrm{x} \text { height) or } \frac{1}{2} \times 5.16 \times 5.16 \times \sin 1.24=12.6\right. \\ & \text { So Area of } R=' 17.1^{\prime}-' 12.6 \text { ' }=4.5 \end{aligned}$ | M1 A1 |
|  |  | M1 A1 <br> (4) 12 |
| Notes | (a) M1: Needs $\theta$ in radians for this formula. Could convert to degrees and use degrees formula. <br> A1: Does not need units <br> (b) M1: Needs $\theta$ in radians for this formula. Could convert to degrees and use degr formula. <br> A1: Does not need units <br> (c) M1: Needs complete correct trig method to achieve $x=$ May have worked in degrees, using 54.4 degrees and 71.1 degrees Using angles of triangle sum to 360degrees is not correct method so is M0 <br> A1: accept answers which round to 5.16 (NB This is given answer) If the answer 5.16 is assumed and verified award M1A0 for correct work <br> (d) M1: Accept answer only as implying method, or just $6+5.7$ <br> A1: can be scored even following wrong answer to part (c) <br> (e) M1: needs complete method for area of triangle $A B D$ not $A B C$ <br> A1: Accept awrt 12.6 (If area of triangle is not evaluated or is given as 12.5 this mark may be implied by 4.5 later) <br> M1: Uses area of $R=$ area of sector - area of triangle ABD (not ABC) <br> A1: Answers wrt 4.5 | rees <br> runcated) |
| Alternative For part (e) | Finds area of segment and area of triangle $B D C$ by correct methods M1 Obtains 2.4585 and 2.0498 - accept answers wrt 2.5, 2.1 A1 Uses area of segment + area of triangle BDC ,to obtain 4.5 (not 4.6) M1, A1 NB Just finding area of segment is M0 |  |

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| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 9 (i) | $\sin (3 x-15)=\frac{1}{2} \text { so } 3 x-15=30 \quad(\alpha) \text { and } x=15$ <br> Need $3 x-15=180-\alpha$ or $3 x-15=540-\alpha$ <br> Need $3 x-15=180-\alpha$ and $3 x-15=360+\alpha$ and $3 x-15=540-\alpha$ $x=55 \text { or } 175$ $x=55,135,175$ | M1 A1 <br> M1 <br> M1 <br> A1 <br> A1 <br> (6) |
| Notes | M1 Correct order of operation: inverse sine then linear algebra - not just $3 x-15=30$ (slips in linear algebra lose Accuracy mark) <br> A1 Obtains first solution 15 <br> M1 Uses either $180-\alpha$ or $540-\alpha$, <br> M1 uses all three $180-\alpha$ and $360+\alpha$ and $540-\alpha$ <br> A1, for one further correct solution 55 or 175, (depends only on second M1) <br> A1 - all 3 further correct solutions <br> If more than 4 solutions in range, lose last A1 <br> Common slips: Just obtains 15 and 55, or 15 and 175 - usually M1A1M1M0A1A0 <br> Just obtains 15 and 135 is usually M1A1M0M0A0A0 (It is easy to get this erroneously) <br> Obtains 5, 45, 125 and 165 - usually M1A0M1M1A0A0 <br> Obtains 25, 65, 145, (185) usually M1A0M1M1A0A0 <br> Working in radians - lose last A1 earned for $\frac{\pi}{12}, \frac{11 \pi}{36}, \frac{3 \pi}{4}$ and $\frac{35 \pi}{36}$ or numerical <br> equivalents <br> Mixed radians and degrees is usually Method marks only <br> Methods involving no working should be sent to Review |  |
| 9 (ii) | At least one of $\quad\left(\frac{a \pi}{10}-b\right)=0($ or $n \pi)$ $\begin{array}{lll}  & \left(\frac{a 3 \pi}{5}-b\right)=\pi & \{\text { or }(n+1) \pi\} \\ \text { or } \quad \text { or in degrees } \\ \left(\frac{a 11 \pi}{10}-b\right)=2 \pi & \{\text { or }(n+2) \pi\} \end{array}$ <br> If two of above equations used eliminates $a$ or $b$ to find one or both of these or uses period property of curve to find $a$ or uses other valid method to find either $a$ or $b \quad$ (May see $\frac{5 \pi}{10} a=\pi$ so $a=$ ) Obtains $a=2$ <br> Obtains $b=\frac{\pi}{5}$ (must be in radians) | M1 <br> M1 <br> A1 <br> A1 |

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\(\left.\begin{array}{|l|l|}\hline Notes \& M1: Award for\left(\frac{a \pi}{10}-b\right)=0 or \frac{a \pi}{10}=b BUT \sin \left(\frac{a \pi}{10}-b\right)=0 is M0 <br>
\& \left.M1: As described above but solving\left(\frac{a \pi}{10}-b\right)=0 \quad with\left(\frac{a 3 \pi}{5}-b\right)=0 is M0 (It gives a=b=0\right) <br>
Special cases: <br>
Can obtain full marks here for both correct answers with no working M1M1A1A1 <br>
For a=2 only, with no working, award M0M1A1A0 For b=\frac{\pi}{5} only with no working <br>

M1M0A0A1\end{array}\right\}\)| Some use translations and stretches to give answers. |
| :--- |
| If they achieve $a=2$ they earn second method and first accuracy. If they achieve correct value for $b$ |
| they earn first method and second accuracy. |
| Common error is $a=2$ and $b=\frac{\pi}{10}$. This is usually M0M1A1A0 unless they have stated |
| $\left(\frac{a \pi}{10}-b\right)=0 \quad$ earlier in which case they earn first M1. |

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## Mark Scheme (Results)

Summer 2012

GCE Core Mathematics C2 (6664) Paper 1

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## Summer 2012 6664 Core Mathematics C2 Mark Scheme

## General Marking Guidance

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## EDEXCEL GCE MATHEMATICS

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4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

## General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

## Method mark for solving 3 term quadratic:

1. Factorisation

$$
\begin{aligned}
& \left(x^{2}+b x+c\right)=(x+p)(x+q), \text { where }|p q|=|c|, \text { leading to } x=\ldots . \\
& \left(a x^{2}+b x+c\right)=(m x+p)(n x+q), \text { where }|p q|=|c| \text { and }|m n|=|a|, \text { leading to } x=\ldots
\end{aligned}
$$

2. Formula

Attempt to use correct formula (with values for $a, b$ and $c$ ), leading to $x=\ldots$
3. Completing the square

Solving $x^{2}+b x+c=0: \quad\left(x \pm \frac{b}{2}\right)^{2} \pm q \pm c, \quad q \neq 0, \quad$ leading to $x=\ldots$

## Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. ( $x^{n} \rightarrow x^{n-1}$ )

## 2. Integration

Power of at least one term increased by 1. $\left(x^{n} \rightarrow x^{n+1}\right)$

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.
Normal marking procedure is as follows:
Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.
Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

## Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

## Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.

## Summer 2012 6664 Core Mathematics 2 Mark Scheme

| Question number | Scheme Marks |
| :---: | :---: |
| 1 <br>  <br>  <br> Notes | $\begin{aligned} {\left[(2-3 x)^{5}\right] } & =\ldots \quad+\binom{5}{1} 2^{4}(-3 x)+\binom{5}{2} 2^{3}(-3 x)^{2}+\ldots, \ldots \ldots \\ & =32,-240 x,+720 x^{2} \end{aligned}$ <br> M1: The method mark is awarded for an attempt at Binomial to get the second and/or third term - need correct binomial coefficient combined with correct power of $\boldsymbol{x}$. Ignore errors (or omissions) in powers of 2 or 3 or sign or bracket errors. Accept any notation for ${ }^{5} C_{1}$ and ${ }^{5} C_{2}$, e.g. $\binom{5}{1}$ and $\binom{5}{2}$ (unsimplified) or 5 and 10 from Pascal's triangle This mark may be given if no working is shown, but either or both of the terms including $x$ is correct. <br> B1: must be simplified to 32 ( writing just $2^{5}$ is $\mathbf{B 0}$ ). $\mathbf{3 2}$ must be the only constant term in the final answer- so $32+80-3 x+80+9 x^{2}$ is B0 but may be eligible for M1A0A0. A1: is cao and is for $-240 x$. (not +240 x ) The $x$ is required for this mark <br> A1: is c.a.o and is for $720 x^{2}$ (can follow omission of negative sign in working) A list of correct terms may be given credit i.e. series appearing on different lines Ignore extra terms in $x^{3}$ and/or $x^{4}$ (isw) |
| Special Case | Special Case: Descending powers of $x$ would be $(-3 x)^{5}+2 \times 5 \times(-3 x)^{4}+2^{2} \times\binom{ 5}{3} \times(-3 x)^{3}+.$. i.e. $-243 x^{5}+810 x^{4}-1080 x^{3}+.$. This is a misread but award as s.c. M1B1A0A0 if completely "correct" or M1 B0A0A0 for correct binomial coefficient in any form with the correct power of $x$ |
| Alternative Method | Method 1: $\left[(2-3 x)^{5}\right]=2^{5}\left(1+\binom{5}{1}\left(-\frac{3 x}{2}\right)+\binom{5}{2}\left(\frac{-3 x}{2}\right)^{2}+..\right)$ is M1B0A0A0 \{ The M1 is for the expression in the bracket and as in first method- need correct binomial coefficient combined with correct power of $x$. Ignore bracket errors or errors (or omissions) in powers of 2 or 3 or sign or bracket errors \} <br> - answers must be simplified to $=32,-240 x,+720 x^{2}$ for full marks (awarded as before) $\left[(2-3 x)^{5}\right]=2\left(1+\binom{5}{1}\left(-\frac{3 x}{2}\right)+\binom{5}{2}\left(\frac{-3 x}{2}\right)^{2}+..\right)$ would also be awarded M1B0A0A0 <br> Method 2: Multiplying out : B1 for 32 and M1A1A1 for other terms with M1 awarded if $x$ or $x^{\wedge} 2$ term is correct. Completely correct is $4 / 4$ |


| Question number | Scheme Marks |
| :---: | :---: |
| 2 | $\begin{gathered} 2 \log x=\log x^{2} \\ \log _{3} x^{2}-\log _{3}(x-2)=\log _{3} \frac{x^{2}}{x-2} \\ \frac{x^{2}}{x-2}=9 \end{gathered}$ <br> Solves $x^{2}-9 x+18=0 \quad$ to give $x=\ldots .$. $x=3, x=6$ |
|  | Total 5 |
| Notes | B1 for this correct use of power rule (may be implied) <br> M1: for correct use of subtraction rule (or addition rule) for logs <br> N.B. $2 \log _{3} x-\log _{3}(x-2)=2 \log _{3} \frac{x}{x-2}$ is M0 <br> A1. for correct equation without logs (Allow any correct equivalent including $3^{2}$ instead of 9.) <br> M1 for attempting to solve $x^{2}-9 x+18=0$ to give $x=$ (see notes on marking quadratics) <br> A1 for these two correct answers |
| Alternative Method | $\log _{3} x^{2}=2+\log _{3}(x-2) \quad$ is B1, <br> so $\quad x^{2}=3^{2+\log _{3}(x-2)}$ needs to be followed by $\left(x^{2}\right)=9(x-2)$ for M1 A1 <br> Here M1 is for complete method i.e.correct use of powers after logs are used correctly |
| Common Slips | $2 \log x-\log x+\log 2=2$ may obtain B1 if $\log x^{2}$ appears but the statement is M0 and so leads to no further marks <br> $2 \log _{3} x-\log _{3}(x-2)=2$ so $\log _{3} x-\log _{3}(x-2)=1$ and $\log _{3} \frac{x}{x-2}=1$ can earn M1 for correct subtraction rule following error, but no other marks |
| Special Case | $\frac{\log x^{2}}{\log (x-2)}=2$ leading to $\frac{x^{2}}{x-2}=9$ and then to $x=3, x=6$, usually earns B1M0A0, but may then earn M1A1 (special case) so $3 / 5$ [ This recovery after uncorrected error is very common] <br> Trial and error, Use of a table or just stating answer with both $x=3$ and $x=6$ should be awarded B0M0A0 then final M1A1 i.e. $2 / 5$ |



| Question number | Scheme ${ }^{\text {arks }}$ |
| :---: | :---: |
| $4 \text { (a) }$ | $f(-2)=2 \cdot(-2)^{3}-7 \cdot(-2)^{2}-10 \cdot(-2)+24$ M1  <br> $=0$ so $(x+2)$ is a factor A1  <br>    <br> $\mathrm{f}(x)=(x+2)\left(2 x^{2}-11 x+12\right)$   <br> $\mathrm{f}(x)=(x+2)(2 x-3)(x-4)$ M1 A1  <br>   dM1 A1 |
| (b) | 6 marks |
| Notes (a) | M1 : Attempts $\mathrm{f}( \pm 2)$ (Long division is M0) <br> A1 : is for $=0$ and conclusion <br> Note: Stating "hence factor" or "it is a factor" or a " $\sqrt{ }$ " (tick) or "QED" is fine for the conclusion. <br> Note also that a conclusion can be implied from a preamble, eg: "If $\mathrm{f}(-2)=0,(x+2)$ is a factor...." (Not just f(-2)=0) <br> $\mathbf{1}^{\text {st }} \mathbf{M 1}$ : Attempts long division by correct factor or other method leading to obtaining ( $2 x^{2} \pm a x \pm b$ ), $a \neq 0, b \neq 0$, even with a remainder. Working need not be seen as could be done "by inspection." <br> Or Alternative Method : $\mathbf{1}^{\text {st }} \mathbf{M 1}$ : Use $(x+2)\left(a x^{2}+b x+c\right)=2 x^{3}-7 x^{2}-10 x+24$ with expansion and comparison of coefficients to obtain $a=2$ and to obtain values for $b$ and $c$ <br> $\mathbf{1}^{\text {st }}$ A1: For seeing $\left(2 x^{2}-11 x+12\right)$. [Can be seen here in (b) after work done in (a)] <br> $\mathbf{2}^{\text {nd }} \mathbf{M} \mathbf{1}$ : Factorises quadratic. (see rule for factorising a quadratic). This is dependent on the previous method mark being awarded and needs factors <br> $\mathbf{2}^{\text {nd }} \mathbf{A 1}$ : is cao and needs all three factors together. Ignore subsequent work (such as a solution to a quadratic equation.) <br> Note: Some candidates will go from $\{(x+2)\}\left(2 x^{2}-11 x+12\right)$ to $\{x=-2\}, x=\frac{3}{2}, 4$, and not list all three factors. Award these responses M1A1M0A0. <br> Finds $x=4$ and $x=1.5$ by factor theorem, formula or calculator and produces factors M1 $\mathrm{f}(x)=(x+2)(2 x-3)(x-4)$ or $\mathrm{f}(x)=2(x+2)(x-1.5)(x-4)$ o.e. is full marks $\mathrm{f}(x)=(x+2)(x-1.5)(x-4)$ loses last A1 |



| $\begin{gathered} \text { Method } 2 \\ \text { for (b) } \end{gathered}$ | Area of $R$ $\begin{aligned} & =\int_{2}^{9}\left(10 x-x^{2}-8\right)-(10-x) \mathrm{d} x \\ & \int_{2}^{9}-x^{2}+11 x-18 \mathrm{~d} x \\ & =-\frac{x^{3}}{3}+\frac{11 x^{2}}{2}-18 x\{+c\} \\ & {\left[-\frac{x^{3}}{3}+\frac{11 x^{2}}{2}-18 x\right]_{2}^{9}=(\ldots \ldots)-(\ldots \ldots)} \end{aligned}$ <br> $3^{\text {rd }}$ M1 (in (b) ): Uses difference between two functions in integral. <br> M: $x^{n} \rightarrow x^{n+1}$ for any one term. <br> A1 at least two out of these three simplified terms <br> Correct integration. (Ignore $+c$ ). <br> Substitutes 9 and 2 (or limits from part(a)) into an "integrated function" and subtracts, either way round. <br> This mark is implied by final answer which rounds to 57.2 <br> See above working(allow bracketing errors) to decide to award $3^{\text {rd }}$ M1 mark for (b) here: $40.5-\left(-16 \frac{2}{3}\right)=57 \frac{1}{6} \mathrm{cao}$ | M1 <br> A1 <br> A1 <br> dM1 <br> B1 <br> M1 <br> A1 <br> (7) |
| :---: | :---: | :---: |
| Special case of above method | $\begin{aligned} & \int_{2}^{9} x^{2}-11 x+18 \mathrm{~d} x=\frac{x^{3}}{3}-\frac{11 x^{2}}{2}+18 x\{+c\} \\ & {\left[\frac{x^{3}}{3}-\frac{11 x^{2}}{2}+18 x\right]_{2}^{9}=(\ldots . .)-(\ldots . .)} \end{aligned}$ <br> This mark is implied by final answer which rounds to 57.2 (not -57.2) <br> Difference of functions implied (see above expression) $40.5-\left(-16 \frac{2}{3}\right)=57 \frac{1}{6} \text { cao }$ | M1A1A1 <br> DM1 <br> B1 <br> M1 <br> A1 |
| Special Case 2 | Integrates expression in $y$ e.g. " $y^{2}-9 y+8=0$ ": This can have first M1 in part (b) and no other marks. (It is not a method for finding this area) |  |
| Notes | Take away trapezium again having used Method 2 loses last two marks Common Error: <br> Integrates $-x^{2}+9 x-18$ is likely to be M1A1A0dM1B0M1A0 <br> Integrates $2-11 x-x^{2}$ is likely to e M1A0A0dM1B0M1A0 <br> Writing $\int_{2}^{9}\left(10 x-x^{2}-8\right)-(10-x) \mathrm{d} x$ only earns final M mark |  |




| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 8 (a) | $(h=) \frac{60}{\pi x^{2}} \quad$ or equivalent exact (not decimal) expression e.g. $\quad(h=) 60 \div \pi x^{2}$ | B1 (1) |
| (b) | $(A=) 2 \pi x^{2}+2 \pi x h \quad \text { or }(A=) 2 \pi r^{2}+2 \pi r h \quad \text { or }(A=) 2 \pi r^{2}+\pi d h$ <br> may not be simplified and may appear on separate lines | B1 |
|  | Either $\quad(A)=2 \pi x^{2}+2 \pi x\left(\frac{60}{\pi x^{2}}\right)$ or As $\pi x h=\frac{60}{x}$ then $(A=) 2 \pi x^{2}+2\left(\frac{60}{x}\right)$ | M1 |
|  | $A=2 \pi x^{2}+\left(\frac{120}{x}\right)$ | A1 cso (3) |
| (c) | $\left(\frac{\mathrm{d} A}{\mathrm{~d} x}\right)=4 \pi x-\frac{120}{x^{2}} \quad \text { or }=4 \pi x-120 x^{-2}$ | M1 A1 |
|  | $4 \pi x-\frac{120}{x^{2}}=0$ implies $x^{3}=\quad$ (Use of $>0$ or $<0$ is M0 then M0A0) | M1 |
|  | $x=\sqrt[3]{\frac{120}{4 \pi}}$ or answers which round to $2.12 \quad$ ( -2.12 is A 0 ) | dM1 A1 |
| (d) | $A=2 \pi(2.12)^{2}+\frac{120}{2.12},=85 \quad$ (only ft $x=2$ or $2.1-$ both give 85 ) | M1, A1 (2) |
| (e) | Either $\frac{d^{2} A}{d x^{2}}=4 \pi+\frac{240}{x^{3}}$ and sign <br> Or (method 2) considers gradient to left and right of their 2.12 (e.g at 2 and 2.5) | M1 |
|  | considered ( May appear in (c) ) Or (method 3) considers value of $A$ either side |  |
|  | which is $>0$ and therefore minimum gradients go from negative to zero to positive so <br> (most substitute 2.12 but it is not essential concludes minimum <br> to see a substitution ) (may appear in (c)) OR finds numerical values of $A$, observing <br>  greater than minimum value and draws conclusion | A1 (2) |
|  |  | 13 marks |
| Notes | (a) B1: This expression must be correct and in part (a) $\frac{60}{\pi r^{2}}$ is B0 <br> (b) B1: Accept any equivalent correct form - may be on two or more lines. <br> M1 : substitute their expression for $h$ in terms of $x$ into Area formula of the form $k x^{2}+c x h$ <br> A1: There should have been no errors in part (b) in obtaining this printed answer <br> (c) M1: At least one power of $x$ decreased by $1 \quad \mathbf{A 1}$ accept any equivalent correct answer <br> M1: Setting $\frac{\mathrm{d} A}{\mathrm{~d} x}=0$ and finding a value for $x^{3}$ ( $x^{3}=$ may be implied by answer). Allow $\frac{d y}{d x}=0$ <br> dM1: Using cube root to find $x$ <br> A1 : For any equivalent correct answer (need 3sf or more) Correct answer implies previous M mark <br> (d) M1 : Substitute the (+ve) $x$ value found in (c) into equation for $A$ and evaluate. A1 is for $\mathbf{8 5}$ only <br> (e) M1: Complete method, usually one of the three listed in the scheme. For first method $A^{\prime \prime}(x)$ must be attempted and sign considered <br> A1: Clear statements and conclusion. (numerical substitution of $x$ is not necessary in first method shown, and $x$ or calculation could be wrong but $A^{\prime \prime}(x)$ must be correct. Must not see 85 substituted) |  |
|  |  |  |  |
|  |  |  |  |

\begin{tabular}{|c|c|c|}
\hline Question \& Scheme \& Marks <br>
\hline $9(a)$
(b)

(c)

(d)

Notes
Specia

Case \& \multicolumn{2}{|l|}{| (a) M1: Lists both of these sums ( $S_{n}=$ ) may be omitted, $r S_{n}$ (or $r S$ ) must be stated |
| :--- |
| $1^{\text {st }}$ two terms must be correct in each series. Last term must be $a r^{n-1}$ or $a r^{n}$ in first series and the corresponding $a r^{n}$ or $a r^{n+1}$ in second series. Must be $n$ and not a number. Reference made to other terms e.g. space or dots to indicate missing terms |
| M1: Subtracts series for $r S$ from series for $S$ (or other way round) to give RHS $= \pm\left(a-a r^{n}\right)$. This may have been obtained by following a pattern. If wrong power stated on line 1 M0 here. (Ignore LHS)M0M0M0A0 |
| dM1: Factorises both sides correctly- must follow from a previous M1 (It is possible to obtain M0M1M1A0 or |
| M1M0M1A0) A1: completes the proof with no errors seen |
| No errors seen: First line absolutely correct, omission of second line, third and fourth lines correct: |
| M1M0M1A1 |
| See next sheet of common errors. |
| Refer any attempts involving sigma notation, or any proofs by induction to team leader. Also attempts which begin with the answer and work backwards. |
| (b) M1: Deduces $r^{2}$ by dividing either term by other and attempts square root |
| A1: any correct equivalent for $r$ e.g. 3/5 Answer only is $2 / 2$ |
| (Method 2) Those who find fourth term must use $\sqrt{a b}$ and not $\frac{1}{2}(a+b)$ then must use it in a division with given term to obtain $r=$ |
| (c) M1: May be done in two steps or more e.g. $5.4 \div r$ then divided by $r$ again |
| A1ft: follow through their value of $r$. Just $a=15$ with no wrong working implies M1A1 |
| (d) M1: States sum to infinity formula with values of $a$ and $r$ found earlier, provided $\|r\|<1$ |
| A1 : uses 15 and 0.6 (or 3/5) (This is not a ft mark) |
| A1: 37.5 or exact equivalent |} <br>

\hline Common errors \& | (i) Fraction inverted in (b) $r^{2}=\frac{5.4}{1.944}$ and $r=1 \frac{2}{3}$, then correct ft gives M1A0 M1 A1ft M0A |
| :--- |
| (ii) Uses $r=0.36$ : |
| (b)M0A0 |
| (c)M1A1ft |
| (d) M1A0A0 i.e. $3 / 7$ |
| (iii) Uses $a r^{3}=5.4, a r^{5}=1.944$ Likely to have (b)M1A1 |
| (c)M0A0 (d) M1A0A0 i.e. $3 / 7$ | \& i.e. 3/7 <br>

\hline
\end{tabular}

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## January 2013

GCE Core Mathematics C2 (6664/01)

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- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.
- Unless indicated in the mark scheme a correct answer with no working should gain full marks for that part of the question.


## EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

1. The total number of marks for the paper is 75 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of $M$ marks)
- Marks should not be subdivided.

In some instances, the mark distributions (e.g. M1, B1 and A1) printed on the candidate's response may differ from the final mark scheme.
3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used.

- bod - benefit of doubt
- ft - follow through
- the symbol will be fúsed for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- $\quad$ The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft , but incorrect answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.
8. The maximum mark allocation for each question/part question(item) is set out in the marking grid and you should allocate a score of ' 0 ' or ' 1 ' for each mark, or "trait", as shown:

|  | 0 | 1 |
| :--- | :---: | :---: |
| aM |  | $\bullet$ |
| aA | $\bullet$ |  |
| bM1 |  | $\bullet$ |
| bA1 | $\bullet$ |  |
| bB | $\bullet$ |  |
| bM2 |  | $\bullet$ |
| bA2 |  | $\bullet$ |

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|  |  |  |  |
| :---: | :---: | :---: | :---: |
| 8. | $y=6-3 x-\frac{4}{x^{3}}$ |  |  |
| (a) | $\frac{\mathrm{d} y}{\mathrm{~d} x}=-3+\frac{12}{x^{4}} \text { or }-3+12 x^{-4}$ | $\begin{array}{\|l\|} \hline \text { M1: } x^{n} \rightarrow x^{n-1} \\ \left(x^{1} \rightarrow x^{0} \text { or } x^{-3} \rightarrow x^{-4} \text { or } 6 \rightarrow 0\right) \\ \hline \text { A1: Correct derivative } \\ \hline \end{array}$ | M1 A1 |
|  | $\begin{aligned} & \frac{\mathrm{d} y}{\mathrm{~d} x}=0 \Rightarrow-3+\frac{12}{x^{4}}=0 \Rightarrow x=\ldots . \text { or } \\ & \frac{\mathrm{d} y}{\mathrm{~d} x}=-3+\frac{12}{\sqrt{2}^{4}} \end{aligned}$ | $y^{\prime}=0$ and attempt to solve for $x$ <br> May be implied by $\frac{\mathrm{d} y}{\mathrm{~d} x}=-3+\frac{12}{x^{4}}=0 \Rightarrow \frac{12}{x^{4}}=3 \Rightarrow x=\ldots \text { or }$ <br> Substitutes $x=\sqrt{2}$ into their $y^{\prime}$ | M1 |
|  | So $x^{4}=4$ and $x=\sqrt{2}$ or $\frac{\mathrm{d} y}{\mathrm{~d} x}=-3+\frac{12}{(\sqrt{2})^{4}} \text { or }-3+12(\sqrt{2})^{-4}=0$ | Correct completion to answer with no errors by solving their $y^{\prime}=0$ or substituting $x=\sqrt{2}$ into their $y^{\prime}$ | A1 |
|  |  |  | (4) |
| (b) | $x=-\sqrt{2}$ | Awrt -1.41 | B1 |
|  |  |  | (1) |
| (c) | $\frac{\mathrm{d}^{2} y}{\mathrm{~d} x^{2}}=\frac{-48}{x^{5}} \text { or }-48 x^{-5}$ | Follow through their first derivative from part (a) | B1ft |
|  |  |  | (1) |
| (d) | An appreciation that either $y^{\prime \prime}>0 \Rightarrow$ a minimum <br> or $y^{\prime \prime}<0 \Rightarrow$ a maximum |  | B1 |
|  | Maximum at P as $y^{\prime \prime}<0$ | Cso | B1 |
|  | Need a fully correct solution for this mark. $y^{\prime \prime}$ need not be evaluated but must be correct and there must be reference to P or to $\sqrt{2}$ and negative or $<0$ and maximum. There must be no incorrect or contradictory statements (NB allow $y^{\prime \prime}=$ awrt-8 or -9) |  |  |
|  | Minimum at Q as $y^{\prime \prime}>0$ | Cso | B1 |
|  | Need a fully correct solution for this mark. $y^{\prime \prime}$ need not be evaluated but must be correct and part (b) must be correct and there must be reference to P or to $-\sqrt{2}$ and positive or $>0$ and minimum. There must be no incorrect or contradictory statements (NB allow $y^{\prime \prime}=$ awrt 8 or 9) |  |  |
|  |  |  | (3) |
|  |  |  | [9] |
|  | Other methods for identifying the nature of the turning points are acceptable. The first B1 is for finding values of $y$ or $d y / d x$ either side of $\sqrt{2}$ or their $x$ at $Q$ and the second and third B1's for fully correct solutions to identify the maximum/minimum. |  |  |



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- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## EDEXCEL GCE MATHEMATI CS

## General Instructions for Marking

1. The total number of marks for the paper is 75 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes:

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- $\quad$ The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.
8. In some instances, the mark distributions (e.g. M1, B1 and A1) printed on the candidate's response may differ from the final mark scheme.

## General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

## Method mark for solving 3 term quadratic:

1. Factorisation
$\left(x^{2}+b x+c\right)=(x+p)(x+q)$, where $|p q|=|c|$, leading to $\mathrm{x}=$
$\left(a x^{2}+b x+c\right)=(m x+p)(n x+q)$, where $|p q|=|c|$ and $|m n|=|a|$, leading to $\mathrm{x}=$
2. Formula

Attempt to use correct formula (with values for $a, b$ and $c$ ).
3. Completing the square

Solving $x^{2}+b x+c=0: \quad\left(x \pm \frac{b}{2}\right)^{2} \pm q \pm c, \quad q \neq 0, \quad$ leading to $\mathrm{x}=\ldots$

## Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by $1 .\left(x^{n} \rightarrow x^{n-1}\right)$

## 2. Integration

Power of at least one term increased by 1. $\left(x^{n} \rightarrow x^{n+1}\right)$

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.
Normal marking procedure is as follows:
Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.
Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

## Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

## Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.

| Question Number | Scheme ${ }^{\text {a }}$ Marks |
| :---: | :---: |
| 1. | $\frac{\mathrm{d} y}{\mathrm{~d} x}=2-16 x^{-3}$ <br> $2-16 x^{-3}=0$ so $x^{-3}=$ or $x^{3}=$, or $2-16 x^{-3}=0$ so $x=2$ $x=2$ only (after correct derivative) $y=2 \times " 2 "+3+\frac{8}{" 2^{2} "}$ $=9$ |
|  | Notes for Question 1 |
|  | $1^{\text {st }} \mathrm{M} 1$ : At least one term differentiated ( not integrated) correctly, so $2 x \rightarrow 2$, or $\frac{8}{x^{2}} \rightarrow-16 x^{-3}$, or $3 \rightarrow 0$ <br> A1: This answer or equivalent e.g. $2-\frac{16}{x^{3}}$ $2^{\text {nd }}$ M1: Sets $\frac{\mathrm{d} y}{\mathrm{~d} x}$ to 0 , and solves to give $x^{3}=$ value or $x^{-3}=$ value <br> (or states $x=2$ with no working following correctly stated $2-16 x^{-3}=0$ ) <br> A1: $x=2$ cso (if $x=-2$ is included this is A0 here) <br> $3^{\text {rd }}$ M1: Attempts to substitutes their positive $x$ (found from attempt to differentiate) into $y=2 x+3+\frac{8}{x^{2}}, x>0$ <br> Or may be implied by $y=9$ or correct follow through from their positive $x$ <br> A1: 9 cao (Does not need to be written as coordinates) (ignore the extra $(-2,1)$ here) |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 2.(a)(b) | $\{x=1.3\} \quad y=0.8572$ (only) | B1 cao |
|  | $\begin{aligned} & \frac{1}{2} \times 0.1 \ldots . . . . . . \\ & \{0.7071+0.9487+2(0.7591+0.8090+" 0.8572 "+0.9037)\} \\ & \ldots\{0.7071+0.9487+2(0.7591+0.8090+" 0.8572 "+0.9037)\} \\ & \{0.05(8.3138)\}=0.41569=\text { awrt } 0.416 \end{aligned}$ | B1 <br> M1 <br> A1ft <br> A1 <br> (4) <br> Total 5 |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  | Notes for Question 2 |  |
| (a) <br> (b) | B1: 0.8572 cao <br> B1 for using $\frac{1}{2} \times 0.1$ or 0.05 or equivalent. <br> M1 It needs the first bracket to contain first $y$ value plus last $y$ value and the second bracket to be multiplied by 2 and to be the summation of the remaining $y$ values in the table with no additional values. If the only mistake is a copying error or is to omit one value from 2nd bracket this may be regarded as a slip and the M mark can be allowed ( An extra repeated term forfeits the M mark however). M0 if values used in brackets are $x$ values instead of $y$ values A1ft for the correct bracket $\{\ldots . .$.$\} following through candidate's y$ value found in part (a). <br> NB: Separate trapezia may be used : B1 for 0.05 , M1 for $1 / 2 h(a+b)$ used 4 or 5 times (and A1ft if it is all correct ) Then A1 as before. (Equivalent correct formulae may be used) Special case: Bracketing mistake $0.05 \times(0.7071+0.9487)+2(0.7591+0.8090+" 0.8572 "+0.9037)$ scores B1 M1 A0 A0 (usually for 6.74079 ) unless the final answer implies that the calculation has been done correctly (then full marks can be given). |  |
|  |  |  |  |







\begin{tabular}{|c|c|c|}
\hline Question Number \& Scheme \& Marks <br>
\hline 8.(a)

(b) \& \begin{tabular}{l}
Way 1: $10^{2}=7^{2}+13^{2}-2 \times 7 \times 13 \cos \theta$ or $\cos \theta=\frac{7^{2}+13^{2}-10^{2}}{2 \times 7 \times 13}$ $\cos \theta=\frac{59}{91}$ or $\cos \theta=\frac{7^{2}+13^{2}-10^{2}}{2 \times 7 \times 13}$ or $\cos \theta=0.6483$ or 0.8644 $(\theta=0.8653789549 \ldots)=0.865$ * (to 3 dp ) <br>
Way 2: Uses $\cos \theta=\frac{x}{7}$, where $7^{2}-x^{2}=10^{2}-(13-x)^{2}$ and finds $x \quad(=59 / 13)$ $\cos \theta=\frac{59}{91}$ and $(\theta=0.8653789549 \ldots)=0.865 *(t o 3 d p)-$ as in Way 1 Area triangle $A B C=\frac{1}{2} \times 13 \times 7 \sin 0.865$ or $\frac{1}{2} \times 13 \times 7 \sin 49.6$ or $20 \sqrt{3}$ Area sector $A B D=\frac{1}{2} \times 7^{2} \times 0.865$ or $\frac{49.6}{360} \times \pi \times 7^{2}$ $=34.6$ (triangle) or 21.2 (Sector) <br>
Area of $S=\frac{1}{2} \times 13 \times 7 \sin 0.865-\frac{1}{2} \times 7^{2} \times 0.865 \quad(=13.4)$ <br>
(Amount of seed =) $13.4 \times 50=670 \mathrm{~g}$ or 680 g (need one of these two answers)

 \& 

A1 o.e <br>
A1* cso <br>
(3) <br>
M1 <br>
A1, A1 <br>
(3) <br>
M1 <br>
M1 <br>
A1 <br>
M1 A1 <br>
M1 A1 (7) <br>
Total 10
\end{tabular} <br>

\hline \& \multicolumn{2}{|l|}{Notes for Question 8} <br>
\hline (a)

(b) \& \begin{tabular}{l}
M1: use correct cosine formula in any form A1: give a value for $\cos \theta$ NB $\cos \theta=\frac{7^{2}+13^{2}-10^{2}}{2 \times 7 \times 13}$ earns M1A1 <br>
A1: deduce and state the printed answer $\theta=0.865$ <br>
M1: Uses Correct method for area of the correct triangle i.e. $A B C$ <br>
M1: Uses Correct method for the area of the sector <br>
A1: This is earned for one of the correct answers. May be implied if these an calculated but the final answer is correct with no errors (or shaded area is 13. <br>
M1: Their area of Triangle $A B C$ - Area of Sector (may have $k r^{2} \theta$ but not $k \theta$ ) <br>
A1: Correct expression or awrt 13.4 or 13.5 (may be implied by final answe <br>
M1: Multiply their previous answer by 50 <br>
A1: 670 g or 680 g (There is an argument for rounding answer up to provide

 \& 

rs are not 13.5) <br>
gh seed)
\end{tabular} <br>

\hline \multicolumn{3}{|l|}{$$
\begin{aligned}
& \text { N.B. }\left(\frac{1}{2} \times 13 \times 7 \sin 0.865-\frac{1}{2} \times 7^{2} \times 0.865\right) \times 50=670 \text { or } 680 \text { earns full marks } \\
&\left(\frac{1}{2} \times 13 \times 7 \sin 0.865-\frac{1}{2} \times 7^{2} \times 0.865\right) \times 50=\text { awrt } 670 \text { or } 680 \text { just loses last mark } \\
&\left(\frac{1}{2} \times 13 \times 7 \sin 0.865-\frac{1}{2} \times 7^{2} \times 0.865\right) \times 50=\text { wrong answer M1M1A0M1A1M1A0 }
\end{aligned}
$$} <br>

\hline
\end{tabular}

\begin{tabular}{|c|c|c|}
\hline Question Number \& Scheme \& Marks <br>
\hline 9.(a)

(b) \& \[
$$
\begin{aligned}
& \sin (2 \theta-30)=-0.6 \text { or } 2 \theta-30=-36.9 \text { or implied by } 216.9 \\
& 2 \theta-30=216.87=(180+36.9) \\
& \theta=\frac{216.87+30}{2}=123.4 \text { or } 123.5 \\
& 2 \theta-30=360-36.9 \quad \text { or } 323.1 \\
& \theta=\frac{323.1+30}{2}=176.6 \\
& 9 \cos ^{2} x-11 \cos x+3\left(1-\cos ^{2} x\right)=0 \text { or } 6 \cos ^{2} x-11 \cos x+3\left(\sin ^{2} x+\cos ^{2} x\right)=0 \\
& 6 \cos ^{2} x-11 \cos x+3=0\left\{\text { as }\left(\sin ^{2} x+\cos ^{2} x\right)=1\right\} \\
& (3 \cos x-1)(2 \cos x-3)=0 \text { implies } \cos x= \\
& \cos x=\frac{1}{3},\left(\frac{3}{2}\right) \\
& x=70.5
\end{aligned}
$$

\] \& | B1 |
| :--- |
| M1 |
| A1 |
| M1 |
| A1 |
| (5) |
| M1 |
| A1 |
| M1 |
| A1 |
| B1 | <br>

\hline \& \[
$$
\begin{aligned}
& x=360-" 70.5 " \\
& x=289.5
\end{aligned}
$$

\] \& | M1 |
| :--- |
| A1cao |
| (7) |
| Total 12 | <br>

\hline \& \multicolumn{2}{|l|}{Notes for Question 9} <br>
\hline (a)

(b) \& \multicolumn{2}{|l|}{| B1: This statement seen and must contain no errors or may implied by - 36.9 |
| :--- |
| M1: Uses $180-\arcsin (-0.6)$ i.e. $180+36.9$ ( or $\pi+\arcsin (0.6)$ in radians) (in $3^{\text {rd }}$ quadrant) |
| A1: allow answers which round to 123.4 or 123.5 must be in degrees |
| M1: Uses $360+\arcsin (-0.6)$ i.e. $360-36.9$ ( or $2 \pi+\arcsin (-0.6)$ in radians) (in 4th quadrant) |
| A1: allow answers which round to 176.6 must be in degrees (A1 implies M1) |
| Ignore extra answers outside range but lose final A 1 for extra answers in the range if both B and A marks have been earned) |
| Working in radians may earn B1M1A0M1A0 |
| M1: Use of $\sin ^{2} x=\left(1-\cos ^{2} x\right)$ or $\left(\sin ^{2} x+\cos ^{2} x\right)=1$ in the given equation |
| A1: Correct three term quadratic in any equivalent form |
| M1: Uses standard method to solve quadratic and obtains $\cos x=$ |
| A1: A1 for $\frac{1}{3}$ with $\frac{3}{2}$ ignored but A0 if $\frac{3}{2}$ is incorrect |
| B1: 70.5 or answers which round to this value |
| M1: $360-\operatorname{arcos}($ their1/3) ( or $2 \pi$-arccos(their1/3) in radians) |
| A1: Second answer |
| Working in radians in (b) may earn M1A1M1A1B0M1A0 |
| Extra values in the range coming from arcos (1/3) - deduct final A mark - so A0 |} <br>

\hline
\end{tabular}

Telephone 01623467467
Fax 01623450481
Email publication.orders@edexcel.com
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## Mark Scheme (Results)

## Summer 2013

GCE Core Mathematics 2 (6664/01)

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
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## EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

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- B marks are unconditional accuracy marks (independent of $M$ marks)
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## 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes:

- bod - benefit of doubt
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-     * The answer is printed on the paper
- $\quad$ The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.
8. In some instances, the mark distributions (e.g. M1, B1 and A1) printed on the candidate's response may differ from the final mark scheme.

## General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

## Method mark for solving 3 term quadratic:

1. Factorisation

$$
\begin{aligned}
& \left(x^{2}+b x+c\right)=(x+p)(x+q) \text {, where }|p q|=|c| \text {, leading to } \mathrm{x}= \\
& \left(a x^{2}+b x+c\right)=(m x+p)(n x+q) \text {, where }|p q|=|c| \text { and }|m n|=|a| \text {, leading to } \mathrm{x}=
\end{aligned}
$$

2. Formula

Attempt to use correct formula (with values for $a, b$ and $c$ ).
3. Completing the square

Solving $x^{2}+b x+c=0: \quad\left(x \pm \frac{b}{2}\right)^{2} \pm q \pm c, \quad q \neq 0, \quad$ leading to $\mathrm{x}=\ldots$

## Method marks for differentiation and integration:

## 1. Differentiation

Power of at least one term decreased by 1. $\left(x^{n} \rightarrow x^{n-1}\right)$
2. Integration

Power of at least one term increased by 1. $\left(x^{n} \rightarrow x^{n+1}\right)$

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.
Normal marking procedure is as follows:
Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.
Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

## Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

## Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.


\begin{tabular}{|c|c|}
\hline Question Number \& Scheme $\quad$ Marks <br>
\hline 2. (a)

(b) \& | $\begin{aligned} & (2+3 x)^{4} \text { - Mark (a) and (b) together } \\ & 2^{4}+{ }^{4} C_{1} 2^{3}(3 x)+{ }^{4} C_{2} 2^{2}(3 x)^{2}+{ }^{4} C_{3} 2^{1}(3 x)^{3}+(3 x)^{4} \end{aligned}$ |
| :--- |
| First term of 16 $\begin{aligned} & \left({ }^{4} C_{1} \times \ldots \times x\right)+\left({ }^{4} C_{2} \times \ldots \times x^{2}\right)+\left({ }^{4} C_{3} \times \ldots \times x^{3}\right)+\left({ }^{4} C_{4} \times \ldots \times x^{4}\right) \\ & =(16+) 96 x+216 x^{2}+216 x^{3}+81 x^{4} \quad \text { Must use Binomial }- \text { otherwise A } 0, \end{aligned}$ $(2-3 x)^{4}=16-96 x+216 x^{2}-216 x^{3}+81 x^{4}$ | <br>

\hline Alternative method (a) \& | $\begin{aligned} & (2+3 x)^{4}=2^{4}\left(1+\frac{3 x}{2}\right)^{4} \\ & 2^{4}\left(1+{ }^{4} C_{1}\left(\frac{3 x}{2}\right)+{ }^{4} C_{2}\left(\frac{3 x}{2}\right)^{2}+{ }^{4} C_{3}\left(\frac{3 x}{2}\right)^{3}+\left(\frac{3 x}{2}\right)^{4}\right) \end{aligned}$ |
| :--- |
| Scheme is applied exactly as before | <br>

\hline \& Notes for Question 2 <br>
\hline (a)

(b) \& | B1: The constant term should be 16 in their expansion |
| :--- |
| M1: Two binomial coefficients must be correct and must be with the correct power of $x$. Accept ${ }^{4} C_{1}$ or $\binom{4}{1}$ or 4 as a coefficient, and ${ }^{4} C_{2}$ or $\binom{4}{2}$ or 6 as another........ Pascal's triangle may be used to establish coefficients. |
| A1: Any two of the final four terms correct (i.e. two of $96 x+216 x^{2}+216 x^{3}+81 x^{4}$ ) in expansion following Binomial Method. |
| A1: All four of the final four terms correct in expansion. (Accept answers without + signs, can be listed with commas or appear on separate lines) |
| B1ft: Award for correct answer as printed above or ft their previous answer provided it has five terms ft and must be subtracting the $x$ and $x^{3}$ terms |
| Allow terms in (b) to be in descending order and allow $+-96 x$ and $+-216 x^{3}$ in the series. (Accept answers without + signs, can be listed with commas or appear on separate lines) | <br>

\hline \& | e.g. The common error $2^{4}+{ }^{4} C_{1} 2^{3} 3 x+{ }^{4} C_{2} 2^{2} 3 x^{2}+{ }^{4} C_{3} 2^{1} 3 x^{3}+3 x^{4}=(16)+96 x+72 x^{2}+24 x^{3}+3 x^{4}$ would earn B1, M1, A0, A0, and if followed by $=(16)-96 x+72 x^{2}-24 x^{3}+3 x^{4}$ gets B1ft so 3/5 |
| :--- |
| Fully correct answer with no working can score B1 in part (a) and B1 in part (b). The question stated use the Binomial theorem and if there is no evidence of its use then M mark and hence A marks cannot be earned. Squaring the bracket and squaring again may also earn B1 M0 A0 A0 B1 if correct Omitting the final term but otherwise correct is B1 M1 A1 A0 B0ft so 3/5 If the series is divided through by 2 or a power of 2 at the final stage after an error or omission resulting in all even coefficients then apply scheme to series before this division and ignore subsequent work (isw) | <br>

\hline
\end{tabular}






| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| $\begin{gathered} \text { 7. (i) } \\ \text { Method } 1 \end{gathered}$ | $\begin{aligned} & \log _{2}\left(\frac{2 x}{5 x+4}\right)=-3 \text { or } \log _{2}\left(\frac{5 x+4}{2 x}\right)=3, \text { or } \log _{2}\left(\frac{5 x+4}{x}\right)=4 \text { (see special case 2) } \\ & \left(\frac{2 x}{5 x+4}\right)=2^{-3} \text { or }\left(\frac{5 x+4}{2 x}\right)=2^{3} \text { or }\left(\frac{5 x+4}{x}\right)=2^{4} \text { or }\left(\log _{2}\left(\frac{2 x}{5 x+4}\right)\right)=\log _{2}\left(\frac{1}{8}\right) \\ & 16 x=5 x+4 \Rightarrow x=\text { (depends on previous Ms and must be this equation or equivalent) } \\ & x=\frac{4}{11} \text { or exact recurring decimal } 0.3 \dot{6} \text { after correct work } \end{aligned}$ | M1 <br> M1 <br> dM1 <br> A1 cso <br> (4) |
|  | $\log _{2}(2 x)+3=\log _{2}(5 x+4)$ <br> So $\log _{2}(2 x)+\log _{2}(8)=\log _{2}(5 x+4) \quad\left(3\right.$ replaced by $\left.\log _{2} 8\right)$ <br> Then $\log _{2}(16 x)=\log _{2}(5 x+4) \quad$ (addition law of $\operatorname{logs}$ ) <br> Then final M1 A1 as before | $\begin{array}{\|l} \hline 2^{\text {nd }} \text { M1 } \\ 1^{\text {st }} \text { M1 } \\ \text { dM1A1 } \\ \hline \end{array}$ |
| (ii) | $\begin{aligned} & \log _{a} y+\log _{a} 2^{3}=5 \\ & \log _{a} 8 y=5 \\ & y=\frac{1}{8} a^{5} \end{aligned}$ <br> Applies product law of logarithms. $y=\frac{1}{8} a^{5}$ | M1 <br> dM1 <br> A1cao |
|  | Notes for Question 7 |  |
| (i) (ii) | $1^{\text {st }}$ M1: Applying the subtraction or addition law of logarithms correctly to make two $\log$ terms in $x$ into one $\log$ term in $x$ <br> $2^{\text {nd }}$ M1: For RHS of either $2^{-3}, 2^{3}, 2^{4}$ or $\log _{2}\left(\frac{1}{8}\right), \log _{2} 8$ or $\log _{2} 16$ i.e. using connection between $\log$ base 2 and 2 to a power. This may follow an earlier error. Use of $3^{2}$ is M0 $3^{\text {rd }} \mathrm{dM} 1$ : Obtains correct linear equation in $x$. usually the one in the scheme and attempts $x=$ A1: cso Answer of $4 / 11$ with no suspect log work preceding this. <br> M1: Applies power law of $\log ^{2}$ arithms to replace $3 \log _{a} 2$ by $\log _{a} 2^{3}$ or $\log _{a} 8$ dM1: (should not be following M0) Uses addition law of ${\operatorname{logs~to~give~} \log _{a} 2^{3} y=5 \text { or } \log _{a} 8 y=5 ~}_{\text {d }}$ |  |
| (i) | Special case 1: $\log _{2}(2 x)=\log _{2}(5 x+4)-3 \Rightarrow \frac{\log _{2}(2 x)}{\log _{2}(5 x+4)}=-3 \Rightarrow \frac{2 x}{5 x+4}=2^{-3} \Rightarrow x=\frac{4}{11}$ or $\log _{2}(2 x)=\log _{2}(5 x+4)-3 \Rightarrow \frac{\log _{2}(2 x)}{\log _{2}(5 x+4)}=-3 \Rightarrow \log _{2} \frac{2 x}{5 x+4}=-3 \Rightarrow \frac{2 x}{5 x+4}=2^{-3} \Rightarrow x=\frac{4}{11}$ each attempt scores M0M1M1A0 - special case |  |
|  | Special case 2: <br> $\log _{2}(2 x)=\log _{2}(5 x+4)-3 \Rightarrow \log _{2} 2+\log _{2} x=\log _{2}(5 x+4)-3$, is M0 until the two log terms are combined to give $\log _{2}\left(\frac{5 x+4}{x}\right)=3+\log _{2} 2$. This earns M1 <br> Then $\left(\frac{5 x+4}{x}\right)=2^{4}$ or $\log _{2}\left(\frac{5 x+4}{x}\right)=\log _{2} 2^{4}$ gets second M1. Then scheme as before. |  |




| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 10. (a) | Equation of form $(x \pm 5)^{2}+(y \pm 9)^{2}=k, \quad k>0$ <br> Equation of form $(x-a)^{2}+(y-b)^{2}=5^{2}$, with values for $a$ and $b$ $(x+5)^{2}+(y-9)^{2}=25=5^{2}$ <br> $P(8,-7)$. Let centre of circle $=X(-5,9)$ $P X^{2}=(8-"-5 ")^{2}+(-7-" 9 ")^{2} \text { or } P X=\sqrt{(8--5)^{2}+(-7-9)^{2}}$ <br> $(P X=\sqrt{425}$ or $5 \sqrt{17}) \quad P T^{2}=(P X)^{2}-5^{2}$ with numerical $P X$ $P T\{=\sqrt{400}\}=20 \quad \text { (allow 20.0) }$ | M1 <br> M1 <br> A1 <br> (3) <br> M1 <br> dM1 <br> A1 cso <br> (3) <br> [6] |
| Alternative 2 for (a) | Equation of the form $x^{2}+y^{2} \pm 10 x \pm 18 y+c=0$ <br> Uses $a^{2}+b^{2}-5^{2}=c$ with their $a$ and $b$ or substitutes $(0,9)$ giving $+9^{2} \pm 2 b \times 9+c=0$ $x^{2}+y^{2}+10 x-18 y+81=0$ | M1 <br> M1 <br> A1 <br> (3) |
| Alternative 2 for (b) | An attempt to find the point $T$ may result in pages of algebra, but solution needs to reach $(-8,5)$ or $\left(\frac{-8}{17}, 11 \frac{2}{17}\right)$ to get first M1 (even if gradient is found first) <br> M1: Use either of the correct points with $P(8,-7)$ and distance between two points formula <br> A1: 20 | M1 <br> dM1 <br> A1cso <br> (3) |
| Alternative 3 for (b) | Substitutes (8,-7) into circle equation so $P T^{2}=8^{2}+(-7)^{2}+10 \times 8-18 \times(-7)+81$ Square roots to give $P T\{=\sqrt{400}\}=20$ | M1 dM1A1 (3) |
|  | Notes for Question 10 |  |
| (a) (b) | The three marks in (a) each require a circle equation - (see special cases which are not circles) M1: Uses coordinates of centre to obtain LHS of circle equation (RHS must be $r^{2}$ or $k>0$ or a positive value) <br> M1: Uses $r=5$ to obtain RHS of circle equation as 25 or $5^{2}$ <br> A1: correct circle equation in any equivalent form <br> Special cases $(x \pm 5)^{2}+(x \pm 9)^{2}=\left(5^{2}\right)$ is not a circle equation so M0M0A0 <br> Also $(x \pm 5)^{2}+(y-9)=\left(5^{2}\right)$ And $(x \pm 5)^{2}-(y \pm 9)^{2}=\left(5^{2}\right)$ are not circles and gain M0M0A0 <br> But $(x-0)^{2}+(y-9)^{2}=5^{2}$ gains M0M1A0 <br> M1: Attempts to find distance from their centre of circle to $P$ (or square of this value). If this is called $P T$ and given as answer this is M0. Solution may use letter other than $X$, as centre was not labelled in the question. <br> N.B. Distance from $(0,9)$ to $(8,-7)$ is incorrect method and is M0, followed by M0A0. <br> dM1: Applies the subtraction form of Pythagoras to find $P T$ or $P T^{2}$ (depends on previous method mark for distance from centre to $\boldsymbol{P}$ ) or uses appropriate complete method involving trigonometry A1: 20 cso |  |



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